

# UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

	CANDIDATE NAME					
	CENTRE NUMBER			]	CANDIDATE NUMBER	
		MATHEMA	TICS			0606/11
	Paper 1					May/June 2013
<u></u>						2 hours
°	Candidates answer on the Question Paper.					
	Additional Mate	erials:	Electronic calculat	tor		
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# READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO **NOT** WRITE IN ANY BARCODES.

Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question. The use of an electronic calculator is expected, where appropriate. You are reminded of the need for clear presentation in your answers.

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question. The total number of marks for this paper is 80.

This document consists of 16 printed pages.



[Turn over

### Mathematical Formulae

#### 1. ALGEBRA

Quadratic Equation

For the equation  $ax^2 + bx + c = 0$ ,

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a} \; .$$

**Binomial Theorem** 

$$(a+b)^n = a^n + \binom{n}{1}a^{n-1}b + \binom{n}{2}a^{n-2}b^2 + \dots + \binom{n}{r}a^{n-r}b^r + \dots + b^n,$$
  
where *n* is a positive integer and  $\binom{n}{r} = \frac{n!}{(n-r)!r!}$ .

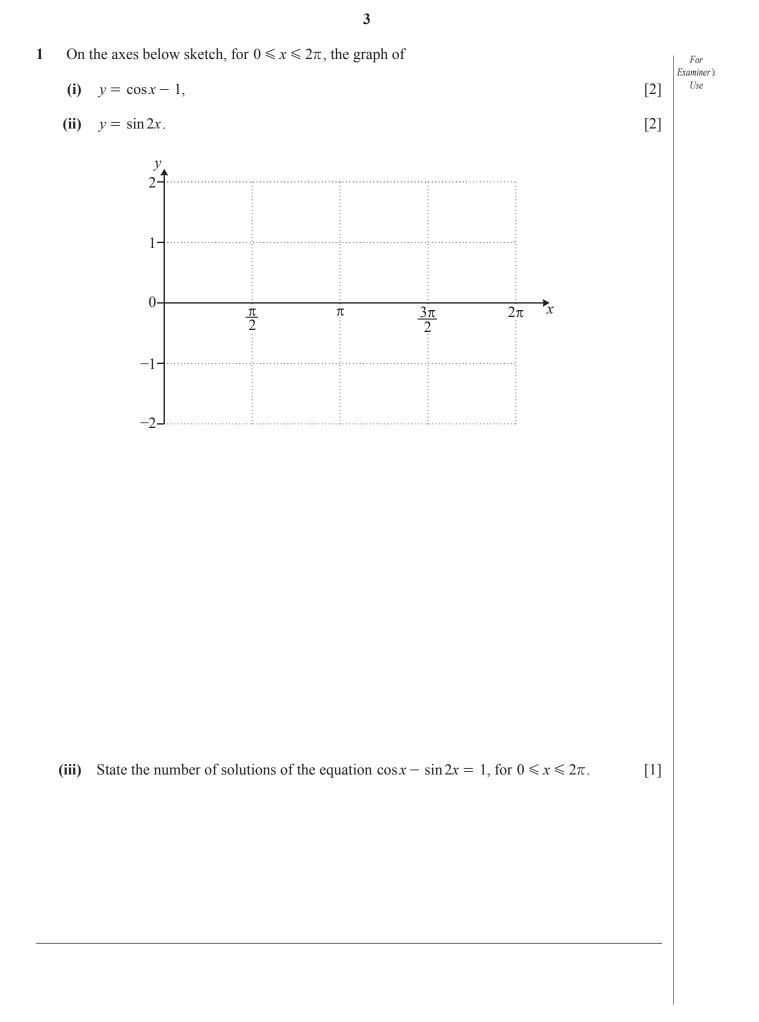
# 2. TRIGONOMETRY

Identities

$$\sin^2 A + \cos^2 A = 1$$
$$\sec^2 A = 1 + \tan^2 A$$
$$\csc^2 A = 1 + \cot^2 A$$

Formulae for  $\triangle ABC$ 

$$\frac{a}{\sin A} = \frac{b}{\sin B} = \frac{c}{\sin C}$$
$$a^2 = b^2 + c^2 - 2bc \cos A$$
$$\Delta = \frac{1}{2} bc \sin A$$



Variables x and y are such that  $y = Ab^x$ , where A and b are constants. The diagram shows the graph of ln y against x, passing through the points (2, 4) and (8, 10). For Examiner's Use  $\ln y$ (8, 10) (2, 4) $\overset{\blacktriangleright}{x}$ 

4

Find the value of *A* and of *b*.

0

2

[5]

- 3 A committee of 6 members is to be selected from 5 men and 9 women. Find the number of For different committees that could be selected if Examiner's Use (i) there are no restrictions, [1] (ii) there are exactly 3 men and 3 women on the committee, [2]
  - (iii) there is at least 1 man on the committee.

