

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

CANDIDATE NAME					
CENTRE NUMBER			CANDIDATE NUMBER		



MATHEMATICS 0581/31

Paper 3 (Core) May/June 2012

2 hours

Candidates answer on the Question Paper.

Additional Materials: Electronic calculator

Electronic calculator Geometrical instruments
Mathematical tables (optional) Tracing paper (optional)

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen.

You may use a pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

DO NOT WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place.

For π , use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together.

The number of marks is given in brackets [] at the end of each question or part question.

The total of the marks for this paper is 104.

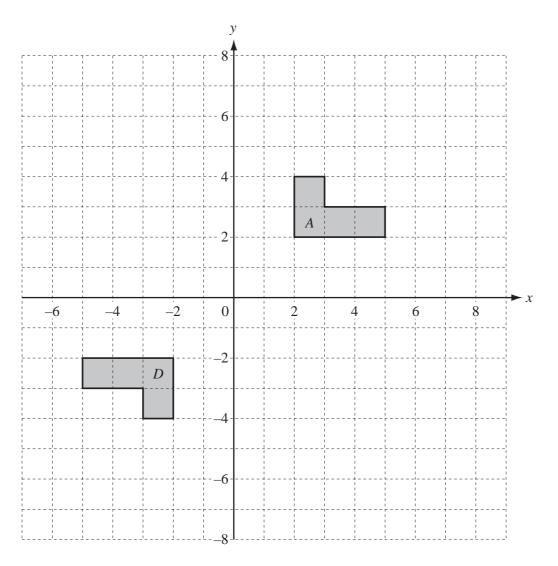
This document consists of 15 printed pages and 1 blank page.



1	(a)	vince and Wendy share \$2000 in the ratio Vince: We	ndy = 19	:21.						
		Calculate the amount of money that Vince receives.								
			() f		[2]					
		Ansv	ver(a) \$		[2]					
	(b)	Wendy has \$265 to spend on some chairs. The chairs cost \$37 each.								
		Work out the largest number of chairs she can buy.								
		Амен	war(h)		[2]					
		Ansv	ver(b)		[2]					
	(c)									
		She gives 27% of the money to Jake and $\frac{2}{5}$ of the mone	y to Karl.							
		Work out the amount of money she gives to Lana.								
		Апсы	ver(c) \$		[3]					
		11157	<i>(e)</i> \$		[2]					
	(d)	Wendy invests \$500 at a rate of 4% per year compound interest.								
		Calculate the total amount of interest she receives at the Give your answer correct to the nearest dollar.	e end of 2	years.						
		Ansv	wer(d) \$		[4]					

For Examiner's Use

For Examiner's Use



Two shapes A and D are shown on the grid.

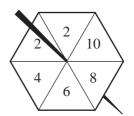
- (a) (i) Reflect shape A in the line x = 0. Label this image B. [2]
 - (ii) Rotate shape A through 180° about (2, 4). Label this image C. [2]
 - (iii) Enlarge shape A with scale factor 2 and centre (3, 7). Label this image E. [2]
- (b) Describe fully the single transformation that maps shape D onto
 - (i) shape B,

Answer(b)(i) [2]

(ii) shape C.

Answer(b)(ii) [2]

3 (a) Jon spins this 6-sided spinner.



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The probability that the spinner lands on any of the six sides is equally likely.

Write down the probability that the spinner lands on

					_
1	(i)	the	num	her	6
- 4	L	uic	muni	-	v.

(ii) a prime number,

$$Answer(a)$$
(ii) [1]

(iii) a number less than 11.

(b) Felix has a 12-sided spinner with the numbers 2, 4, 5, 7 and 9 written on it.

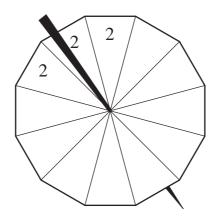
It is equally likely to land on any side.

The table shows the probability of the spinner landing on each number.

Number on spinner	2	4	5	7	9
Probability	$\frac{1}{4}$	$\frac{1}{3}$	$\frac{1}{6}$	$\frac{1}{6}$	$\frac{1}{12}$

The diagram of the spinner has been completed for the number 2.

Complete the diagram for the numbers 4, 5, 7 and 9.



[3]

(c) Felix says that his spinner is more likely to land on a 2 than Jon's spinner.

Explain why he is wrong.

Answer(c)

[1]

(d) Felix spins his 12-sided spinner 60 times and records the results.

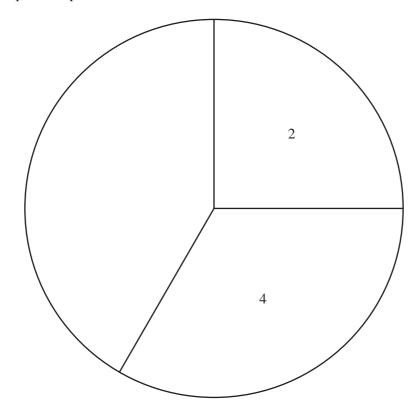
Number on spinner	Frequency	Pie chart sector angle
2	15	90°
4	20	120°
5	5	30°
7	12	
9	8	

(i) Complete the table by working out the sector angles for the numbers 7 and 9.

