

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		

058591206

MATHEMATICS 0581/23

Paper 2 (Extended) October/November 2011

1 hour 30 minutes

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator Geometrical instruments

Mathematical tables (optional) Tracing paper (optional)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 70.

This document consists of 12 printed pages.



1	Martha divides \$240 between spending and saving in the ratio								
	spending: saving = $7:8$.								
	Calculate the amount Martha has for spending.								
		Answer \$	[2]						
_									
2	210 211	212 213 214 215 216							
	From the list of numbers, find								
	(a) a prime number,								
		Answer(a)	[1]						
	(b) a cube number.								
	(b) a cube number.								
		Answer(b)[[1]						
									
3	Solve the simultaneous equations.	x + 5y = 22							
		x + 3y = 22 $x + 3y = 12$							
		Answer x =							
			· 21						
		y =[[2]						

For Examiner's Use 4 Find the value of $\left(\frac{27}{8}\right)^{-\frac{4}{3}}$.

For Examiner's Use

Give your answer as an exact fraction.

Answer	 [2]
	 ъ.

- 5 The population of a city is 128 000, correct to the nearest thousand.
 - (a) Write 128 000 in standard form.

Answer(a) [1]

(b) Write down the upper bound of the population.

Answer(b) [1]

Pedro invested \$800 at a rate of 5% per year **compound** interest. Calculate the **total** amount he has after 2 years.

Answer \$ _____[2]

7 Show that $3^{-2} + 2^{-2} = \frac{13}{36}$.

Write down all the steps of your working.

Answer

[2]

8	Find the value of	$\frac{\sqrt[3]{17.1 - 1.89}}{10.4 + \sqrt{8.36}}$				•					
							A	nswer		***	[2]
9	In Vienna, the mic This information i			in °C,	are rec	corded	during	g a weel	k in December.		
		-2	2	1	-3	-1	-2	0			
	Calculate										
	(a) the difference	e between the	highes	st temp	eratur	e and t	he low	est tem	nperature,		
						A	Inswer	r(a)		°C	[1]
	(b) the mean tem	perature.									
						А	Inswer	·(b)		°C	[2]
10	Maria decides to i	ncrease her ho	mewo	ork tim	e of 8	hours]	per we	ek by 1	5%.		
	Calculate her new Give your answer			es.							

Answer h min [3]

For Examiner's Use

11	Factorise completely. $p^2x -$	$4q^2x$
		Answer [3]
12	Alberto changes 800 Argentine pesos (ARS) into do He spends \$150 and changes the remaining dollars $1 = 3.8025$ ARS.	
	Calculate the amount Alberto now has in pesos.	
		Answer ARS [3]
13	During a marathon race an athlete loses 2% of his n At the end of the race his mass is 67.13 kg.	nass.
	Calculate his mass before the race.	
		Answer kg [3]

For Examiner's Use

2r

For Examiner's Use

The sphere of radius r fits exactly inside the cylinder of radius r and height 2r. Calculate the percentage of the cylinder occupied by the sphere.

[The volume, V, of a sphere with radius r is $V = \frac{4}{3}\pi r^3$.]

Answer	%	[3]
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NOT TO SCALE

ap = px + c

Write p in terms of a, c and x.

$$Answer p =$$
 [3]

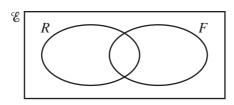
	7
16	The time, t , for a pendulum to swing varies directly as the square root of its length, l . When $l = 9$, $t = 6$.
	(a) Find a formula for t in terms of l .
	Answer(a) t =
	(b) Find t when $l = 2.25$.

Examiner's Use

[2]

Answer(b) t =	[1]

17



In the Venn diagram, $\mathscr{E} = \{\text{students in a survey}\}, R = \{\text{students who like rugby}\}\$ and $F = \{\text{students who like football}\}.$

$$n(\mathscr{E}) = 20$$

$$n(R \cup F) = 17$$
 $n(R) = 13$

$$n(R) = 13$$

$$n(F) = 11$$

(a) Find

(i)
$$n(R \cap F)$$
,

(ii)
$$n(R' \cap F)$$
.

