

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

| | CANDIDATE NAME | | |
|---------|--------------------|---|--------------------|
| | CENTRE NUMBER | CANDIDATE NUMBER | |
| * 5 9 | MATHEMATICS | | 0581/41 |
| 0 2 | Paper 4 (Extended | d) | May/June 2010 |
| 6 6 | | | 2 hours 30 minutes |
| 9 | Candidates answe | | |
| * 7 9 0 | Additional Materia | Is: Electronic calculator Geometrical instrumen Mathematical tables (optional) Tracing paper (optional | |

READ THESE INSTRUCTIONS FIRST

Write your Centre number, candidate number and name on all the work you hand in.Write in dark blue or black pen.You may use a pencil for any diagrams or graphs.Do not use staples, paper clips, highlighters, glue or correction fluid.Do **NOT** WRITE IN ANY BARCODES.

Answer all questions.

If working is needed for any question it must be shown below that question.

Electronic calculators should be used.

If the degree of accuracy is not specified in the question, and if the answer is not exact, give the answer to three significant figures. Give answers in degrees to one decimal place. For π use either your calculator value or 3.142.

At the end of the examination, fasten all your work securely together. The number of marks is given in brackets [] at the end of each question or part question. The total of the marks for this paper is 130.

This document consists of 19 printed pages and 1 blank page.

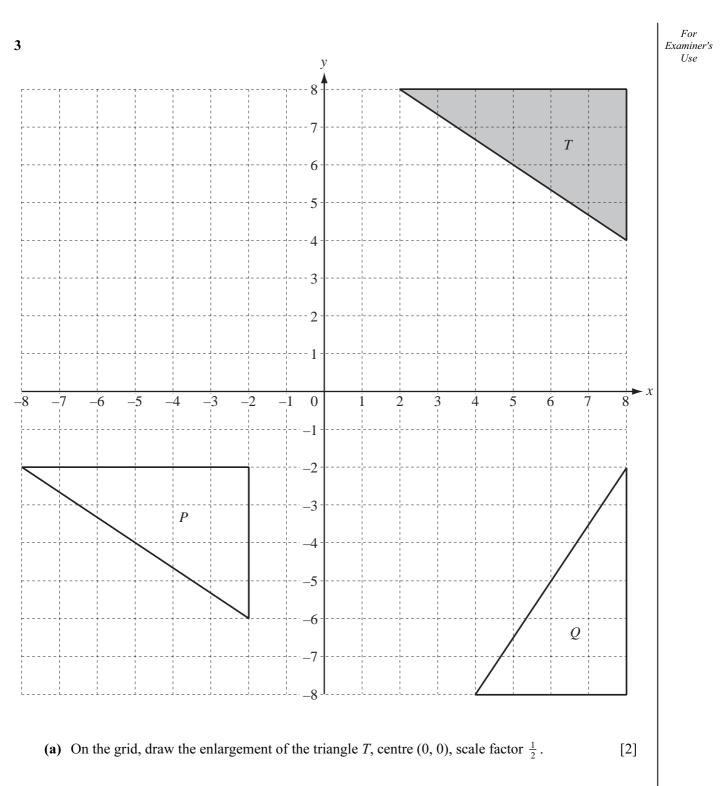


[Turn over

| A s | chool has 220 boys and 280 girls. | | | Ex |
|-----|---|------------------|-----------|-----|
| (a) | Find the ratio of boys to girls, in its simplest form | l . | | |
| (h) | The notic of students to too shows is 10 + 1 | Answer(a) | | [1] |
| (0) | The ratio of students to teachers is 10 : 1. Find the number of teachers. | | | |
| | | Answer(b) | | [2] |
| (c) | There are 21 students on the school's committee. The ratio of boys to girls is 3 : 4. Find the number of girls on the committee. | | | |
| | | Answer(c) | | [2] |
| (d) | The committee organises a disco and sells tickets. 35% of the school's students each buy a ticket. E Calculate the total amount received from selling t | ach ticket cost | s \$1.60. | |
| | | Answer(d) \$ | | [3] |
| (e) | The cost of running the disco is \$264. This is an increase of 10% on the cost of running Calculate the cost of running last year's disco. | last year's dise | co. | |
| | | Answer(e) \$ | | [2] |

