

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

	CANDIDATE NAME							
* 9 4	CENTRE NUMBER			CANDIDATE NUMBER				
	MATHEMATICS		0581/41					
5 0	Paper 4 (Extend	ed)	October/November 2010					
2 4			2 hours 30 minutes					
6	Candidates answer on the Question Paper.							
05*	Additional Mater	rials: Electronic calculator Mathematical tables (optional)		Geometrical instruments Tracing paper (optional)				
	READ THESE IN	ISTRUCTIONS FIRS	T					

Write your Centre number, candidate number and name on all the work you hand in.Write in dark blue or black pen.You may use a pencil for any diagrams or graphs.Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place. For π use either your calculator value or 3.142.

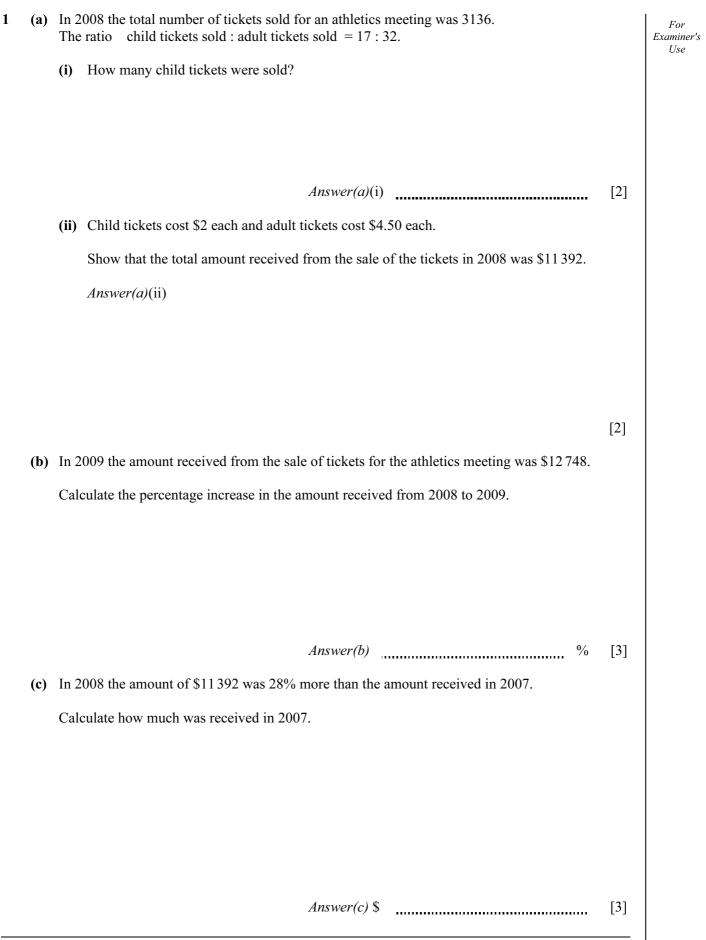
At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question.