(b) A student who likes rugby is chosen at random.

Find the probability that this student also likes football.

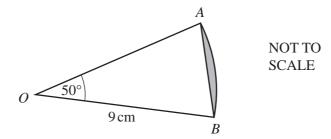
Answer(b) [1] 18 Write as a single fraction, in its simplest form.

1-x	2 + x
	$\frac{1-2x}{1-2x}$

For Examiner's Use

Answer	 [4]

19



The diagram shows a sector AOB of a circle, centre O, radius 9 cm with angle $AOB = 50^{\circ}$.

Calculate the area of the segment shaded in the diagram.

Answer	 cm^2	[4]

20	(a)	$ \mathbf{N} = \begin{pmatrix} 2 \\ 6 \end{pmatrix} $. The order of the matrix \mathbf{N} is 2×1 .
		$P = (1 3)$. The order of the matrix P is 1×2 .
		(i) Write down the order of the matrix NP .

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Answer(a)(i) [1]

(ii) Calculate PN.

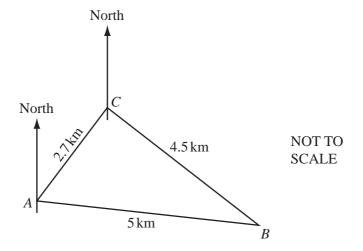
Answer(a)(ii) [1]

(b) $\mathbf{M} = \begin{pmatrix} 2 & 3 \\ 2 & 4 \end{pmatrix}$.

Find \mathbf{M}^{-1} , the inverse of \mathbf{M} .

 $Answer(b) \mathbf{M}^{-1} = [2]$

For Examiner's Use



The diagram shows 3 ships A, B and C at sea.

AB = 5 km, BC = 4.5 km and AC = 2.7 km.

(a) Calculate angle *ACB*. Show all your working.

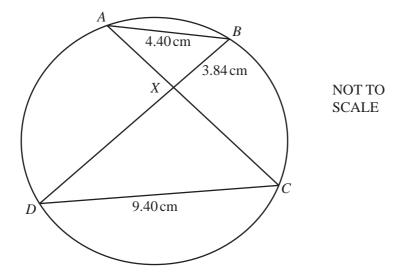
$$Answer(a) \text{ Angle } ACB =$$
 [4]

(b) The bearing of A from C is 220° .

Calculate the bearing of *B* from *C*.

Answer(b) [1]

Examiner's Use



A, B, C and D lie on a circle. AC and BD intersect at X.

(a) Give a reason why angle BAX is equal to angle CDX.

Answer(a) [1]

- **(b)** $AB = 4.40 \,\mathrm{cm}$, $CD = 9.40 \,\mathrm{cm}$ and $BX = 3.84 \,\mathrm{cm}$.
 - (i) Calculate the length of CX.

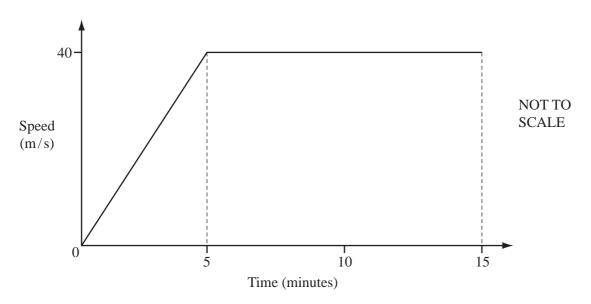
(ii) The area of triangle ABX is 5.41 cm².

Calculate the area of triangle *CDX*.

Answer(b)(ii) cm² [2]

Question 23 is printed on the next page.





The diagram shows the speed-time graph for the first 15 **minutes** of a train journey. The train accelerates for 5 minutes and then continues at a constant speed of 40 metres/**second**.

(a) Calculate the acceleration of the train during the first 5 minutes. Give your answer in m/s².

Answer(a) m/s^2 [2]

(b) Calculate the average speed for the first 15 minutes of the train journey. Give your answer in m/s.

Answer(b) m/s [3]

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