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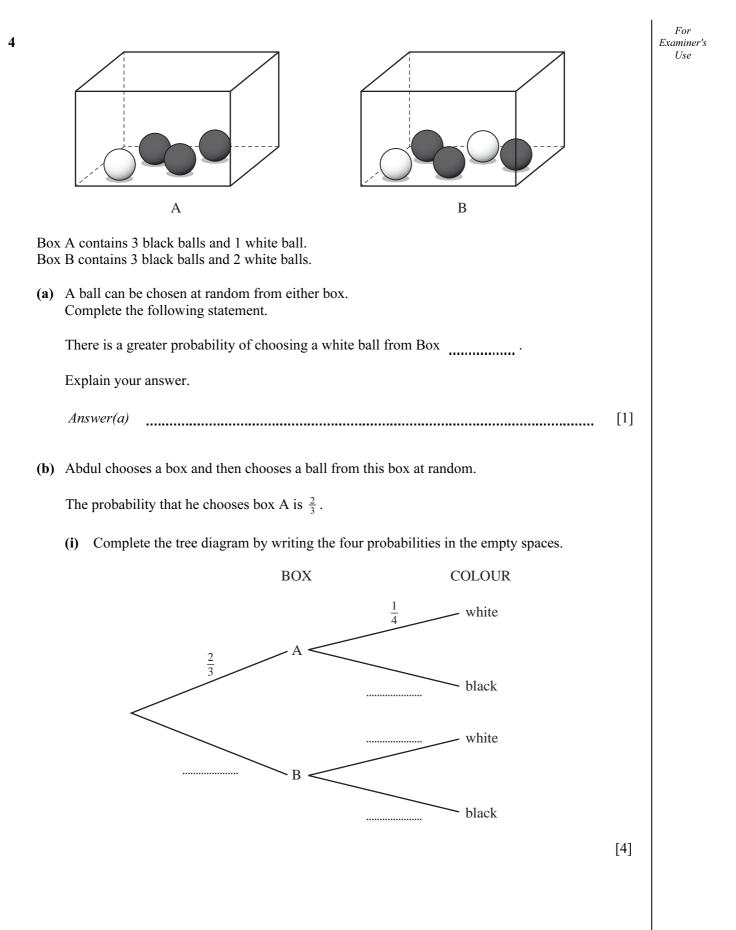
0581/41/M/J/10

(b) The matrix
$$\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix}$$
 represents a transformation.
(i) Calculate the matrix product $\begin{pmatrix} -1 & 0 \\ 0 & 1 \end{pmatrix} \begin{pmatrix} 8 & 8 & 2 \\ 4 & 8 & 8 \end{pmatrix}$.