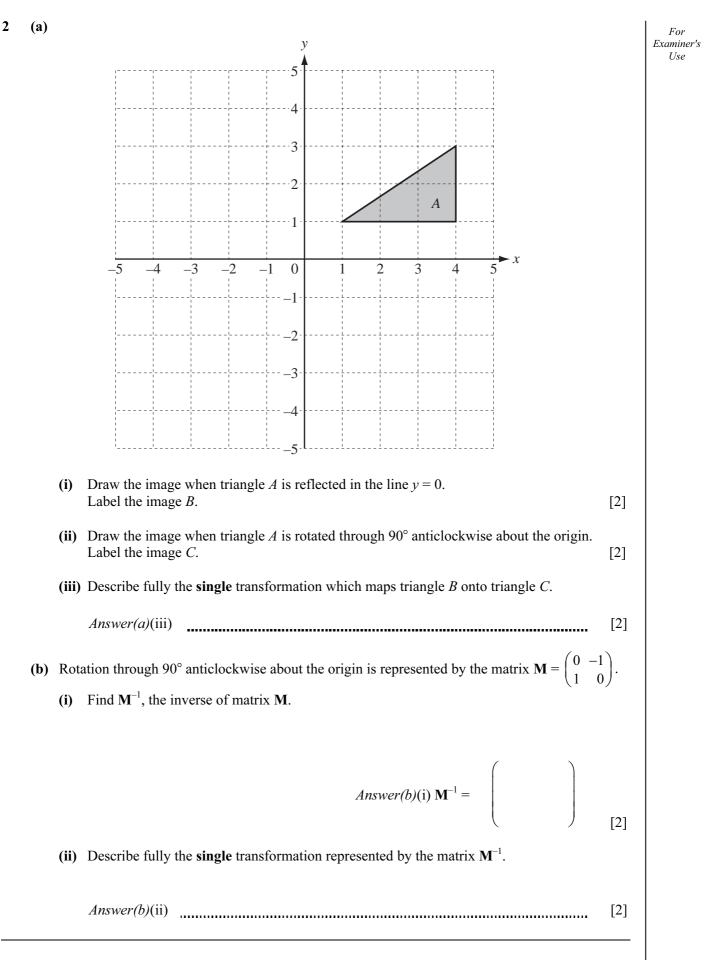
The total of the marks for this paper is 130.

This document consists of 16 printed pages.



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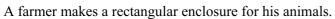




x

NOT TO SCALE For Examiner's

Use



He uses a wall for one side and a total of 72 metres of fencing for the other three sides.

Wall

Enclosure

The enclosure has width x metres and area A square metres.

(a) Show that $A = 72x - 2x^2$.

Answer (a)

3

(b) Factorise completely $72x - 2x^2$.

Answer(b) [2]

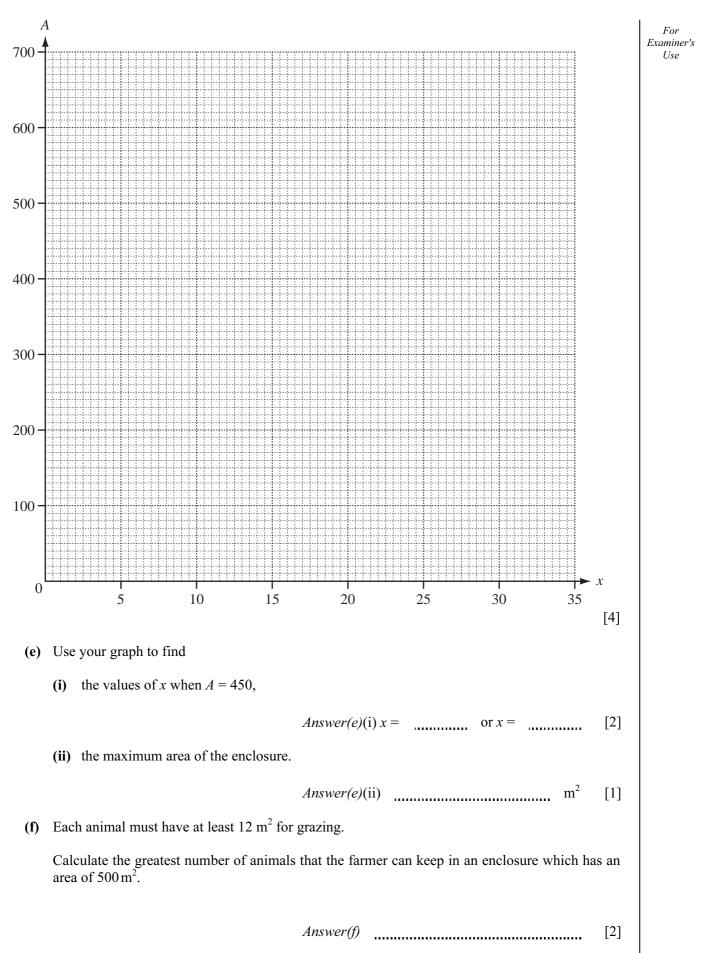
(c) Complete the table for $A = 72x - 2x^2$.

