## Performance Pillar

## P2 - Performance Management

## Thursday 29 August 2013

## Instructions to candidates

| You are allowed three hours to answer this question paper. |
| :--- |
| You are allowed 20 minutes reading time before the examination begins <br> during which you should read the question paper and, if you wish, make <br> annotations on the question paper. However, you will not be allowed, under <br> any circumstances, to open the answer book and start writing or use your <br> calculator during this reading time. <br> You are strongly advised to carefully read ALL the question requirements <br> before attempting the question concerned (that is all parts and/or sub- <br> questions). <br> ALL answers must be written in the answer book. Answers written on the <br> question paper will not be submitted for marking. <br> You should show all workings as marks are available for the method you use. <br> ALL QUESTIONS ARE comPULSORY. <br> Section A comprises 5 questions and is on pages 2 to 4. <br> Section B comprises 2 questions and is on pages 6 to 9. <br> Maths tables and formulae are provided on pages 11 to 14. <br> The list of verbs as published in the syllabus is given for reference on page <br> 15. <br> Write your candidate number, the paper number and examination subject title <br> in the spaces provided on the front of the answer book. Also write your <br> contact ID and name in the space provided in the right hand margin and seal <br> to close. <br> Tick the appropriate boxes on the front of the answer book to indicate which <br> questions you have answered. |

# SECTION A - 50 MARKS <br> [You are advised to spend no longer than 18 minutes on each question in this section.] 

ANSWER ALL FIVE QUESTIONS IN THIS SECTION. EACH QUESTION IS WORTH 10 MARKS. YOU SHOULD SHOW YOUR WORKINGS AS MARKS ARE AVAILABLE FOR THE METHOD YOU USE.

## Question One

The standard selling price and costs per unit of a new product for the first period are shown below:

|  |  | $\$$ |
| :--- | :---: | :---: |
| Selling price | 750 |  |
| Materials | 6 kg at $\$ 50$ per kg | 300 |
| Labour (see below) | 20 hours at $\$ 10$ per hour | 200 |
| Variable overheads | 25 machine hours at $\$ 4$ per machine hour | 100 |
| Fixed overheads (see below) |  | 120 |

## Labour hours

The labour hours are the average labour hours per unit based on the budgeted output for the period of 128 units and the assumption that a $90 \%$ learning curve will apply throughout the period. The learning index for a $90 \%$ learning curve is -0.152 .

## Fixed overheads

The fixed overheads are specific fixed overheads for this product and the absorption rate was based on the budgeted output for the period of 128 units.

## Required:

(a) Calculate the sensitivity of the budgeted profit for the period for this product to a change in the price per kg of materials.
(2 marks)
(b) Calculate the budgeted labour hours for the first unit of this product to be produced.
(c) Calculate the sensitivity of the budgeted profit for the period for this product to a change in the rate of learning.

Note: all workings must be shown.

## Question Two

A factory uses a standard absorption costing system. The fixed production overhead absorption rate is based on labour hours. Extracts from the budgeted and actual results for the previous period are shown below:

|  | Budget | Actual |
| :--- | ---: | ---: |
| Output (units) | 1,500 | 1,600 |
| Fixed production overhead | $\$ 300,000$ | $\$ 310,000$ |
| Labour hours | 600 | 580 |

## Required:

(a) Calculate:
(i) The fixed production overhead expenditure variance
(ii) The fixed production overhead volume variance
(3 marks)

The factory is thinking of introducing an activity based costing system. An analysis of the fixed production overheads for the previous period showed that included in the budgeted fixed production overheads of $\$ 300,000$ was $\$ 72,000$ for materials handling. Costs for materials handling are incurred when materials are shipped from the storage area to the processing plant. Further analysis revealed:

|  | Budget | Actual |
| :--- | :--- | :---: |
| Materials handling costs | $\$ 72,000$ | $\$ 69,000$ |
| Number of material shipments | 90 | 85 |
| Total quantity of materials shipped | 360 tonne | 348 tonne |

## Required:

(b) Calculate using activity based costing principles:
(i) The materials handling shipment expenditure variance
(ii) The materials handling shipment efficiency variance

## Question Three

## Required:

Discuss how activity based costing could improve the linkage between cost control and responsibility accounting at each of the four levels of the activity based costing hierarchy of activities.
(Total for Question Three = 10 marks)

## Question Four

## Required:

Compare and contrast feedforward and feedback controls by using a budgeting system to explain your points.
(Total for Question Four = 10 marks)

## Question Five

Many service organisations, for example banks, have outsourced their customer liaison and support service operations to "inbound call centres". Inbound call centres deal with product support or information enquiries from customers.

