UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS GCE Ordinary Level

MARK SCHEME for the October/November 2010 question paper for the guidance of teachers

4024 MATHEMATICS (SYLLABUS D)

4024/11 Paper 1, maximum raw mark 80

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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Abbreviations

cao correct answer only cso correct solution only

dep dependent

ft follow through after error isw ignore subsequent working

oe or equivalent SC Special Case

www without wrong working art anything rounding to soi seen or implied

	1		1	
1	(a)	7.7, $7\frac{7}{10}$, only	1	
	(b)	0.039 oe	1	
2	(a)	$\frac{16}{21}$ oe	1	
	(b)	$\frac{3}{4}$ oe	1	
3	(a)	$\frac{3}{5}$ cao	1	
	(b)	725	1	
4	(a)	5	1	
	(b)	16	1	
5	(a)	\wedge	1	
	(b)		1	
6	(a)	40.5	1	
	(b)	12.15 ft $0.3 \times \text{their} (a)$	1ft	
7	9		2	or B1 for " k " = 36 (oe), or for $4 \times 3^2 = y \times 2^2$ (oe)
8	10 fi	from using 0.4 , 7^2 and 2	2	M1 for 0.4 and (49 or 50), or for $\sqrt[3]{8.11} = 2$
9	(a)	$(x) > 4\frac{1}{2}$	1	Must be " $x >$ "
	(b)	-3, -2	1	
10	(a)	2	1	
	(b)	$\frac{1}{2}$, or 0.5, only	1	