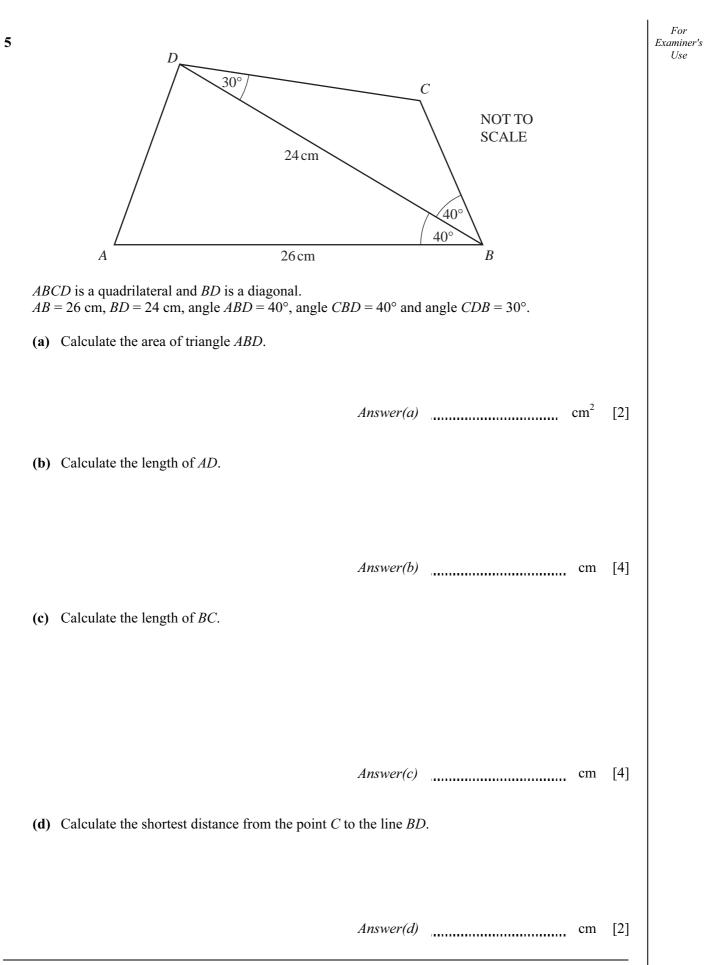
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| | ii) On the grid, draw the image of the triangle T under this transformation. | [2] |
|-----|--|-----|
| | iii) Describe fully this single transformation. | |
| | Answer(b)(iii) | [2] |
| (c) | Describe fully the single transformation which maps (i) triangle <i>T</i> onto triangle <i>P</i> , | |
| | Answer(c)(i) | [2] |
| | (ii) triangle T onto triangle Q . | |
| | Answer(c)(ii) | [3] |
| | | |

(d) Find the 2 by 2 matrix which represents the transformation in **part (c)(ii)**.



| | (ii) Find the probability that Abdul chooses box A and a black ball. | | | | | |
|-----|--|--|--|--|--|--|
| | <i>Answer(b)</i> (ii) [2] (iii) Find the probability that Abdul chooses a black ball. | | | | | |
| | Answer(b)(iii) [2] | | | | | |
| (c) | Tatiana chooses a box and then chooses two balls from this box at random (without replacement). | | | | | |
| | The probability that she chooses box A is $\frac{2}{3}$. | | | | | |
| | Find the probability that Tatiana chooses two white balls. | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | | | | | | |
| | <i>Answer(c)</i> [2] | | | | | |
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6 The masses of 60 potatoes are measured. The table shows the results.

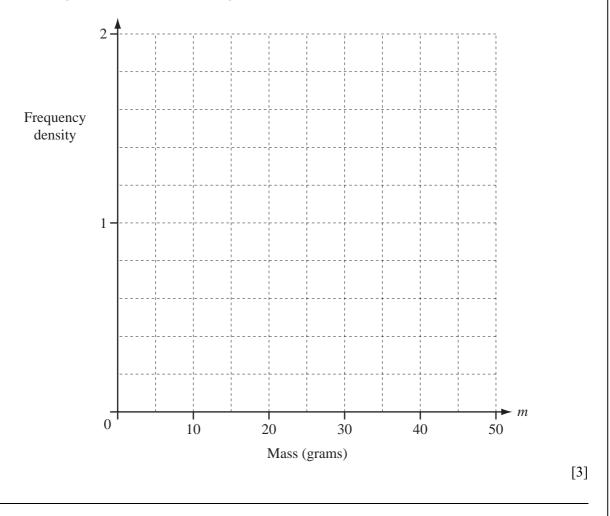
| Mass (<i>m</i> grams) | $10 < m \le 20$ | $20 < m \le 40$ | $40 < m \le 50$ |
|------------------------|-----------------|-----------------|-----------------|
| Frequency | 10 | 30 | 20 |

9

(a) Calculate an estimate of the mean.