## Required:

Explain, in the context of the modern business environment, the advantages and disadvantages of outsourcing customer liaison and product support to "inbound call centres".
(Total for Question Five = 10 marks)
(Total for Section A = 50 marks)

## End of Section A. Section B starts on page 6

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## SECTION B - 50 MARKS

[You are advised to spend no longer than 45 minutes on each question in this section.]

## ANSWER BOTH QUESTIONS IN THIS SECTION. EACH QUESTION IS WORTH 25 MARKS. YOU SHOULD SHOW YOUR WORKINGS AS MARKS ARE AVAILABLE FOR THE METHOD YOU USE.

## Question Six

A company produces three products ( $\mathrm{X}, \mathrm{Y}$ and Z ) from the same resources (but in different quantities). Extracts from the original budget for Month 11 are shown below:

|  | X | Y | Z |
| :--- | ---: | ---: | ---: |
| Selling price (\$ per unit) | 24 | 41 | 42 |
| Total cost (\$ per unit) | 20 | 20 | 35 |
| Labour hours per unit | 0.5 | 1.5 | 1.5 |
| Machine hours per unit | 1 | 2 | 0.75 |
| Production and sales (units) | 10,000 | 6,000 | 10,000 |

Variable costs are $40 \%$ of the total cost of each unit.
Fixed costs are absorbed at the rate of $150 \%$ of variable costs based on the budgeted production quantities as shown above.

It has now become known that during Month 11 essential maintenance work will have to be carried out. This will limit the availability of resources to:

Labour hours: 12,500 hours
Machine hours: 30,000 hours

## Required:

(a) Produce, using marginal costing principles, a columnar statement that shows the profit maximising production plan for Month 11 and the resulting profit or loss.
(b) Calculate the three shadow prices for labour hours. Your answer must state the range of labour hours that each shadow price covers.
(5 marks)

Marketing intelligence has now revealed that a new competitor is about to enter the market in Month 11 with a product that is much better than Product Y . It has therefore been decided that production of Product $Y$ will stop immediately. The competitor will also sell products that will have an impact on the demand for Products $X$ and $Z$.

Further work by the Marketing Department has revealed the relationships between the selling price and the monthly demand for Product X, and also for Product Z, as shown in the table below. There is no relationship between Product $X$ and Product $Z$ other than they use the same resources. The products must be produced separately, each in batches of 1,000 units.

|  | Selling price (\$) |  |
| :---: | :---: | :---: |
| Demand (units) | Product X | Product Z |
| 2,000 | 28 | 66 |
| 4,000 | 27 | 60 |
| 6,000 | 26 | 54 |
| 8,000 | 25 | 48 |
| 10,000 | 24 | 42 |
| 12,000 | 23 | 36 |
| 14,000 | 22 | 30 |
| 16,000 | 21 | 24 |

The table should be interpreted as follows:
If the selling price of Product $X$ was set at $\$ 28$ then up to 2,000 units could be sold. To sell more than 2,000 units it would be necessary to reduce the price. For example, if the price was reduced to $\$ 25$ per unit up to 8,000 units could be sold. The only selling prices that would be used are those shown in the table.

## Required:

## (c) Calculate:

(i) The revised optimum production plan for Products $X$ and $Z$.
(ii) The total contribution that the plan in (c)(i) would earn.

## Question Seven

HPR harvests, processes and roasts coffee beans. The company has two divisions
Division $\mathbf{P}$ is located in Country $Y$. It harvests and processes coffee beans. The processed coffee beans are sold to Division R and external customers.

Division R is located in Country Z. It roasts processed coffee beans and then sells them to external customers.

Countries $Y$ and $Z$ use the same currency but have different taxation rates.
The budgeted information for the next year is as follows:

## Division $\mathbf{P}$

| Capacity | 1,000 tonnes |
| :--- | :--- |
| External demand for processed coffee beans | 800 tonnes |
| Demand from Division R for processed coffee beans | 625 tonnes |
| External market selling price for processed coffee beans | $\$ 11,000$ per tonne |
| Variable costs | $\$ 7,000$ per tonne |
| Annual fixed costs | $\$ 1,500,000$ |

## Division R

Sales of roasted coffee beans
Market selling price for roasted coffee beans
500 tonnes
\$20,000 per tonne
The production of 1 tonne of roasted coffee beans requires an input of 1.25 tonnes of processed coffee beans. The cost of roasting is $\$ 2,000$ per tonne of input plus annual fixed costs of $\$ 1,000,000$.

