## Performance Pillar

## P2 - Performance Management

## Wednesday 2 March 2011

## Instructions to candidates

| You are allowed three hours to answer this question paper. |
| :--- |
| You are allowed 20 minutes reading time before the examination begins <br> during which you should read the question paper and, if you wish, make <br> annotations on the question paper. However, you will not be allowed, under <br> any circumstances, open the answer book and start writing or use your <br> calculator during this reading time. |
| You are strongly advised to carefully read ALL the question requirements <br> before attempting the question concerned (that is all parts and/or sub- <br> questions). |
| ALL answers must be written in the answer book. Answers written on the <br> question paper will not be submitted for marking. |
| You should show all workings as marks are available for the method you use. |
| ALL QUESTIONS ARE comPULSORY. |
| Section A comprises 5 questions and is on pages 2 to 5. |
| Section B comprises 2 questions and is on pages 6 to 9. |
| Maths tables and formulae are provided on pages 11 to 14. |
| The list of verbs as published in the syllabus is given for reference on page <br> 15. |
| Write your candidate number, the paper number and examination subject title <br> in the spaces provided on the front of the answer book. Also write your <br> contact ID and name in the space provided in the right hand margin and seal <br> to close. |

Tick the appropriate boxes on the front of the answer book to indicate which questions you have answered.


SECTION A - 50 MARKS
[Note: The indicative time for answering this section is 90 minutes.]
ANSWER ALL FIVE QUESTIONS IN THIS SECTION. EACH QUESTION IS WORTH 10 MARKS. YOU SHOULD SHOW YOUR WORKINGS AS MARKS ARE AVAILABLE FOR THE METHOD YOU USE.

## Question One

The standard direct labour cost of one batch of 100 units of a product is $\$ 50.40$. This assumes a standard time of 4.2 hours, costing $\$ 12$ per hour. The standard time of 4.2 direct labour hours is the average time expected per batch based on a product life of 12,800 units or 128 batches. The expected time for the first batch was 20 hours and an $80 \%$ learning curve is expected to apply throughout the product's life.

The company has now completed the production of 32 batches of the product and the total actual direct labour cost was $\$ 3,493$. The following direct labour variances have also been calculated:

Direct labour rate \$85 Adverse
Direct labour efficiency \$891 Adverse
Further analysis has shown that the direct labour efficiency variance was caused solely by the actual rate of learning being different from that expected. However, the time taken for the first batch was 20 hours as expected.

## Required:

(a) Calculate the actual rate of learning that occurred.
(b) Assuming that the actual rate of learning and the actual labour rate continue throughout the life of the product, calculate the total direct labour cost that the company will incur during the life of the product.
(4 marks)
(Total for Question One = 10 marks)

## Question Two

PR currently uses a constant flow production system to manufacture components for the motor industry. The demand from the motor industry is higher in certain months of the year and lower in others. PR holds inventory so that it can supply the components as they are demanded. Increasingly, the costs to PR of holding inventory are having a significant effect on its profits and the management of PR are considering changing the production system to one that operates on a just-in-time (JIT) basis.

## Required:

(a) Explain the concepts of a JIT production system.
(4 marks)
(b) Explain TWO reasons why the profit of PR may NOT increase as a result of changing to a JIT production system.
(6 marks)
(Total for Question Two = 10 marks)

## Question Three

A college is preparing its budget for 2012. In previous years the director of the college has prepared the college budget without the participation of senior staff and presented it to the college board for approval.

Last year the college board criticised the director over the lack of participation of his senior staff in the preparation of the budget for 2011 and requested that for the 2012 budget the senior staff were to be involved.

## Required:

Discuss the potential advantages and disadvantages to the college of involving the senior staff in the budget preparation process.
(Total for Question Three = 10 marks)

## Question Four

KHL manufactures a single product and operates a budgetary control system that reports performance using variances on a monthly basis. The company has an agreement with a local supplier and calls off raw materials as and when required. Consequently there is no inventory of raw materials.
The following details have been extracted from the budget working papers for 2011:

|  | Annual Activity (units) |  |  |
| :--- | :---: | :---: | :---: |
|  | 50,000 | 70,000 | 90,000 |
|  | $\$ 000$ | $\$ 000$ | $\$ 000$ |
| Sales revenue | 3,200 | 4,480 | 5,760 |
|  |  |  |  |
| Direct materials (3 kgs per unit) | 600 | 840 | 1,080 |
| Direct labour (2 hours per unit) | 1,000 | 1,400 | 1,800 |
| Variable overhead (2 hours per unit) | 400 | 560 | 720 |
| Fixed overhead (2 hours per unit)* | 600 | 600 | 600 |

*The fixed overhead absorption rate of $\$ 5$ per hour was based on an annual budget of 60,000 units of the product being produced at a constant monthly rate throughout the year, with the fixed overhead cost being incurred in equal monthly amounts.