x	0	5	10	15	20	25	30	35
A	0	310	520			550	360	

[3]

[2]

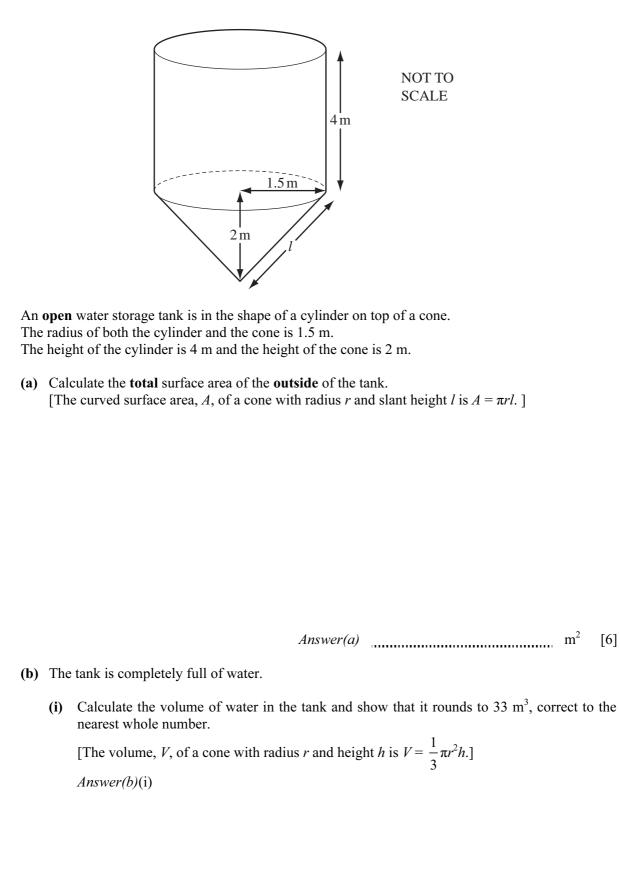
(d) Draw the graph of $A = 72x - 2x^2$ for $0 \le x \le 35$ on the grid opposite.



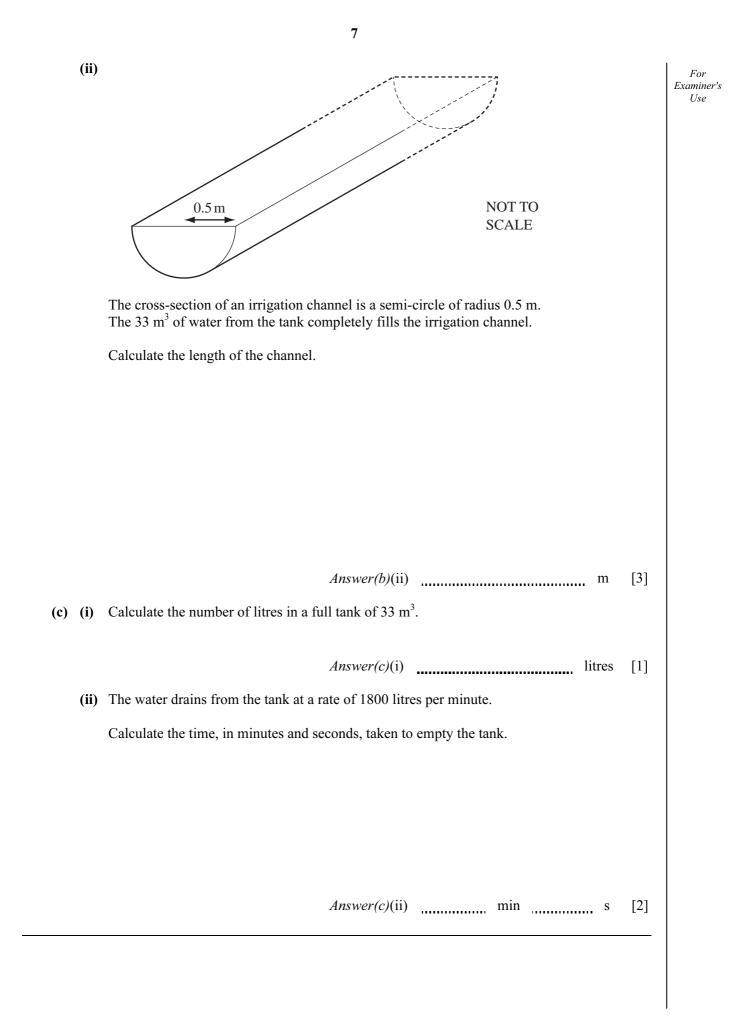
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4