## Transfer Pricing Policy of HPR

Division P must satisfy the demand from Division R for processed coffee beans before selling any to external customers.

The transfer price for the processed coffee beans is variable cost plus 10\% per tonne.

## Taxation

The rate of taxation on company profits is $45 \%$ in Country $Y$ and $25 \%$ in Country $Z$.

## Required:

(a)
(i) Produce statements that show the budgeted profit after tax for the next year for each of the two divisions. Your profit statements should show sales and costs split into external sales and internal transfers where appropriate.
(ii) Discuss the potential tax consequences of HPR's current transfer pricing policy.
(b) Produce statements that show the budgeted contributions that would be earned by each of the two divisions if HPR's head office changed its policy to state that transfers must be made at opportunity cost. Your statements should show sales and costs split into external sales and internal transfers where appropriate.
(6 marks)
(c) Explain TWO behavioural issues that could arise as a result of the head office of HPR imposing transfer prices instead of allowing the divisional managers to set the prices.

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## PRESENT VALUE TABLE

Present value of 1 unit of currency, that is $(1+r)^{-n}$ where $r=$ interest rate; $n=$ number of periods until payment or receipt.

| Periods |  |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| $(n)$ | Interest rates $(r)$ |  |  |  |  |  |  |  |  |  |  |
|  | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 |  |
| 2 | 0.980 | 0.961 | 0.943 | 0.925 | 0.907 | 0.890 | 0.873 | 0.857 | 0.842 | 0.826 |  |
| 3 | 0.971 | 0.942 | 0.915 | 0.889 | 0.864 | 0.840 | 0.816 | 0.794 | 0.772 | 0.751 |  |
| 4 | 0.961 | 0.924 | 0.888 | 0.855 | 0.823 | 0.792 | 0.763 | 0.735 | 0.708 | 0.683 |  |
| 5 | 0.951 | 0.906 | 0.863 | 0.822 | 0.784 | 0.747 | 0.713 | 0.681 | 0.650 | 0.621 |  |
| 6 | 0.942 | 0.888 | 0.837 | 0.790 | 0.746 | 0705 | 0.666 | 0.630 | 0.596 | 0.564 |  |
| 7 | 0.933 | 0.871 | 0.813 | 0.760 | 0.711 | 0.665 | 0.623 | 0.583 | 0.547 | 0.513 |  |
| 8 | 0.923 | 0.853 | 0.789 | 0.731 | 0.677 | 0.627 | 0.582 | 0.540 | 0.502 | 0.467 |  |
| 9 | 0.914 | 0.837 | 0.766 | 0.703 | 0.645 | 0.592 | 0.544 | 0.500 | 0.460 | 0.424 |  |
| 10 | 0.905 | 0.820 | 0.744 | 0.676 | 0.614 | 0.558 | 0.508 | 0.463 | 0.422 | 0.386 |  |
| 11 | 0.896 | 0.804 | 0.722 | 0.650 | 0.585 | 0.527 | 0.475 | 0.429 | 0.388 | 0.350 |  |
| 12 | 0.887 | 0.788 | 0.701 | 0.625 | 0.557 | 0.497 | 0.444 | 0.397 | 0.356 | 0.319 |  |
| 13 | 0.879 | 0.773 | 0.681 | 0.601 | 0.530 | 0.469 | 0.415 | 0.368 | 0.326 | 0.290 |  |
| 14 | 0.870 | 0.758 | 0.661 | 0.577 | 0.505 | 0.442 | 0.388 | 0.340 | 0.299 | 0.263 |  |
| 15 | 0.861 | 0.743 | 0.642 | 0.555 | 0.481 | 0.417 | 0.362 | 0.315 | 0.275 | 0.239 |  |
| 16 | 0.853 | 0.728 | 0.623 | 0.534 | 0.458 | 0.394 | 0.339 | 0.292 | 0.252 | 0.218 |  |
| 17 | 0.844 | 0.714 | 0.605 | 0.513 | 0.436 | 0.371 | 0.317 | 0.270 | 0.231 | 0.198 |  |
| 18 | 0.836 | 0.700 | 0.587 | 0.494 | 0.416 | 0.350 | 0.296 | 0.250 | 0.212 | 0.180 |  |
| 19 | 0.828 | 0.686 | 0.570 | 0.475 | 0.396 | 0.331 | 0.277 | 0.232 | 0.194 | 0.164 |  |
| 20 | 0.820 | 0.673 | 0.554 | 0.456 | 0.377 | 0.312 | 0.258 | 0.215 | 0.178 | 0.149 |  |