[3]

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(ii) Complete the pie chart.



[2]

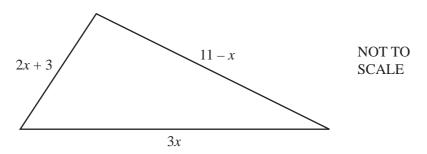
(iii) Write down the mode.

Answer(d)(iii) [1]

(iv) Calculate the mean.

Answer(d)(iv) [3] 4 In this question all the measurements are in centimetres.

For Examiner's Use



The diagram shows a triangle with sides of length 2x + 3, 11 - x and 3x.

(a)	Explain	why	x must	be	less	than	11
-----	---------	-----	--------	----	------	------	----

Answer(a)	
	[1]

(b) Write down an expression, in terms of x, for the perimeter of the triangle. Give your answer in its simplest possible form.

$$Answer(b) \qquad [2]$$

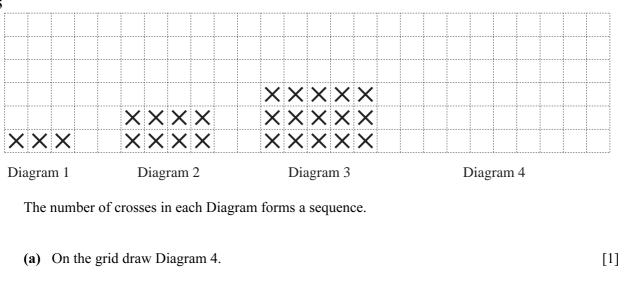
- (c) The perimeter of the triangle is 32 cm.
 - (i) Write down an equation in terms of x and solve it.

$$Answer(c)(i) x =$$
 [3]

(ii) Work out the length of the shortest side of the triangle.

Answer(c)(ii) _____ cm [2]

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(b) Write down the number of crosses needed to draw Diagram 5.

Answer(b)		[1]
\ /		

(c) Diagram 1 has 1 row of 3 crosses. Diagram 2 has 2 rows of 4 crosses.

(i) Complete this statement for Diagram n.

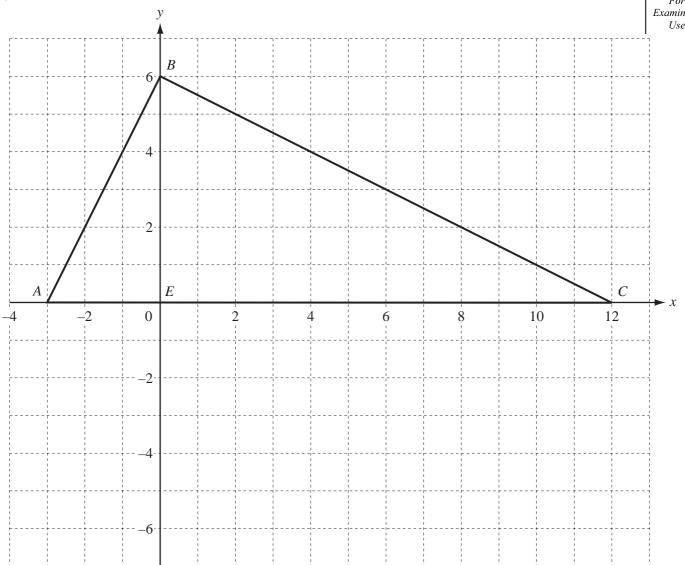
Diagram n has n rows of		crosses.	[]	1
-----------------------------	--	----------	----	---

(ii) Write down, in terms of n, how many crosses are needed to draw Diagram n.

$$Answer(c)$$
(ii) [1]

(iii) Find the number of crosses needed to draw Diagram 20.

Examiner's Use



Triangle ABC is drawn on a 1cm² grid. E is the point (0, 0).

(a) Write down the gradient of the line AB.

Answer(a)	[2	•
miswer (u)	 14	•

(b) The gradient of BC is -0.5.

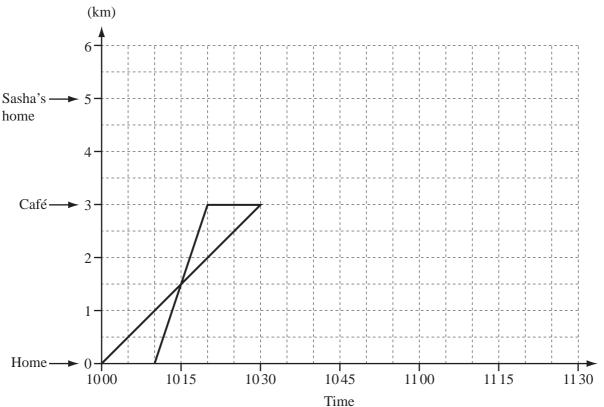
Write down the equation of the line BC in the form y = mx + c.

$$Answer(b) y =$$
 [2]