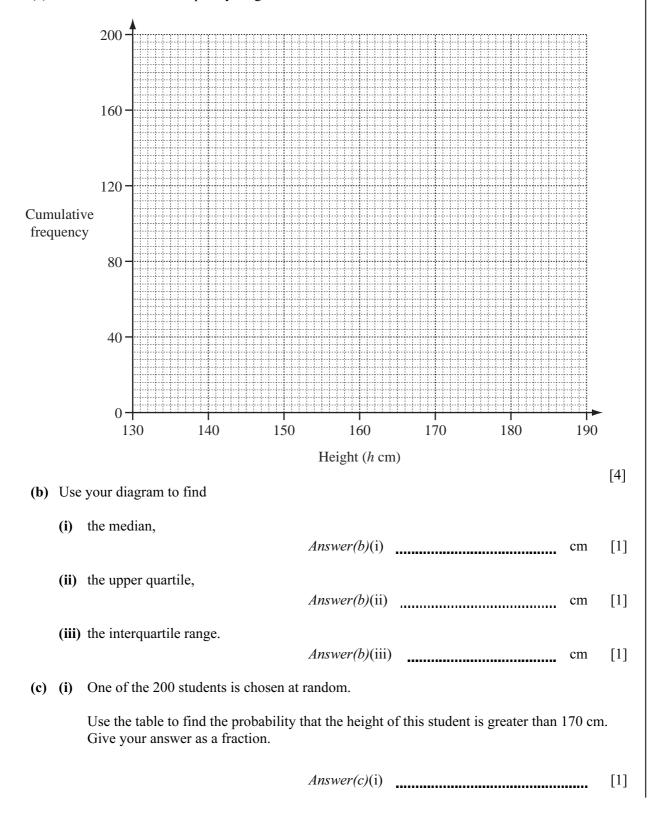
[4]



- Height (h cm) ≤130 ≤140 ≤150 ≤160 ≤165 ≤170 ≤180 ≤190 Cumulative frequency 0 10 50 95 115 145 180 200
- 5 The cumulative frequency table shows the distribution of heights, *h* centimetres, of 200 students.

For Examiner's Use

(a) Draw a cumulative frequency diagram to show the information in the table.



(ii) One of the 200 students is chosen at random and then a second student is chosen at random from the remaining students.

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[2]

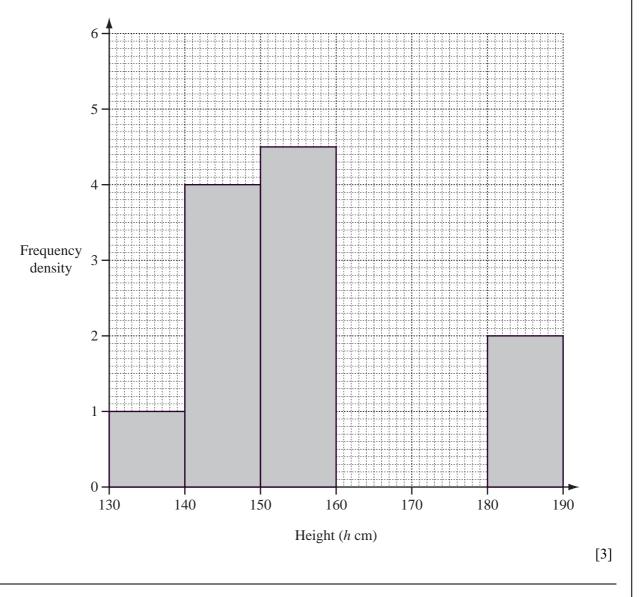
Calculate the probability that one has a height greater than 170 cm and the other has a height of 140 cm or less. Give your answer as a fraction.