| Periods | Interest rates $(r)$ |  |  |  |  |  |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :---: |
| $(n)$ | $11 \%$ | $12 \%$ | $13 \%$ | $14 \%$ | $15 \%$ | $16 \%$ | $17 \%$ | $18 \%$ | $19 \%$ | $20 \%$ |  |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 |  |
| 2 | 0.812 | 0.797 | 0.783 | 0.769 | 0.756 | 0.743 | 0.731 | 0.718 | 0.706 | 0.694 |  |
| 3 | 0.731 | 0.712 | 0.693 | 0.675 | 0.658 | 0.641 | 0.624 | 0.609 | 0.593 | 0.579 |  |
| 4 | 0.659 | 0.636 | 0.613 | 0.592 | 0.572 | 0.552 | 0.534 | 0.516 | 0.499 | 0.482 |  |
| 5 | 0.593 | 0.567 | 0.543 | 0.519 | 0.497 | 0.476 | 0.456 | 0.437 | 0.419 | 0.402 |  |
| 6 | 0.535 | 0.507 | 0.480 | 0.456 | 0.432 | 0.410 | 0.390 | 0.370 | 0.352 | 0.335 |  |
| 7 | 0.482 | 0.452 | 0.425 | 0.400 | 0.376 | 0.354 | 0.333 | 0.314 | 0.296 | 0.279 |  |
| 8 | 0.434 | 0.404 | 0.376 | 0.351 | 0.327 | 0.305 | 0.285 | 0.266 | 0.249 | 0.233 |  |
| 9 | 0.391 | 0.361 | 0.333 | 0.308 | 0.284 | 0.263 | 0.243 | 0.225 | 0.209 | 0.194 |  |
| 10 | 0.352 | 0.322 | 0.295 | 0.270 | 0.247 | 0.227 | 0.208 | 0.191 | 0.176 | 0.162 |  |
| 11 | 0.317 | 0.287 | 0.261 | 0.237 | 0.215 | 0.195 | 0.178 | 0.162 | 0.148 | 0.135 |  |
| 12 | 0.286 | 0.257 | 0.231 | 0.208 | 0.187 | 0.168 | 0.152 | 0.137 | 0.124 | 0.112 |  |
| 13 | 0.258 | 0.229 | 0.204 | 0.182 | 0.163 | 0.145 | 0.130 | 0.116 | 0.104 | 0.093 |  |
| 14 | 0.232 | 0.205 | 0.181 | 0.160 | 0.141 | 0.125 | 0.111 | 0.099 | 0.088 | 0.078 |  |
| 15 | 0.209 | 0.183 | 0.160 | 0.140 | 0.123 | 0.108 | 0.095 | 0.084 | 0.079 | 0.065 |  |
| 16 | 0.188 | 0.163 | 0.141 | 0.123 | 0.107 | 0.093 | 0.081 | 0.071 | 0.062 | 0.054 |  |
| 17 | 0.170 | 0.146 | 0.125 | 0.108 | 0.093 | 0.080 | 0.069 | 0.060 | 0.052 | 0.045 |  |
| 18 | 0.153 | 0.130 | 0.111 | 0.095 | 0.081 | 0.069 | 0.059 | 0.051 | 0.044 | 0.038 |  |
| 19 | 0.138 | 0.116 | 0.098 | 0.083 | 0.070 | 0.060 | 0.051 | 0.043 | 0.037 | 0.031 |  |
| 20 | 0.124 | 0.104 | 0.087 | 0.073 | 0.061 | 0.051 | 0.043 | 0.037 | 0.031 | 0.026 |  |

