

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

| CANDIDATE NAME | | | | |
|-------------------|----------|-----------------------|---------------------|----------------------|
| CENTRE NUMBER | | | CANDIDATE NUMBER | |
| ADDITIONAL N | /ATHEN | MATICS | | 0606/01 |
| Paper 1 | | | For E | xamination from 2013 |
| SPECIMEN PA | PER | | | |
| | | | | 2 hours |
| Candidates ans | wer on t | the Question Paper. | | |
| Additional Mate | rials: | Electronic calculator | | |

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 80.

This document consists of 15 printed pages and 1 blank page.



Mathematical Formulae

1. ALGEBRA

Quadratic Equation

For the equation $ax^2 + bx + c = 0$,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}.$$

Binomial Theorem

$$(a+b)^{n} = a^{n} + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^{2} + \dots + \binom{n}{r}a^{n-r}b^{r} + \dots + b^{n},$$

where *n* is a positive integer and $\binom{n}{r} = \frac{n!}{(n-r)!r!}$.

2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1.$$

$$\sec^2 A = 1 + \tan^2 A.$$

$$\csc^2 A = 1 + \cot^2 A.$$

Formulae for $\triangle ABC$

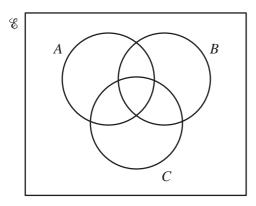
$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C} \,.$$

$$a^2 = b^2 + c^2 - 2bc \cos A.$$

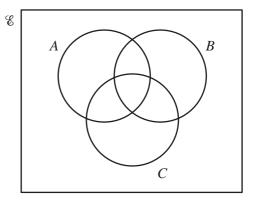
$$\Delta = \frac{1}{2} bc \sin A.$$

1 Shade the region corresponding to the set given below each Venn diagram.

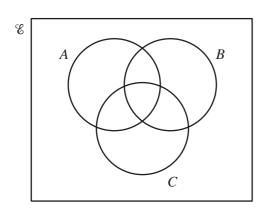
For Examiner's Use



 $A \cup (B \cap C)$



 $A \cap (B \cup C)$



 $(A \cup B \cup C)'$

[3]

2 Find the set of values of x for which $(2x+1)^2 > 8x+9$.

[4]

3 Prove that
$$\frac{\sin A}{1 + \cos A} + \frac{1 + \cos A}{\sin A} \equiv 2 \csc A.$$

[4] For Examiner's Use

A function f is such that $f(x) = ax^3 + bx^2 + 3x + 4$. When f(x) is divided by x - 1, the remainder is 3. When f(x) is divided by 2x + 1, the remainder is 6. Find the value of a and of b. [5]

For Examiner's Use

5 (i) Solve the equation $2t = 9 + \frac{5}{t}$. [3]

(ii) Hence, or otherwise, solve the equation $2x^{\frac{1}{2}} = 9 + 5x^{-\frac{1}{2}}$. [3]

| _ | ~ . | | | | ~ |
|---|---------------------------|--------------------------------|---------------------|------------------------------|--------|
| 6 | Given that $\mathbf{a} =$ | = 5 i – 12 ⁱ | i and that b | $= p\mathbf{i} + \mathbf{j}$ | , finc |

Examiner's [2]

Use

(i) the unit vector in the direction of a,

(ii) the values of the constants p and q such that $q\mathbf{a} + \mathbf{b} = 19\mathbf{i} - 23\mathbf{j}$.

[3]

7 (i) Express $4x^2 - 12x + 3$ in the form $(ax + b)^2 + c$, where a, b and c are constants and a > 0. [3]

For Examiner's Use

(ii) Hence, or otherwise, find the coordinates of the stationary point of the curve $y = 4x^2 - 12x + 3$.

(iii) Given that $f(x) = 4x^2 - 12x + 3$, write down the range of f.

[1]

8 A curve is such that $\frac{d^2y}{dx^2} = 4e^{-2x}$. Given that $\frac{dy}{dx} = 3$ when x = 0 and that the curve passes through the point $(2, e^{-4})$, find the equation of the curve. [6]

For Examiner's Use 9 (i) Find, in ascending powers of x, the first 3 terms in the expansion of $(2-3x)^5$.

For Examiner's Use

[3]

The first 3 terms in the expansion of $(a + bx)(2 - 3x)^5$ in ascending powers of x are $64 - 192x + cx^2$.

(ii) Find the value of a, of b and of c.

[5]

10 (a) Functions f and g are defined, for $x \in \mathbb{R}$, by

For Examiner's Use

$$f(x) = 3 - x$$
,
 $g(x) = \frac{x}{x+2}$, where $x \neq 2$.

(i) Find fg(x).

[2]

(ii) Hence find the value of x for which fg(x) = 10.

[2]

- **(b)** A function h is defined, for $x \in \mathbb{R}$, by $h(x) = 4 + \ln x$, where x > 1.
 - (i) Find the range of h.

[1]

(ii) Find the value of $h^{-1}(9)$.

[2]

| (iii) | On the same axes, sketch the graphs of $y = h(x)$ and $y = h^{-1}(x)$. |
|-------|---|
| | |

[3] For Examiner's Use

11 Solve the following equations.

(i) $\tan 2x - 3\cot 2x$, for $0^{\circ} < x < 180^{\circ}$

For Examiner's Use

[4]

(ii)
$$\csc y = 1 - 2\cot^2 y$$
, for $0^{\circ} \le y \le 360^{\circ}$

[5]

(iii)
$$\sec(z + \frac{\pi}{2}) = -2$$
, for $0 < z < \pi$ radians.

[3] Examiner's Use

12 A curve has equation $y = \frac{x^2}{x+1}$.

For Examiner's Use

(i) Find the coordinates of the stationary points of the curve.

[5]

The normal to the curve at the point where x = 1 meets the x-axis at M. The tangent to the curve at the point where x = -2 meets the y-axis at N.

For Examiner's Use

(ii) Find the area of the triangle MNO, where O is the origin.

[6]

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