(d) (i) Complete this frequency table which shows the distribution of the heights of the 200 students.

Height (<i>h</i> cm)	130< <i>h</i> ≤140	140< <i>h</i> ≤150	150< <i>h</i> ≤160	160< <i>h</i> ≤165	165< <i>h</i> ≤170	170< <i>h</i> ≤180	180< <i>h</i> ≤190
Frequency	10	40	45	20			

(ii) Complete this histogram to show the distribution of the heights of the 200 students.



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10 A NOT TO 19.5 cm 16.5 cm **SCALE** 11 cm R Q B⁴ С The diagram shows a toy boat. AC = 16.5 cm, AB = 19.5 cm and PR = 11 cm. Triangles *ABC* and *PQR* are **similar**.

(i) Calculate PQ.

(ii) Calculate BC.

Answer(a)(ii) BC = cm [3]

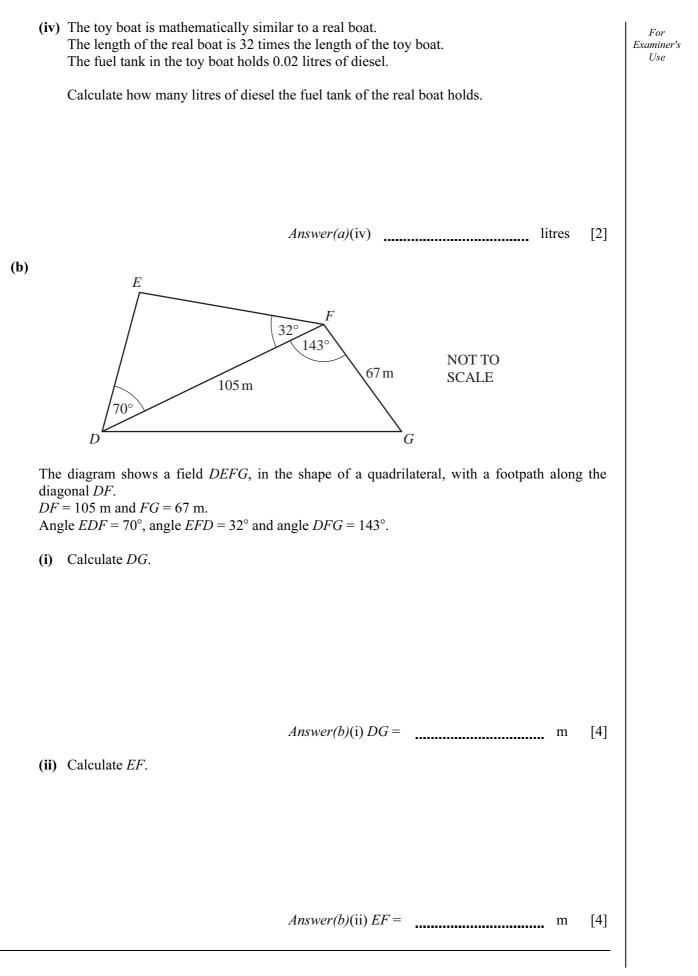
Answer(a)(i) PQ = cm [2]