Cumulative present value of 1 unit of currency per annum, Receivable or Payable at the end of each year for $n$ years $\frac{1-(1+r)^{-n}}{r}$

| Periods | Interest rates $(r)$ |  |  |  |  |  |  |  |  |  |  |
| :---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | ---: | :--- | :---: |
| $(n)$ | $1 \%$ | $2 \%$ | $3 \%$ | $4 \%$ | $5 \%$ | $6 \%$ | $7 \%$ | $8 \%$ | $9 \%$ | $10 \%$ |  |
| 1 | 0.990 | 0.980 | 0.971 | 0.962 | 0.952 | 0.943 | 0.935 | 0.926 | 0.917 | 0.909 |  |
| 2 | 1.970 | 1.942 | 1.913 | 1.886 | 1.859 | 1.833 | 1.808 | 1.783 | 1.759 | 1.736 |  |
| 3 | 2.941 | 2.884 | 2.829 | 2.775 | 2.723 | 2.673 | 2.624 | 2.577 | 2.531 | 2.487 |  |
| 4 | 3.902 | 3.808 | 3.717 | 3.630 | 3.546 | 3.465 | 3.387 | 3.312 | 3.240 | 3.170 |  |
| 5 | 4.853 | 4.713 | 4.580 | 4.452 | 4.329 | 4.212 | 4.100 | 3.993 | 3.890 | 3.791 |  |
| 6 | 5.795 | 5.601 | 5.417 | 5.242 | 5.076 | 4.917 | 4.767 | 4.623 | 4.486 | 4.355 |  |
| 7 | 6.728 | 6.472 | 6.230 | 6.002 | 5.786 | 5.582 | 5.389 | 5.206 | 5.033 | 4.868 |  |
| 8 | 7.652 | 7.325 | 7.020 | 6.733 | 6.463 | 6.210 | 5.971 | 5.747 | 5.535 | 5.335 |  |
| 9 | 8.566 | 8.162 | 7.786 | 7.435 | 7.108 | 6.802 | 6.515 | 6.247 | 5.995 | 5.759 |  |
| 10 | 9.471 | 8.983 | 8.530 | 8.111 | 7.722 | 7.360 | 7.024 | 6.710 | 6.418 | 6.145 |  |
| 11 | 10.368 | 9.787 | 9.253 | 8.760 | 8.306 | 7.887 | 7.499 | 7.139 | 6.805 | 6.495 |  |
| 12 | 11.255 | 10.575 | 9.954 | 9.385 | 8.863 | 8.384 | 7.943 | 7.536 | 7.161 | 6.814 |  |
| 13 | 12.134 | 11.348 | 10.635 | 9.986 | 9.394 | 8.853 | 8.358 | 7.904 | 7.487 | 7.103 |  |
| 14 | 13.004 | 12.106 | 11.296 | 10.563 | 9.899 | 9.295 | 8.745 | 8.244 | 7.786 | 7.367 |  |
| 15 | 13.865 | 12.849 | 11.938 | 11.118 | 10.380 | 9.712 | 9.108 | 8.559 | 8.061 | 7.606 |  |
| 16 | 14.718 | 13.578 | 12.561 | 11.652 | 10.838 | 10.106 | 9.447 | 8.851 | 8.313 | 7.824 |  |
| 17 | 15.562 | 14.292 | 13.166 | 12.166 | 11.274 | 10.477 | 9.763 | 9.122 | 8.544 | 8.022 |  |
| 18 | 16.398 | 14.992 | 13.754 | 12.659 | 11.690 | 10.828 | 10.059 | 9.372 | 8.756 | 8.201 |  |
| 19 | 17.226 | 15.679 | 14.324 | 13.134 | 12.085 | 11.158 | 10.336 | 9.604 | 8.950 | 8.365 |  |
| 20 | 18.046 | 16.351 | 14.878 | 13.590 | 12.462 | 11.470 | 10.594 | 9.818 | 9.129 | 8.514 |  |


