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4037/02

For Examination from 2011

2 hours

No Additional Materials are required.

Write your Centre number, candidate number and name on all the work you hand in.
Write in dark blue or black pen.
You may use a pencil for any diagrams or graphs.
Do not use staples, paper clips, highlighters, glue or correction fluid.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 80.

For Examiner's Use	
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12	
Total	

This document consists of **16** printed pages.



Mathematical Formulae**1. ALGEBRA***Quadratic Equation*

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}.$$

Binomial Theorem

$$(a + b)^n = a^n + \binom{n}{1} a^{n-1} b + \binom{n}{2} a^{n-2} b^2 + \dots + \binom{n}{r} a^{n-r} b^r + \dots + b^n,$$

where n is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$.

2. TRIGONOMETRY*Identities*

$$\sin^2 A + \cos^2 A = 1.$$

$$\sec^2 A = 1 + \tan^2 A.$$

$$\operatorname{cosec}^2 A = 1 + \cot^2 A.$$

Formulae for $\triangle ABC$

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}.$$

$$a^2 = b^2 + c^2 - 2bc \cos A.$$

$$\Delta = \frac{1}{2} bc \sin A.$$

- 1 Given that $A = \begin{pmatrix} 13 & 6 \\ 7 & 4 \end{pmatrix}$, find the inverse matrix A^{-1} and hence solve the simultaneous equations

$$\begin{aligned} 13x + 6y &= 41, \\ 7x + 4y &= 24. \end{aligned}$$

[4]

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- 2 Variables x and y are connected by the equation $y = (2x - 9)^3$. Given that x is increasing at the rate of 4 units per second, find the rate of increase of y when $x = 7$. [4]

- 3 Find the set of values of m for which the line $y = mx + 2$ does not meet the curve $y = x^2 - 5x + 18$.
[5]

*For
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Use*

-
- 4 (a) A sports team of 3 attackers, 2 centres and 4 defenders is to be chosen from a squad of 5 attackers, 3 centres and 6 defenders. Calculate the number of different ways in which this can be done. [3]

- (b) How many different 4-digit numbers greater than 3000 can be formed using the six digits 1, 2, 3, 4, 5 and 6 if no digit can be used more than once? [3]

For
Examiner's
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- 5 (i) Differentiate $x \ln x$ with respect to x . [2]

- (ii) Hence find $\int \ln x \, dx$. [3]

6 Solve the following equations.

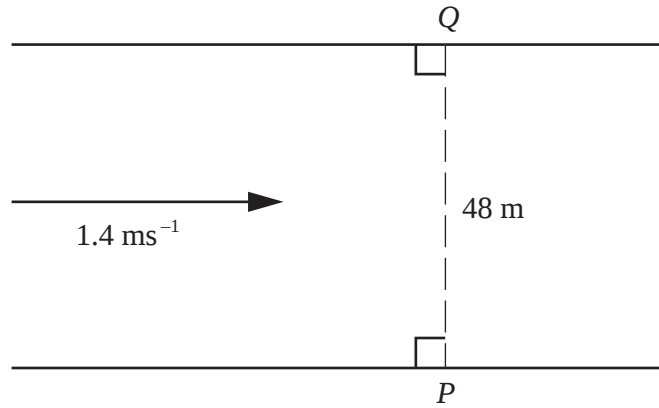
(i) $\frac{4^x}{2^{5-x}} = \frac{2^{4x}}{8^{x-3}}$

[3]

*For
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(ii) $\lg(2y + 10) + \lg y = 2$

[3]



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The diagram shows a river with parallel banks. The river is 48 m wide and is flowing with a speed of 1.4 ms^{-1} . A boat travels in a straight line from a point P on one bank to a point Q which is on the other bank directly opposite P . It is given that the boat takes 10 seconds to cross the river.