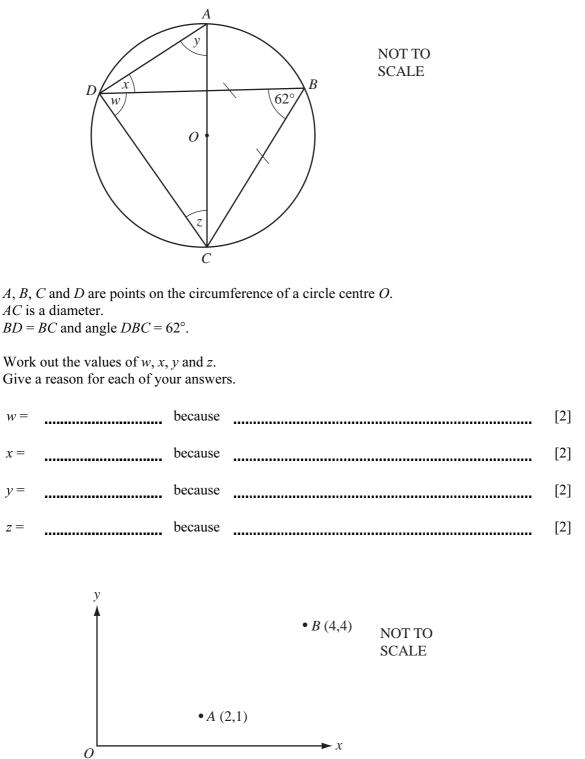
(iii) Calculate angle ABC.

Answer(a)(iii) Angle ABC = [2]

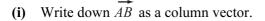
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(a)









[1]

Answer(b)(i) $\overrightarrow{AB} =$

7

(a)

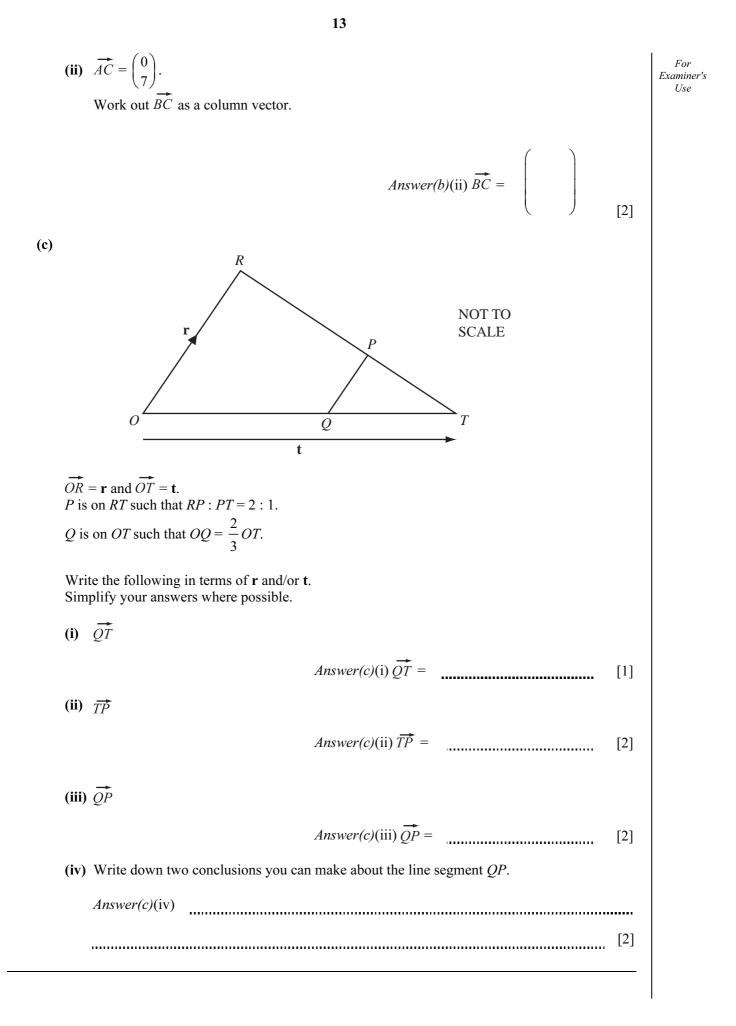
W =

x =

y =

z =

(b)