| Periods <br> (n) | Interest rates (r) |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 11\% | 12\% | 13\% | 14\% | 15\% | 16\% | 17\% | 18\% | 19\% | 20\% |
| 1 | 0.901 | 0.893 | 0.885 | 0.877 | 0.870 | 0.862 | 0.855 | 0.847 | 0.840 | 0.833 |
| 2 | 1.713 | 1.690 | 1.668 | 1.647 | 1.626 | 1.605 | 1.585 | 1.566 | 1.547 | 1.528 |
| 3 | 2.444 | 2.402 | 2.361 | 2.322 | 2.283 | 2.246 | 2.210 | 2.174 | 2.140 | 2.106 |
| 4 | 3.102 | 3.037 | 2.974 | 2.914 | 2.855 | 2.798 | 2.743 | 2.690 | 2.639 | 2.589 |
| 5 | 3.696 | 3.605 | 3.517 | 3.433 | 3.352 | 3.274 | 3.199 | 3.127 | 3.058 | 2.991 |
| 6 | 4.231 | 4.111 | 3.998 | 3.889 | 3.784 | 3.685 | 3.589 | 3.498 | 3.410 | 3.326 |
| 7 | 4.712 | 4.564 | 4.423 | 4.288 | 4.160 | 4.039 | 3.922 | 3.812 | 3.706 | 3.605 |
| 8 | 5.146 | 4.968 | 4.799 | 4.639 | 4.487 | 4.344 | 4.207 | 4.078 | 3.954 | 3.837 |
| 9 | 5.537 | 5.328 | 5.132 | 4.946 | 4.772 | 4.607 | 4.451 | 4.303 | 4.163 | 4.031 |
| 10 | 5.889 | 5.650 | 5.426 | 5.216 | 5.019 | 4.833 | 4.659 | 4.494 | 4.339 | 4.192 |
| 11 | 6.207 | 5.938 | 5.687 | 5.453 | 5.234 | 5.029 | 4.836 | 4.656 | 4.486 | 4.327 |
| 12 | 6.492 | 6.194 | 5.918 | 5.660 | 5.421 | 5.197 | 4.988 | 4.793 | 4.611 | 4.439 |
| 13 | 6.750 | 6.424 | 6.122 | 5.842 | 5.583 | 5.342 | 5.118 | 4.910 | 4.715 | 4.533 |
| 14 | 6.982 | 6.628 | 6.302 | 6.002 | 5.724 | 5.468 | 5.229 | 5.008 | 4.802 | 4.611 |
| 15 | 7.191 | 6.811 | 6.462 | 6.142 | 5.847 | 5.575 | 5.324 | 5.092 | 4.876 | 4.675 |
| 16 | 7.379 | 6.974 | 6.604 | 6.265 | 5.954 | 5.668 | 5.405 | 5.162 | 4.938 | 4.730 |
| 17 | 7.549 | 7.120 | 6.729 | 6.373 | 6.047 | 5.749 | 5.475 | 5.222 | 4.990 | 4.775 |
| 18 | 7.702 | 7.250 | 6.840 | 6.467 | 6.128 | 5.818 | 5.534 | 5.273 | 5.033 | 4.812 |
| 19 | 7.839 | 7.366 | 6.938 | 6.550 | 6.198 | 5.877 | 5.584 | 5.316 | 5.070 | 4.843 |
| 20 | 7.963 | 7.469 | 7.025 | 6.623 | 6.259 | 5.929 | 5.628 | 5.353 | 5.101 | 4.870 |

## PROBABILITY

$A \cup B=A$ or $B . \quad A \cap B=A$ and $B$ (overlap).
$P(B \mid A)=$ probability of $B$, given $A$.

## Rules of Addition

If $A$ and $B$ are mutually exclusive:
If $A$ and $B$ are not mutually exclusive:

$$
\begin{aligned}
& P(A \cup B)=P(A)+P(B) \\
& P(A \cup B)=P(A)+P(B)-P(A \cap B)
\end{aligned}
$$

## Rules of Multiplication

If $A$ and $B$ are independent:

$$
\begin{aligned}
& P(A \cap B)=P(A) * P(B) \\
& P(A \cap B)=P(A) * P(B \mid A)
\end{aligned}
$$

If $A$ and $B$ are not independent:
$E(X)=\sum$ (probability * payoff)

## DESCRIPTIVE STATISTICS

Arithmetic Mean

$$
\bar{x}=\frac{\sum x}{n} \quad \bar{x}=\frac{\sum f x}{\sum f} \quad \text { (frequency distribution) }
$$

Standard Deviation

$$
S D=\sqrt{\frac{\sum(x-\bar{x})^{2}}{n}} \quad S D=\sqrt{\frac{\sum \mathrm{fx}^{2}}{\sum \mathrm{f}}-\overline{\mathrm{x}^{2}}} \text { (frequency distribution) }
$$