- (i) Find the speed of the boat in still water. [4]

- (ii) Find the angle to the bank at which the boat should be steered. [2]

- 8 The function f is defined, for $0 \leq x \leq 2\pi$, by

$$f(x) = 3 + 5 \sin 2x.$$

State

- (i) the amplitude of f , [1]

- (ii) the period of f , [1]

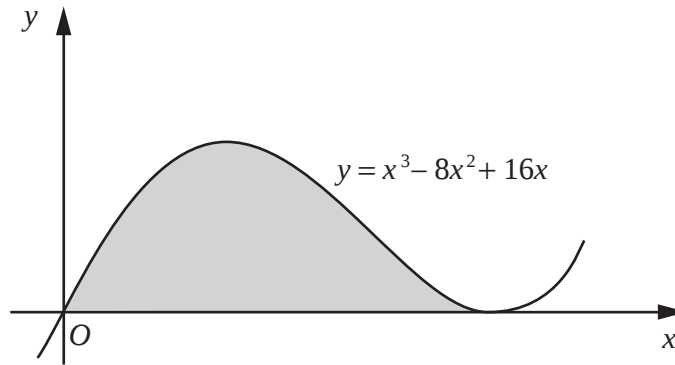
- (iii) the maximum and minimum values of f . [2]

Sketch the graph of $y = f(x)$. [3]

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- 9 The line $y = 2x - 9$ intersects the curve $x^2 + y^2 + xy + 3x = 46$ at the points A and B . Find the equation of the perpendicular bisector of AB . [8]

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The diagram shows part of the curve $y = x^3 - 8x^2 + 16x$.

- (i) Show that the curve has a minimum point at (4, 0) and find the coordinates of the maximum point. [4]

- (ii) Find the area of the shaded region enclosed by the x -axis and the curve.

[4]

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- 11 The table shows experimental values of two variables x and y .