(c)	Write down the ratio $AE: EC$. Give your answer in its simplest form.	For Examiner's Use
	Answer(c) :	[2]
(d)	Measure angle ABE.	
	Answer(d) Angle $ABE =$	[1]
(e)	Triangle ABE is similar to triangle BCE.	
	Explain what the word similar tells you about the triangles <i>ABE</i> and <i>BCE</i> .	
	Answer(e)	
		[2]
(f)	Calculate the area of triangle <i>ABC</i> .	
	Answer(f) cm ²	[3]
(g)	ABCD is a rectangle.	
	(i) Mark point D on the grid.	[1]
	(ii) Write down the co-ordinates of D .	
	Answer(g)(ii) ([1]



For Examiner's Use



Poppy and Toni go to a café which is 3 km from their home. They take the same route.

Poppy leaves home at 1000 and walks. Toni leaves home at 1010 and cycles.

These journeys are shown on the travel graph.

(a)	(i)	How l	long does	Toni	wait at 1	the café	before I	Poppy	arrives'	•
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Answer(a)(i) _____ min [1]

(ii) The graphs cross at 1015.

Describe what this means.

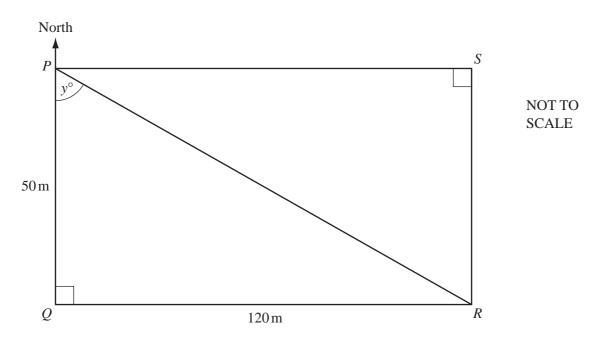
(iii) Calculate Toni's average speed from home to the café in kilometres per hour.

Answer(a)(iii) km/h [2]

(b)	Pop	py and Toni stay at the café until 1050.	
	(i)	At 10 50 Poppy walks to visit her friend Sasha. Sasha's home is 5 km from Poppy's home. Poppy walks at the same speed as before.	
		Complete the travel graph for Poppy.	[2]
	(ii)	At 1050 Toni starts to cycle home. At 1055, when she has travelled half the distance home, her bicycle has a puncture. She then walks the rest of the way home at 4.5 km/h.	
		Complete the travel graph for Toni.	[2]
	(iii)	Calculate the average speed for Toni's journey home from the café.	
		Answer(b)(iii) km/h	[3]

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The diagram shows a rectangular field, PQRS. $QR = 120 \,\text{m}$, $PQ = 50 \,\text{m}$ and P is due North of Q.

Bill and Said run from P to R. Bill runs along the sides PQ and QR. Said runs directly from P to R.

- (a) Calculate how far
 - (i) Bill runs,

Answer(a)(i)	m	[1]	l

(ii) Said runs.

Answer(a)(ii) m [2]

(b) Bill takes 34 seconds to reach R.

Calculate Bill's average speed.

Answer(b) _____ m/s [1]

(c)	Said runs at 4 m/s.				
	Who arrives at <i>R</i> first and by how many s	seconds?			
	Answer(c)	arrives at R first by		seconds.	[3]
(d)	(i) Use trigonometry to calculate the size	ze of the angle marked	y.		
		Answer(d)(i	()		[2]
	(ii) Find the bearing of R from P.	This wer (a) (· ····································		[2]
	(ii) Time the searing of it from T.				
		Answer(d)(i	i)		[1]
(e)	Calculate the area of the field in square I Give your answer in standard form.	kilometres.			
		Answer(e)		km ²	[4]

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9 (a)

3 cm NOT TO SCALE For Examiner's Use

A cylindrical drinking glass has radius $3\,\mathrm{cm}$ and height $8\,\mathrm{cm}$.

(i)	Calculate the volume of water the glass holds when it is filled to the top.
	Give the units of your answer.

Answer(a)(i)		[3]
11115 Wer (a) (1)	 	L

(ii) Water is poured into a number of these glasses from a jug containing 1.5 litres. Each glass has a horizontal line 2 cm from the top.

Calculate how many of these glasses can be filled up to the line from the jug.

Answer(a)(ii) [4]

(b) A cylindrical pipe has a circumference of 16 cm.

Calculate the diameter of the pipe.

Answer(b) cm [2]

15 (c) A cuboid measures 6 cm by 5 cm by 4 cm. 4cm NOT TO **SCALE** 5 cm 6cm Work out the surface area of the cuboid. Answer(c) cm^2 [3] (d) 1m^3 of copper has a mass of m kg. The volume of one copper sphere is $v \text{ m}^3$. Write down an expression for (i) the mass, in kilograms, of one sphere, Answer(d)(i) kg [1] the mass, in kilograms, of s spheres,

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(iii) the mass, in grams, of s spheres.

Answer(d)(ii) kg [1]

Answer(d)(iii) g [1]

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