Page 3	Mark Scheme: Teachers' version	Syllabus	Paper
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(b) 74 (c) 246 ft 360 – (their (a) + their (b)) 12 (a) $13x$ 1 (b) $\frac{1}{12y}$ (c) $12a^3b^4$ 1 13 (a) $2a(8a-3), 2a(-3+8a), \text{ only}$ 1 Not $2a(8a+-3)$ (b) $(3x-4)(y+2)$ 2 Or C1 for $(3x\pm4)(y\pm2)$ or B1 for any factorisation of any two terms; e.g. $3x(2+y), x(6+3y), -2(2y+4)$ 14 (a) 1.8×10^7 1 (b) 5×10^{-4} 2 or C1 for figs 5 15 (a) 15.7 2 or B1 for $\frac{100}{360} \times 2 \times \pi \times 9$ oe with " π " as π , 3.14 , 3.142 or $\frac{22}{7}$ (b) 33.7 ft their (a) + 18 1ft 16 (a) $-\frac{1}{3}$ (b) Correct region indicated by shading. 2 Or C1 for region below $y = x + 3$ and above $3y + x = 3$ indicated by shading or by R. 17 (a) $\begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ 2 or C1 for 4 or 5 correct elements (b) $(8 \ 0 \ -2)$ 1 18 Both $x = -6$ and $y = 7$ 3 or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been					
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(b) $\frac{1}{12y}$ 1 (c) $12a^3b^4$ 1 13 (a) $2a(8a-3), 2a(-3+8a)$, only 1 Not $2a(8a+-3)$ (b) $(3x-4)(y+2)$ 2 Or C1 for $(3x\pm4)(y\pm2)$ or B1 for any factorisation of any two terms; e.g. $3x(2+y), x(6+3y), -2(2y+4)$ 14 (a) 1.8×10^7 1 (b) 5×10^{-4} 2 or C1 for figs 5 15 (a) 15.7 2 or B1 for $\frac{100}{360} \times 2 \times \pi \times 9$ oe with " π " as π , 3.14 , 3.142 or $\frac{22}{7}$ (b) 33.7 ft their (a) + 18 1ft 16 (a) $-\frac{1}{3}$ 1 (b) Correct region indicated by shading. 2 Or C1 for region below $y = x + 3$ and above $3y + x = 3$ indicated by shading or by R. 17 (a) $\begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ 2 or C1 for 4 or 5 correct elements (b) $(8 \times 0 - 2)$ 1 18 Both $x = -6$ and $y = 7$ 3 or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been		(c)	246 ft 360 – (their (a) + their (b))	1ft	
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(b) $(3x-4)(y+2)$ 2 Or C1 for $(3x \pm 4)(y \pm 2)$ or B1 for any factorisation of any two terms; e.g. $3x(2+y)$, $x(6+3y)$, $-2(2y+4)$ 14 (a) 1.8×10^7 1 (b) 5×10^{-4} 2 or C1 for figs 5 15 (a) 15.7 2 or B1 for $\frac{100}{360} \times 2 \times \pi \times 9$ oe with " π " as π , 3.14 , 3.142 or $\frac{22}{7}$ (b) 33.7 ft their (a) + 18 16 (a) $-\frac{1}{3}$ 1 (b) Correct region indicated by shading. 2 Or C1 for region below $y = x + 3$ and above $3y + x = 3$ indicated by shading or by R. 17 (a) $\begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ 2 or C1 for 4 or 5 correct elements (b) $(8 \ 0 \ -2)$ 1 B Both $x = -6$ and $y = 7$ 3 or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been	13	· · ·			Not $2a(8a + -3)$
or B1 for any factorisation of any two terms; e.g. $3x(2+y)$, $x(6+3y)$, $-2(2y+4)$ 14 (a) 1.8×10^7 1					
(b) 5×10^{-4} 2or C1 for figs 515(a) 15.7 2or B1 for $\frac{100}{360} \times 2 \times \pi \times 9$ oe with " π " as π , 3.14, 3.142 or $\frac{22}{7}$ (b)33.7 ft their (a) + 181ft16(a) $-\frac{1}{3}$ 1(b)Correct region indicated by shading.2Or C1 for region below $y = x + 3$ and above $3y + x = 3$ indicated by shading or by R.17(a) $\begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ 2or C1 for 4 or 5 correct elements(b) $(8 \times 0 - 2)$ 118Both $x = -6$ and $y = 7$ 3or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been		(b)	(3x-4)(y+2)	2	or B1 for any factorisation of any two terms;
15 (a) 15.7 2 or B1 for $\frac{100}{360} \times 2 \times \pi \times 9$ oe with " π " as π , 3.14, 3.142 or $\frac{22}{7}$ (b) 33.7 ft their (a) + 18 16 (a) $-\frac{1}{3}$ (b) Correct region indicated by shading. 2 Or C1 for region below $y = x + 3$ and above $3y + x = 3$ indicated by shading or by R. 17 (a) $\begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ 2 or C1 for 4 or 5 correct elements (b) $(8 \ 0 \ -2)$ 1 Or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been	14	(a)	1.8×10^7	1	
(b) 33.7 ft their (a) + 18 16 (a) $-\frac{1}{3}$ (b) Correct region indicated by shading. 1 (b) Correct region indicated by shading. 2 Or C1 for region below $y = x + 3$ and above $3y + x = 3$ indicated by shading or by R. 17 (a) $\begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ 2 or C1 for 4 or 5 correct elements (b) $(8 \ 0 \ -2)$ 1 18 Both $x = -6$ and $y = 7$ 3 or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been		(b)	5×10^{-4}	2	or C1 for figs 5
(b)33.7 ft their (a) + 181ft16(a) $-\frac{1}{3}$ 1(b)Correct region indicated by shading.2Or C1 for region below $y = x + 3$ and above $3y + x = 3$ indicated by shading or by R.17(a) $\begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ 2or C1 for 4 or 5 correct elements(b) $(8 \ 0 \ -2)$ 118Both $x = -6$ and $y = 7$ 3or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been	15	(a)	15.7	2	or B1 for $\frac{100}{360} \times 2 \times \pi \times 9$ oe
16(a) $-\frac{1}{3}$ 1(b) Correct region indicated by shading.2 Or C1 for region below $y = x + 3$ and above $3y + x = 3$ indicated by shading or by R.17(a) $\begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ 2 or C1 for 4 or 5 correct elements(b) $\begin{pmatrix} 8 & 0 & -2 \end{pmatrix}$ 118Both $x = -6$ and $y = 7$ 3 or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been					with " π " as π , 3.14, 3.142 or $\frac{22}{7}$
(b)Correct region indicated by shading.2Or C1 for region below $y = x + 3$ and above $3y + x = 3$ indicated by shading or by R.17(a) $\begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ 2or C1 for 4 or 5 correct elements(b) $(8 \ 0 \ -2)$ 118Both $x = -6$ and $y = 7$ 3or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been		(b)	33.7 ft their (a) + 18	1ft	
$3y + x = 3 \text{ indicated by shading or by R.}$ $17 \textbf{(a)} \begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix}$ $2 \text{or C1 for 4 or 5 correct elements}$ $18 \text{Both } x = -6 \text{and} y = 7$ $3 \text{or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been}$	16	(a)	$-\frac{1}{3}$	1	
(b) $(8 \ 0 \ -2)$ 118Both $x = -6$ and $y = 7$ 3or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been		(b)	Correct region indicated by shading.	2	
Both $x = -6$ and $y = 7$ 3 or C2 for either or C1 for a pair of values that fits either equation, provided that this pair has been	17	(a)	$ \begin{pmatrix} 3 & -2 & 1 \\ 0 & 6 & -6 \end{pmatrix} $	2	or C1 for 4 or 5 correct elements
or C1 for a pair of values that fits either equation, provided that this pair has been		(b)	(8 0 -2)	1	
equation, provided that this pair has been	18	Both	1x = -6 and y = 7	3	
obtained by the method of substitution, equal coeffs., or matrices/determinants and not by trial and error.					equation, provided that this pair has been obtained by the method of substitution, equal coeffs., or matrices/determinants and not by
19 (a) $\frac{4}{25}$ or 0.16	19	(a)	$\frac{4}{25}$ or 0.16	1	
(b) 0		(b)	0	1	
(c) $\frac{12}{25}$ or 0.48 2 or C1 for $\frac{6}{25}$, or $\frac{8}{25}$, or $\frac{10}{25}$, or $\frac{16}{25}$ (or for 0.24, 0.32, 0.4, 0.64)		(c)	$\frac{12}{25}$ or 0.48	2	
20 (a) 1:6	20	(a)	1:6	1	(01.101.0.2.1, 0.02, 0.1, 0.01)
(b) (i) $(3, 2)$ (ii) $k = -5$ 1 2 or B1 for $4 \times 5 + 6k$		(b)			or B1 for $4 \times 5 + 6k$