The following actual performance relates to February 2011:

|  | $\$$ | $\$$ |
| :--- | ---: | :---: |
| Sales revenue (5,700 units) |  | 330,600 |
|  | 70,680 |  |
| Direct materials (18,600 kgs) | 128,800 |  |
| Direct labour (11,500 hours) | 47,150 |  |
| Variable overhead (11,500 hours) | $\underline{60,000}$ |  |
| Fixed overhead absorbed | $\underline{15,630}$ | $\underline{291,630}$ |
| Finished goods inventory adjustment |  | 38,970 |
| Gross profit |  | $\underline{3,000}$ |
| Fixed overhead over-absorption |  | $\underline{41,970}$ |

For February 2011 budgeted sales were 6,000 units, the selling price variance was $\$ 34,200$ Adverse and the sales volume profit variance was \$4,200 Adverse. The actual fixed overhead incurred was $\$ 57,000$.
Budgeted profit for February 2011 was \$84,000.

## Required:

Prepare a statement for February 2011 that reconciles the budgeted profit of $\$ 84,000$ with the actual profit of $\$ 41,970$.
You should show the variances in as much detail as possible given the data provided.
(Total for Question Four = 10 marks)

## Question Five

ZX is a new banking organisation which is about to open its first branches. ZX believes that it needs to offer potential customers a new banking experience if it is to win customers from other banks.

Whereas other banks have focused on interest rates and levels of bank charges, ZX believes that quality and availability of service is an important factor in the choice made by customers.

## Required:

Explain how Total Quality Management (TQM) would enable ZX to gain competitive advantage in the banking sector.
(Total for Question Five = 10 marks)
(Total for Section A = 50 marks)

## End of Section A

Section B starts on page 6

SECTION B - 50 MARKS
[Note: The indicative time for answering this section is 90 minutes.]
ANSWER BOTH QUESTIONS IN THIS SECTION. EACH QUESTION IS WORTH 25 MARKS. YOU SHOULD SHOW YOUR WORKINGS AS MARKS ARE AVAILABLE FOR THE METHOD YOU USE.

## Question Six

WZ is a manufacturing company with two factories. The company's West factory currently produces a number of products. Four of these products use differing quantities of the same resources. Details of these four products and their resource requirements are as follows:

| Product | J | K | L | M |
| :---: | :---: | :---: | :---: | :---: |
|  | \$/unit | \$/unit | \$/unit | \$/unit |
| Selling price | 56 | 40 | 78 | 96 |
| Direct labour (\$8 per hour) | 20 | 16 | 24 | 20 |
| Direct material A (\$3 per litre) | 6 | 3 | 0 | 9 |
| Direct material B (\$5 per kg) | 10 | 0 | 15 | 20 |
| Variable overhead (see note 1) |  |  |  |  |
| Labour related | 1.25 | 1 | 1.50 | 1.25 |
| Machine related | 1.25 | 2 | 0.75 | 1 |
| Total variable cost | 38.50 | 22 | 41.25 | 51.25 |
| Other data: |  |  |  |  |
| Machine hours per unit | 5 | 8 | 3 | 4 |
| Maximum demand per week | 1,000 | 3,500 | 2,800 | 4,500 |

## Notes

1. An analysis of the variable overhead shows that some of it is caused by the number of labour hours and the remainder is caused by the number of machine hours.
2. Currently WZ purchases a component $P$ from an external supplier for $\$ 35$ per component. A single unit of this component is used in producing $N$ the company's only other product. Product $N$ is produced in WZ's other factory and does not use any of the resources identified above. Product $N$ currently yields a positive contribution. WZ could manufacture the component in its West factory, but to do so would require: 1 hour of direct labour, 0.5 machine hours, and 2 kgs of direct material B . WZ purchases 500 components per week. WZ could not produce the component in its other factory.
3. The purchasing director has recently advised you that the availability of direct materials $A$ and $B$ is to be restricted to 21,000 litres and $24,000 \mathrm{kgs}$ per week respectively. This restriction is unlikely to change for at least 10 weeks. No restrictions are expected on any other resources.
4. WZ does not hold inventory of either finished goods or raw materials.
5. WZ has already signed a contract, which must be fulfilled, to deliver the following units of its products each week for the next 10 weeks:

| Product | Contract units |
| :---: | :---: |
| J | 100 |
| K | 200 |
| L | 150 |
| M | 250 |

These quantities are in addition to the maximum demand identified above.