[3]

4 (i) Given that  $\log_4 x = \frac{1}{2}$ , find the value of x.

(ii) Solve 
$$2\log_4 y - \log_4(5y - 12) = \frac{1}{2}$$
.

[4]

For Examiner 's

Use

[1]

5 (i) Find 
$$\int \left(1 - \frac{6}{x^2}\right) dx$$
. [2] For Examiner's Use

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(ii) Hence find the value of the positive constant k for which  $\int_{k}^{3k} \left(1 - \frac{6}{x^2}\right) dx = 2.$  [4]

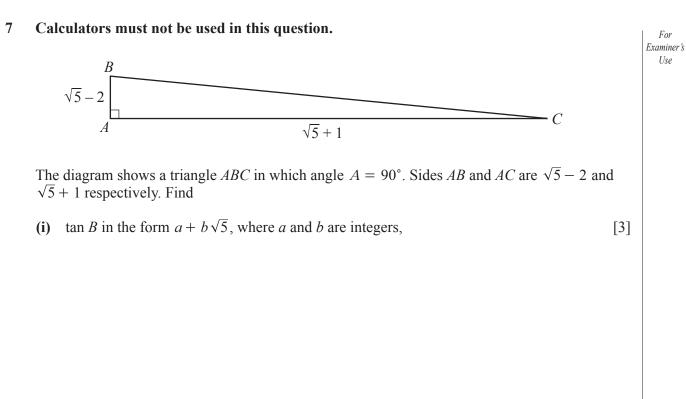
6 (i) Given that  $\mathbf{A} = \begin{pmatrix} 2 & -1 \\ 3 & 5 \end{pmatrix}$ , find  $\mathbf{A}^{-1}$ .

(ii) Using your answer from part (i), or otherwise, find the values of a, b, c and d such that

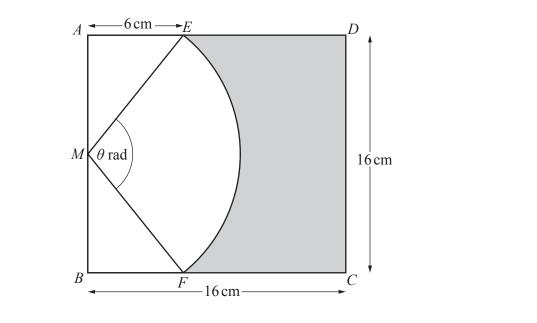
$$\mathbf{A} \begin{pmatrix} a & b \\ c & -1 \end{pmatrix} = \begin{pmatrix} 7 & 5 \\ 17 & d \end{pmatrix}.$$
 [5]

[2]





(ii)  $\sec^2 B$  in the form  $c + d\sqrt{5}$ , where c and d are integers.



The diagram shows a square *ABCD* of side 16 cm. *M* is the mid-point of *AB*. The points *E* and *F* are on *AD* and *BC* respectively such that AE = BF = 6 cm. *EF* is an arc of the circle centre *M*, such that angle *EMF* is  $\theta$  radians.

(i) Show that  $\theta = 1.855$  radians, correct to 3 decimal places.

(ii) Calculate the perimeter of the shaded region.

[4]

[2]

For

Examiner's Use

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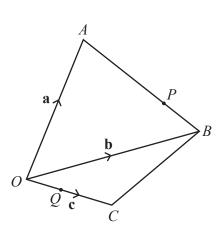
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(iii) Calculate the area of the shaded region.

[3] For Examiner's Use





The figure shows points A, B and C with position vectors **a**, **b** and **c** respectively, relative to an origin O. The point P lies on AB such that AP:AB = 3:4. The point Q lies on OC such that OQ:QC = 2:3.

(i) Express  $\overrightarrow{AP}$  in terms of **a** and **b** and hence show that  $\overrightarrow{OP} = \frac{1}{4}(\mathbf{a} + 3\mathbf{b})$ . [3]

(ii) Find  $\overrightarrow{PQ}$  in terms of **a**, **b** and **c**.

[3]

(iii) Given that  $5\overrightarrow{PQ} = 6\overrightarrow{BC}$ , find **c** in terms of **a** and **b**.

For Examiner 's

Use

[2]

10 The point A, whose x-coordinate is 2, lies on the curve with equation  $y = x^3 - 4x^2 + x + 1$ .For<br/>Examiner's<br/>Use(i) Find the equation of the tangent to the curve at A.[4]

This tangent meets the curve again at the point *B*.

(ii) Find the coordinates of *B*.

[4]

(iii) Find the equation of the perpendicular bisector of the line *AB*.

For Examiner's Use

[4]

Question 11 is printed on the next page.

11 (a) Solve 
$$2\sin\left(x+\frac{\pi}{3}\right) = -1$$
 for  $0 \le x \le 2\pi$  radians. [4] For Examiner's Use

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(b) Solve  $\tan y - 2 = \cot y$  for  $0^{\circ} \le y \le 180^{\circ}$ .

[6]

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