## INDEX NUMBERS

Price relative $=100 * P_{1} / P_{0} \quad$ Quantity relative $=100 * Q_{1} / Q_{0}$
Price: $\quad \frac{\sum w *\left(\frac{P_{1}}{P_{o}}\right)}{\sum w} \times 100$
Quantity: $\quad \frac{\sum w *\left(\frac{Q_{1}}{Q_{o}}\right)}{\sum w} \times 100$

## TIME SERIES

Additive Model

$$
\text { Series }=\text { Trend }+ \text { Seasonal + Random }
$$

Multiplicative Model

$$
\text { Series }=\text { Trend * Seasonal * Random }
$$

## FINANCIAL MATHEMATICS

## Compound Interest (Values and Sums)

Future Value $S$, of a sum of $X$, invested for $n$ periods, compounded at $r \%$ interest

$$
S=X[1+r]^{n}
$$

## Annuity

Present value of an annuity of $£ 1$ per annum receivable or payable for $n$ years, commencing in one year, discounted at $r \%$ per annum:

$$
\mathrm{PV}=\frac{1}{r}\left[1-\frac{1}{[1+r]^{n}}\right]
$$

## Perpetuity

Present value of $£ 1$ per annum, payable or receivable in perpetuity, commencing in one year, discounted at $r \%$ per annum:

$$
\mathrm{PV}=\frac{1}{r}
$$

## LEARNING CURVE

$$
Y_{x}=a X^{b}
$$

where:
$Y_{x}=$ the cumulative average time per unit to produce $X$ units;
$a=$ the time required to produce the first unit of output;
$X=$ the cumulative number of units;
$b=$ the index of learning.
The exponent $b$ is defined as the log of the learning curve improvement rate divided by $\log 2$.

## INVENTORY MANAGEMENT

Economic Order Quantity

$$
\mathrm{EOQ}=\sqrt{\frac{2 \mathrm{C}_{0} \mathrm{D}}{\mathrm{C}_{\mathrm{h}}}}
$$

where: $\mathrm{C}_{0}=$ cost of placing an order
$\mathrm{C}_{\mathrm{h}} \quad=\quad$ cost of holding one unit in inventory for one year
D $=$ annual demand

## LIST OF VERBS USED IN THE QUESTION REQUIREMENTS

A list of the learning objectives and verbs that appear in the syllabus and in the question requirements for each question in this paper.
It is important that you answer the question according to the definition of the verb.

| LEARNING OBJECTIVE | VERBS USED | DEFINITION |
| :---: | :---: | :---: |
| Level 1 - KNOWLEDGE |  |  |
| What you are expected to know. | List | Make a list of |
|  | State | Express, fully or clearly, the details/facts of |
|  | Define | Give the exact meaning of |
| Level 2 - COMPREHENSION |  |  |
| What you are expected to understand. | Describe | Communicate the key features |
|  | Distinguish | Highlight the differences between |
|  | Explain | Make clear or intelligible/State the meaning or purpose of |
|  | Identify | Recognise, establish or select after consideration |
|  | Illustrate | Use an example to describe or explain something |
| Level 3 - APPLICATION |  |  |
| How you are expected to apply your knowledge. | Apply | Put to practical use |
|  | Calculate | Ascertain or reckon mathematically |
|  | Demonstrate | Prove with certainty or to exhibit by practical means |
|  | Prepare | Make or get ready for use |
|  | Reconcile | Make or prove consistent/compatible |
|  | Solve | Find an answer to |
|  | Tabulate | Arrange in a table |
| Level 4 - ANALYSIS |  |  |
| How are you expected to analyse the detail of what you have learned. | Analyse | Examine in detail the structure of |
|  | Categorise | Place into a defined class or division |
|  | Compare and contrast | Show the similarities and/or differences between |
|  | Construct | Build up or compile |
|  | Discuss | Examine in detail by argument |
|  | Interpret | Translate into intelligible or familiar terms |
|  | Prioritise | Place in order of priority or sequence for action |
|  | Produce | Create or bring into existence |
| Level 5 - EVALUATION |  |  |
| How are you expected to use your learning to evaluate, make decisions or recommendations. | Advise | Counsel, inform or notify |
|  | Evaluate | Appraise or assess the value of |
|  | Recommend | Advise on a course of action |

## Performance Pillar

## Management Level Paper

## P2 - Performance Management

## September 2013