## Required:

(a) Calculate whether WZ should continue to purchase the component P or whether it should manufacture it internally during the next 10 weeks.
(11 marks)
(b) Prepare a statement to show the optimum weekly usage of the West factory's available resources.

Note: You are NOT required to use linear programming.
(c)
(i) Assuming no other changes, calculate the purchase price of the component $P$ at which your advice in part (a) above would change.
(ii) Explain TWO non-financial factors that should be considered before deciding whether or not to manufacture the component internally.
(d) If you were to solve part (b) above using linear programming state the following:

- The objective function
- The inequality for the material A constraint
- The inequality for the material $B$ constraint


## Section B continues on page 8

## Question Seven

The PZ Group comprises two companies: P Limited and Z Limited. Both companies manufacture similar items and are located in different regions of the same country. Return on Capital Employed (ROCE) is used as the group's performance measure and is also used to determine divisional managers' bonuses. The results of the two companies and of the group for the year ended $31^{\text {st }}$ December 2010 and the balance sheets at that date are as follows:

|  | $\begin{gathered} P \text { Limited } \\ \$ 000 \end{gathered}$ | $\begin{gathered} \text { Z Limited } \\ \$ 000 \end{gathered}$ | $\begin{gathered} \text { PZ Group } \\ \$ 000 \end{gathered}$ |
| :---: | :---: | :---: | :---: |
| Revenue | 200,000 | 220,000 | 400,000 |
| Cost of sales | 170,000 | 160,000 | 310,000 |
| Gross profit | 30,000 | 60,000 | 90,000 |
| Administration costs | 10,000 | 30,000 | 40,000 |
| Interest payable | 10,000 |  | 10,000 |
| Pre-tax profit | 10,000 | 30,000 | 40,000 |
| Non-current assets: |  |  |  |
| Original cost | 1,000,000 | 1,500,000 | 2,500,000 |
| Accumulated depreciation | 590,400 | 1,106,784 | 1,697,184 |
| Net book value | 409,600 | 393,216 | 802,816 |
| Net current assets | 50,000 | 60,000 | 110,000 |
|  | 459,600 | 453,216 | 912,816 |
| Non-current borrowings | 150,000 |  | 150,000 |
| Shareholders' funds | 309,600 | 453,216 | 762,816 |
| Capital employed | 459,600 | 453,216 | 912,816 |

## Notes

1. During the year $Z$ Limited sold goods to $P$ Limited that had cost $Z$ Limited $\$ 10,000$. The transactions relating to this sale have been eliminated from the PZ Group results stated above.
2. Both companies use the group depreciation policy of $20 \%$ per annum on a reducing balance basis for their non-current assets. Neither company made any additions or disposals of non-current assets during the year.

## Required:

(a) Calculate the Return on Capital Employed (ROCE) ratios for each of the two companies for the year and analyse these into their secondary ratio components of:
(i) Pre-tax profit \%
(ii) Asset Turnover
(b)
(i) Calculate Z's gross profit margin on its internal sales and compare this to the gross profit margin on its external sales.
(ii) Discuss the performance of the two companies EXCLUDING the effects of the intra group transactions.

Due to operational difficulties, the directors of the PZ Group are to impose a transfer pricing policy.
(c) Explain THREE factors that they should consider when setting the transfer pricing policy.

## End of question paper

## Maths tables and formulae are on pages 11 to 14

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## PRESENT VALUE TABLE

Present value of 1 unit of currency, that is $(1+r)^{-n}$ where $r=$ interest rate; $n=$ number of periods until payment or receipt.