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21	(a)	0.32	2	or B1 for $\cos ABD = -0.53 \text{ soi}$
	, ,	2.12	2	or B1 for $\cos b = \frac{BC}{4}$ soi
	(b)	2.12	2	or M1 for a valid method.
22	(a)	36, 52, 62, 70	1	
	(b)	3 < t < 4	1	
	(c)	10 4	1 1	
23	(a)	$8^2 - 6^2 = 4 \times 7$	1	
	(b)	$(n+1)^2 - (n-1)^2 (=4n)$	1	
	(c)	2080 cao	1	
	(d)	Both $x = 122$ and $y = 120$	1	
24	(a)	Reflection	1	
		$y=-\frac{1}{2}$	1	
	(b)	(i) ΔC has vertices $(-1, 0), (-2,0)$ and $(-2, 2)$	1	
		(ii) $\begin{pmatrix} 0 & -1 \\ 1 & 0 \end{pmatrix}$	1	
25	(a)	$(-)\frac{4}{5}$, (-)0.8, only	1	
	(b)	[Rectangle = 4×20] + [triangle = $\frac{1}{2} \times 5 \times 4$];	1	
		or trapezium = $\frac{1}{2} \times 4(20 + 25)$ or		
		$\frac{1}{2} \times 4 \times 45$		
	(c)	Straight line from (0, 0) to (20, 80).	1	If zero scored, then C1 for any graph starting at (0, 0) and ending at (25, 90) with a positive
		Curve, concave downwards, from (20, 80) to (25, 90).	1	(not zero) gradient throughout.
26	(a)	Both $\angle A = \angle C$ (given) and $\angle B$ is common or $\angle ABC = \angle DBC$ oe with no incorrect statements.	1	
	(b)	5 www	3	or M1 for $\frac{AB}{6} = \frac{6}{4}$ oe e.g. $x + 4$ for AB
				and A1 for $AB = 9$

Page 5	Mark Scheme: Teachers' version	Syllabus	Paper
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27	(a)	96° to 98° inclusive	1	
	(b)	(i) Arc of circle, centre C, radius 8 cm(ii) Bisector of angle BAC	1 1	
	(c)	Correct region shaded	1	Dep. on reasonable attempts at loci in (b).