8	(a)		$f(x) = 2x - 1 \qquad \qquad g(x) = x^2$	2		For Examiner's
		Wo	rk out			Use
		(i)	f(2),	Answer(a)(i)	[1]	
		(ii)	g(-2),	Answer(a)(ii)	[1]	
		(iii)	ff(x) in its simplest form,			
		(iv)	$f^{-1}(x)$, the inverse of $f(x)$,	Answer(a)(iii) $ff(x) =$	[2]	
		(v)	x when $gf(x) = 4$.	Answer(a)(iv) $f^{-1}(x) =$	[2]	
	(b)	<i>y</i> is	Answer(a)(v) x inversely proportional to x and y	= or $x == 8 when x = 2.$	[4]	
		Fin (i)	d, an equation connecting y and x ,			
			y when $x = \frac{1}{2}$.	Answer(b)(i)	[2]	
				Answer(b)(ii) $y =$	[1]	

(a) The first five terms P_1 , P_2 , P_3 , P_4 and P_5 of a sequence are given below.

	1	$= 1 = P_1$	
	1 + 2	$= 3 = P_2$	
	1 + 2 + 3	$= 6 = P_3$	
	1 + 2 + 3 + 4	$= 10 = P_4$	
	1 + 2 + 3 + 4 + 5	$= 15 = P_5$	
(i)	Write down the next	term, P_6 , in the sequence 1, 3, 6, 10, 15	
		Answer(a)(i)	[1]
(ii)	The formula for the <i>n</i>	th term of this sequence is	
		$\mathbf{P}_n = \frac{1}{2}n(n+1).$	
	Show this formula is	true when $n = 6$.	
	Answer (a)(ii)		
			[1]
(iii)	Use the formula to fin	nd P_{50} , the 50th term of this sequence.	
		Answer(a)(iii)	[1]
(iv)	Use your answer to p	art (iii) to find 3 + 6 + 9 + 12 + 15 + + 150.	
		Answer(a)(iv)	[1]
(v)	Find $1 + 2 + 3 + 4 + 5$	$5 + \dots + 150.$	
		Answer(a)(v)	[1]
(vi)	Use your answers to are not multiples of 3	parts (iv) and (v) to find the sum of the numbers less than 150 wh	
		Answer(a)(vi)	[1]
	Т	his question continues on the next page.	

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- (b) The first five terms, S_1 , S_2 , S_3 , S_4 and S_5 of a different sequence are given below.
 - $(1 \times 1) = 1 = S_1$ $(1 \times 2) + (2 \times 1) = 4 = S_2$ $(1 \times 3) + (2 \times 2) + (3 \times 1) = 10 = S_3$ $(1 \times 4) + (2 \times 3) + (3 \times 2) + (4 \times 1) = 20 = S_4$ $(1 \times 5) + (2 \times 4) + (3 \times 3) + (4 \times 2) + (5 \times 1) = 35 = S_5$
 - (i) Work out the next term, S_6 , in the sequence 1, 4, 10, 20, 35...

Answer(b)(i) [2]

(ii) The formula for the *n*th term of this sequence is

$$S_n = \frac{1}{6}n(n+1)(n+2).$$

Show this formula is true for n = 6.

Answer(b)(ii)

(iii) Find $(1 \times 20) + (2 \times 19) + (3 \times 18) \dots + (20 \times 1)$.

Answer(b)(iii) [1]

(c) Show that $S_6 - S_5 = P_6$, where P_6 is your answer to part (a)(i).

Answer(c)

(d) Show by algebra that
$$S_n - S_{n-1} = P_n$$
. $[P_n = \frac{1}{2}n(n+1)]$
Answer(d)

[1]

[1]

^[3]

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