| Periods | Interest rates (r) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ( $n$ ) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0705 | 0.666 | 0.630 | 0.596 | 0.564 |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 |
| 9 | 0.914 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.350 |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 |
| 16 | 0.853 | 0.728 | 0.623 | 0.534 | 0.458 | 0.394 | 0.339 | 0.292 | 0.252 | 0.218 |
| 17 | 0.844 | 0.714 | 0.605 | 0.513 | 0.436 | 0.371 | 0.317 | 0.270 | 0.231 | 0.198 |
| 18 | 0.836 | 0.700 | 0.587 | 0.494 | 0.416 | 0.350 | 0.296 | 0.250 | 0.212 | 0.180 |
| 19 | 0.828 | 0.686 | 0.570 | 0.475 | 0.396 | 0.331 | 0.277 | 0.232 | 0.194 | 0.164 |
| 20 | 0.820 | 0.673 | 0.554 | 0.456 | 0.377 | 0.312 | 0.258 | 0.215 | 0.178 | 0.149 |


| Periods |  |  |  |  |  |  |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| $(n)$ | Interest rates $(r)$ |  |  |  |  |  |  |  |  |  |  |
|  | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 |  |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 |  |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 |  |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 |  |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 |  |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 |  |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 |  |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 |  |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 |  |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 |  |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 |  |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 |  |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.079 | 0.065 |  |
| 16 | 0.188 | 0.163 | 0.141 | 0.123 | 0.107 | 0.093 | 0.081 | 0.071 | 0.062 | 0.054 |  |
| 17 | 0.170 | 0.146 | 0.125 | 0.108 | 0.093 | 0.080 | 0.069 | 0.060 | 0.052 | 0.045 |  |
| 18 | 0.153 | 0.130 | 0.111 | 0.095 | 0.081 | 0.069 | 0.059 | 0.051 | 0.044 | 0.038 |  |
| 19 | 0.138 | 0.116 | 0.098 | 0.083 | 0.070 | 0.060 | 0.051 | 0.043 | 0.037 | 0.031 |  |
| 20 | 0.124 | 0.104 | 0.087 | 0.073 | 0.061 | 0.051 | 0.043 | 0.037 | 0.031 | 0.026 |  |

Cumulative present value of 1 unit of currency per annum, Receivable or Payable at the end of each year for $n$ years $\frac{1-(1+r)^{-n}}{r}$

| Periods | Interest rates (r) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| ( $n$ ) | 1\% | 2\% | 3\% | 4\% | 5\% | 6\% | 7\% | 8\% | 9\% | 10\% |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 |
| 3 | 2.941 | 2.884 | 2.829 | 2.775 | 2.723 | 2.673 | 2.624 | 2.577 | 2.531 | 2.487 |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | 3.465 | 3.387 | 3.312 | 3.240 | 3.170 |
| 5 | 4.853 | 4.713 | 4.580 | 4.452 | 4.329 | 4.212 | 4.100 | 3.993 | 3.890 | 3.791 |
| 6 | 5.795 | 5.601 | 5.417 | 5.242 | 5.076 | 4.917 | 4.767 | 4.623 | 4.486 | 4.355 |
| 7 | 6.728 | 6.472 | 6.230 | 6.002 | 5.786 | 5.582 | 5.389 | 5.206 | 5.033 | 4.868 |
| 8 | 7.652 | 7.325 | 7.020 | 6.733 | 6.463 | 6.210 | 5.971 | 5.747 | 5.535 | 5.335 |
| 9 | 8.566 | 8.162 | 7.786 | 7.435 | 7.108 | 6.802 | 6.515 | 6.247 | 5.995 | 5.759 |
| 10 | 9.471 | 8.983 | 8.530 | 8.111 | 7.722 | 7.360 | 7.024 | 6.710 | 6.418 | 6.145 |
| 11 | 10.368 | 9.787 | 9.253 | 8.760 | 8.306 | 7.887 | 7.499 | 7.139 | 6.805 | 6.495 |
| 12 | 11.255 | 10.575 | 9.954 | 9.385 | 8.863 | 8.384 | 7.943 | 7.536 | 7.161 | 6.814 |
| 13 | 12.134 | 11.348 | 10.635 | 9.986 | 9.394 | 8.853 | 8.358 | 7.904 | 7.487 | 7.103 |
| 14 | 13.004 | 12.106 | 11.296 | 10.563 | 9.899 | 9.295 | 8.745 | 8.244 | 7.786 | 7.367 |
| 15 | 13.865 | 12.849 | 11.938 | 11.118 | 10.380 | 9.712 | 9.108 | 8.559 | 8.061 | 7.606 |
| 16 | 14.718 | 13.578 | 12.561 | 11.652 | 10.838 | 10.106 | 9.447 | 8.851 | 8.313 | 7.824 |
| 17 | 15.562 | 14.292 | 13.166 | 12.166 | 11.274 | 10.477 | 9.763 | 9.122 | 8.544 | 8.022 |
| 18 | 16.398 | 14.992 | 13.754 | 12.659 | 11.690 | 10.828 | 10.059 | 9.372 | 8.756 | 8.201 |
| 19 | 17.226 | 15.679 | 14.324 | 13.134 | 12.085 | 11.158 | 10.336 | 9.604 | 8.950 | 8.365 |
| 20 | 18.046 | 16.351 | 14.878 | 13.590 | 12.462 | 11.470 | 10.594 | 9.818 | 9.129 | 8.514 |