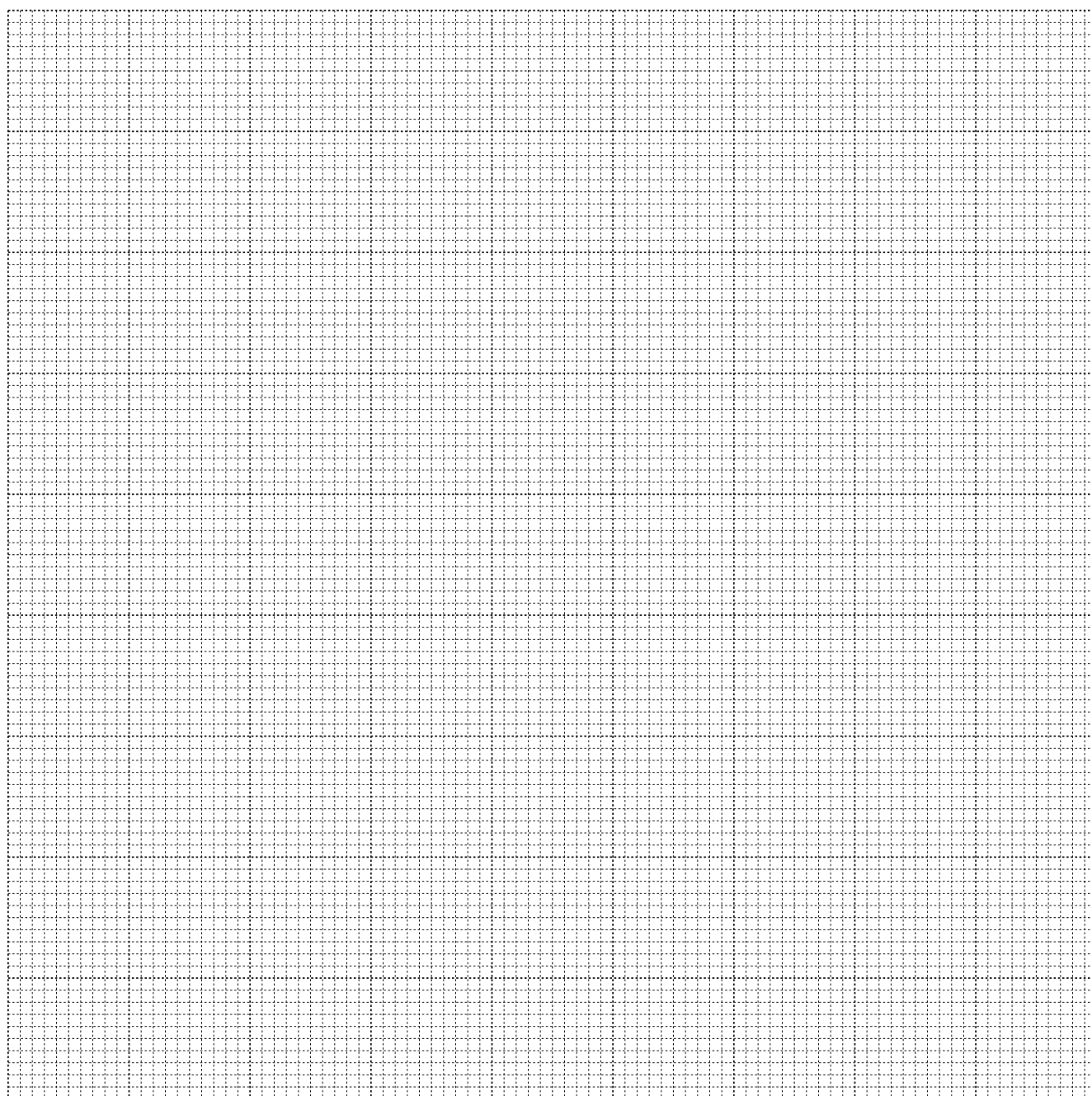
x	2	4	6	8
y	2.25	0.81	0.47	0.33

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- (i) On the graph paper below, plot xy against $\frac{1}{x}$ and draw a straight line graph.

[3]

xy				
$\frac{1}{x}$				



(ii) Use your graph to express y in terms of x .

[5]

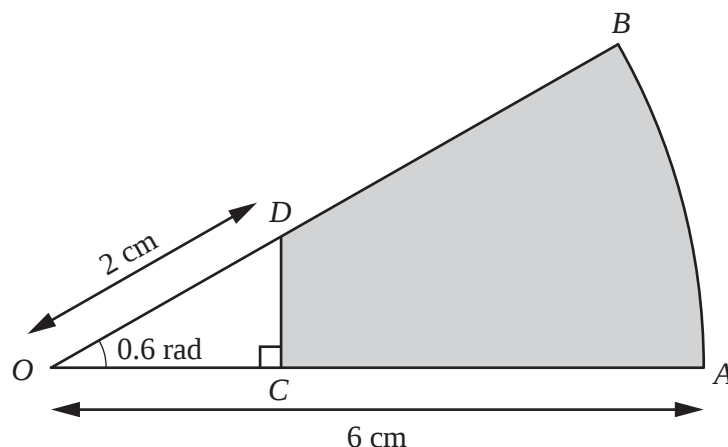
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(iii) Estimate the value of x and of y for which $xy = 4$.

[3]

12 Answer only **one** of the following two alternatives.

EITHER



The diagram shows a sector AOB of a circle with centre O and radius 6 cm. Angle $AOB = 0.6$ radians. The point D lies on OB such that the length of OD is 2 cm. The point C lies on OA such that OCD is a right angle.

(i) Show that the length of OC is approximately 1.65 cm and find the length of CD . [4]

(ii) Find the perimeter of the shaded region. [3]

(iii) Find the area of the shaded region. [3]

OR

A particle moves in a straight line so that t seconds after passing a fixed point O its acceleration, $a \text{ ms}^{-2}$, is given by $a = 4t - 12$. Given that its speed at O is 16 ms^{-1} , find

(i) the values of t at which the particle is stationary, [5]

(ii) the distance the particle travels in the fifth second. [5]

Start your answer to Question 12 here.

Indicate which question you are answering.

EITHER	
OR	

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Continue your answer to Question 12 here.

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Continue your answer here if necessary.

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