| Periods <br> (n) | Interest rates (r) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 |
| 3 | 2.444 | 2.402 | 2.361 | 2.322 | 2.283 | 2.246 | 2.210 | 2.174 | 2.140 | 2.106 |
| 4 | 3.102 | 3.037 | 2.974 | 2.914 | 2.855 | 2.798 | 2.743 | 2.690 | 2.639 | 2.589 |
| 5 | 3.696 | 3.605 | 3.517 | 3.433 | 3.352 | 3.274 | 3.199 | 3.127 | 3.058 | 2.991 |
| 6 | 4.231 | 4.111 | 3.998 | 3.889 | 3.784 | 3.685 | 3.589 | 3.498 | 3.410 | 3.326 |
| 7 | 4.712 | 4.564 | 4.423 | 4.288 | 4.160 | 4.039 | 3.922 | 3.812 | 3.706 | 3.605 |
| 8 | 5.146 | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | 4.207 | 4.078 | 3.954 | 3.837 |
| 9 | 5.537 | 5.328 | 5.132 | 4.946 | 4.772 | 4.607 | 4.451 | 4.303 | 4.163 | 4.031 |
| 10 | 5.889 | 5.650 | 5.426 | 5.216 | 5.019 | 4.833 | 4.659 | 4.494 | 4.339 | 4.192 |
| 11 | 6.207 | 5.938 | 5.687 | 5.453 | 5.234 | 5.029 | 4.836 | 4.656 | 4.486 | 4.327 |
| 12 | 6.492 | 6.194 | 5.918 | 5.660 | 5.421 | 5.197 | 4.988 | 7.793 | 4.611 | 4.439 |
| 13 | 6.750 | 6.424 | 6.122 | 5.842 | 5.583 | 5.342 | 5.118 | 4.910 | 4.715 | 4.533 |
| 14 | 6.982 | 6.628 | 6.302 | 6.002 | 5.724 | 5.468 | 5.229 | 5.008 | 4.802 | 4.611 |
| 15 | 7.191 | 6.811 | 6.462 | 6.142 | 5.847 | 5.575 | 5.324 | 5.092 | 4.876 | 4.675 |
| 16 | 7.379 | 6.974 | 6.604 | 6.265 | 5.954 | 5.668 | 5.405 | 5.162 | 4.938 | 4.730 |
| 17 | 7.549 | 7.120 | 6.729 | 6.373 | 6.047 | 5.749 | 5.475 | 5.222 | 4.990 | 4.775 |
| 18 | 7.702 | 7.250 | 6.840 | 6.467 | 6.128 | 5.818 | 5.534 | 5.273 | 5.033 | 4.812 |
| 19 | 7.839 | 7.366 | 6.938 | 6.550 | 6.198 | 5.877 | 5.584 | 5.316 | 5.070 | 4.843 |
| 20 | 7.963 | 7.469 | 7.025 | 6.623 | 6.259 | 5.929 | 5.628 | 5.353 | 5.101 | 4.870 |

## PROBABILITY

$A \cup B=A$ or $B . \quad A \cap B=\boldsymbol{A}$ and $\boldsymbol{B}$ (overlap).
$P(B \mid A)=$ probability of $B$, given $A$.

## Rules of Addition

If $A$ and $B$ are mutually exclusive:
If $A$ and $B$ are not mutually exclusive:

$$
\begin{aligned}
& P(A \cup B)=P(A)+P(B) \\
& P(A \cup B)=P(A)+P(B)-P(A \cap B)
\end{aligned}
$$

## Rules of Multiplication

If $A$ and $B$ are independent::
$P(A \cap B)=P(A) * P(B)$
If $A$ and $B$ are not independent:
$P(A \cap B)=P(A) * P(B \mid A)$
$E(X)=\sum$ (probability * payoff)

## DESCRIPTIVE STATISTICS

Arithmetic Mean

$$
\bar{x}=\frac{\sum x}{n} \quad \bar{x}=\frac{\sum f x}{\sum f} \quad \text { (frequency distribution) }
$$

Standard Deviation

$$
S D=\sqrt{\frac{\sum(x-\bar{x})^{2}}{n}} \quad S D=\sqrt{\frac{\sum \mathrm{fx}^{2}-\overline{x^{2}}}{\sum \mathrm{f}}} \text { (frequency distribution) }
$$

## INDEX NUMBERS

Price relative $=100 * P_{1} / P_{0} \quad$ Quantity relative $=100 * Q_{1} / Q_{0}$
Price: $\quad \frac{\sum w *\left(\frac{P_{1}}{P_{o}}\right)}{\sum w} \times 100$
Quantity: $\quad \frac{\sum w *\left(\frac{Q_{1}}{Q_{0}}\right)}{\sum w} \times 100$

## TIME SERIES

Additive Model

$$
\text { Series }=\text { Trend }+ \text { Seasonal + Random }
$$

Multiplicative Model

$$
\text { Series }=\text { Trend * Seasonal * Random }
$$

## FINANCIAL MATHEMATICS

## Compound Interest (Values and Sums)

Future Value $S$, of a sum of $X$, invested for $n$ periods, compounded at $r \%$ interest

$$
S=X[1+r]^{n}
$$

## Annuity

Present value of an annuity of $£ 1$ per annum receivable or payable for $n$ years, commencing in one year, discounted at $r \%$ per annum:

$$
\mathrm{PV}=\frac{1}{r}\left[1-\frac{1}{[1+r]^{n}}\right]
$$

## Perpetuity

Present value of $£ 1$ per annum, payable or receivable in perpetuity, commencing in one year, discounted at $r \%$ per annum:

$$
\mathrm{PV}=\frac{1}{r}
$$

## LEARNING CURVE

$$
Y_{x}=a X^{b}
$$

where:
$Y_{X}=$ the cumulative average time per unit to produce $X$ units;
$a=$ the time required to produce the first unit of output;
$X=$ the cumulative number of units;
$b=$ the index of learning.
The exponent $b$ is defined as the log of the learning curve improvement rate divided by $\log 2$.

## INVENTORY MANAGEMENT

Economic Order Quantity

$$
\mathrm{EOQ}=\sqrt{\frac{2 C_{0} D}{C_{h}}}
$$

where: $\mathrm{C}_{0}=$ cost of placing an order
$\mathrm{C}_{\mathrm{h}}=$ cost of holding one unit in inventory for one year
D $=$ annual demand

## LIST OF VERBS USED IN THE QUESTION REQUIREMENTS

A list of the learning objectives and verbs that appear in the syllabus and in the question requirements for each question in this paper.

It is important that you answer the question according to the definition of the verb.

| LEARNING OBJECTIVE | VERBS USED | DEFINITION |
| :---: | :---: | :---: |
| Level 1 - KNOWLEDGE |  |  |
| What you are expected to know. | List | Make a list of |
|  | State | Express, fully or clearly, the details/facts of |
|  | Define | Give the exact meaning of |
| Level 2 - COMPREHENSION |  |  |
| What you are expected to understand. | Describe | Communicate the key features |
|  | Distinguish | Highlight the differences between |
|  | Explain | Make clear or intelligible/State the meaning or purpose of |
|  | Identify | Recognise, establish or select after consideration |
|  | Illustrate | Use an example to describe or explain something |
| Level 3 - APPLICATION |  |  |
| How you are expected to apply your knowledge. | Apply | Put to practical use |
|  | Calculate | Ascertain or reckon mathematically |
|  | Demonstrate | Prove with certainty or to exhibit by practical means |
|  | Prepare | Make or get ready for use |
|  | Reconcile | Make or prove consistent/compatible |
|  | Solve | Find an answer to |
|  | Tabulate | Arrange in a table |
| Level 4 - ANALYSIS |  |  |
| How are you expected to analyse the detail of what you have learned. |  |  |
|  | Categorise | Place into a defined class or division |
|  | Compare and contrast | Show the similarities and/or differences between |
|  | Construct | Build up or compile |
|  | Discuss | Examine in detail by argument |
|  | Interpret | Translate into intelligible or familiar terms |
|  | Prioritise | Place in order of priority or sequence for action |
|  | Produce | Create or bring into existence |
| Level 5 - EVALUATION |  |  |
| How are you expected to use your learning to evaluate, make decisions or recommendations. |  |  |
|  | Evaluate | Appraise or assess the value of |
|  | Recommend | Advise on a course of action |

## Performance Pillar

## Management Level Paper

## P2 - Performance Management

## March 2011