(b) On the grid, draw an accurate histogram to show the information in the table.



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For 7 (a) Calculate the volume of a cylinder of radius 31 centimetres and length 15 metres. Examiner's UseGive your answer in cubic metres. Answer(a) m^3 [3] (b) A tree trunk has a circular cross-section of radius 31 cm and length 15 m. One cubic metre of the wood has a mass of 800 kg. Calculate the mass of the tree trunk, giving your answer in tonnes. Answer(b) _____ tonnes [2] (c) NOT TO plastic SCALE sheet E The diagram shows a pile of 10 tree trunks. Each tree trunk has a circular cross-section of radius 31 cm and length 15 m. A plastic sheet is wrapped around the pile. *C* is the centre of one of the circles.

10

CE and CD are perpendicular to the straight edges, as shown.

| (i) | Show that angle $ECD = 120^{\circ}$. Answer(c)(i) | | For Examiner's Use |
|-------|---|--------------------|--------------------------|
| (ii) | Calculate the length of the arc <i>DE</i> , giving your answer in metres. | [2] | |
| (iii) | <i>Answer(c)</i> (ii) 1 The edge of the plastic sheet forms the perimeter of the cross-section of the pile. The perimeter consists of three straight lines and three arcs. Calculate this perimeter, giving your answer in metres. | m [2] | |
| (iv) | Answer(c)(iii) | m [3] | |
| | Answer(c)(iv) 1 | m ² [1] | |

11

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8 (a) $f(x) = 2^x$

Complete the table.

| x | -2 | -1 | 0 | 1 | 2 | 3 | 4 | |
|---------------------|----|-----|---|---|---|---|---|-----|
| $y = \mathbf{f}(x)$ | | 0.5 | 1 | 2 | 4 | | | |
| | | | | | | | | [3] |

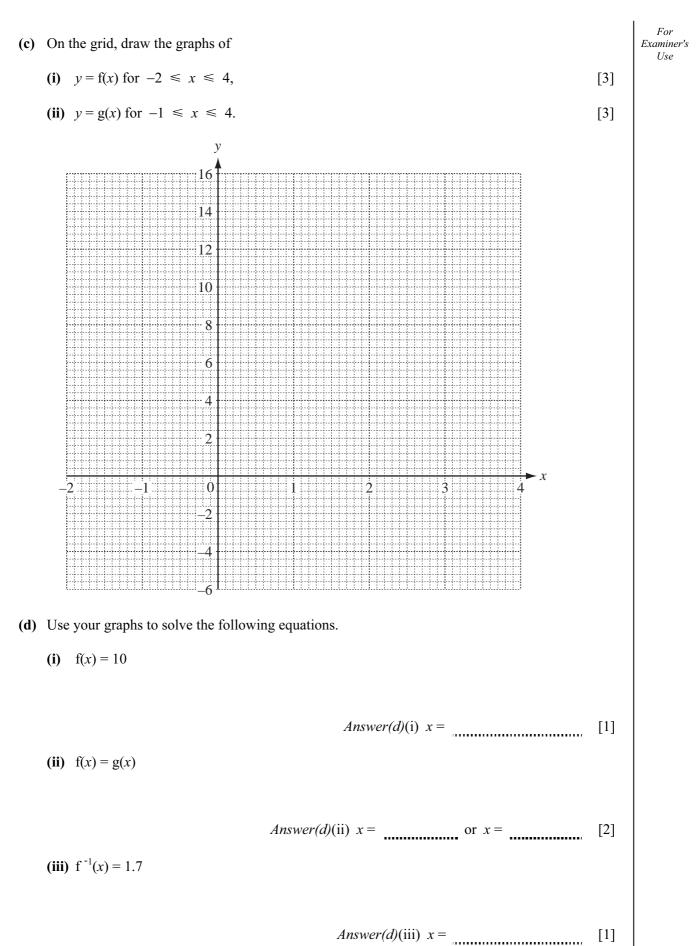
(b) g(x) = x(4-x)

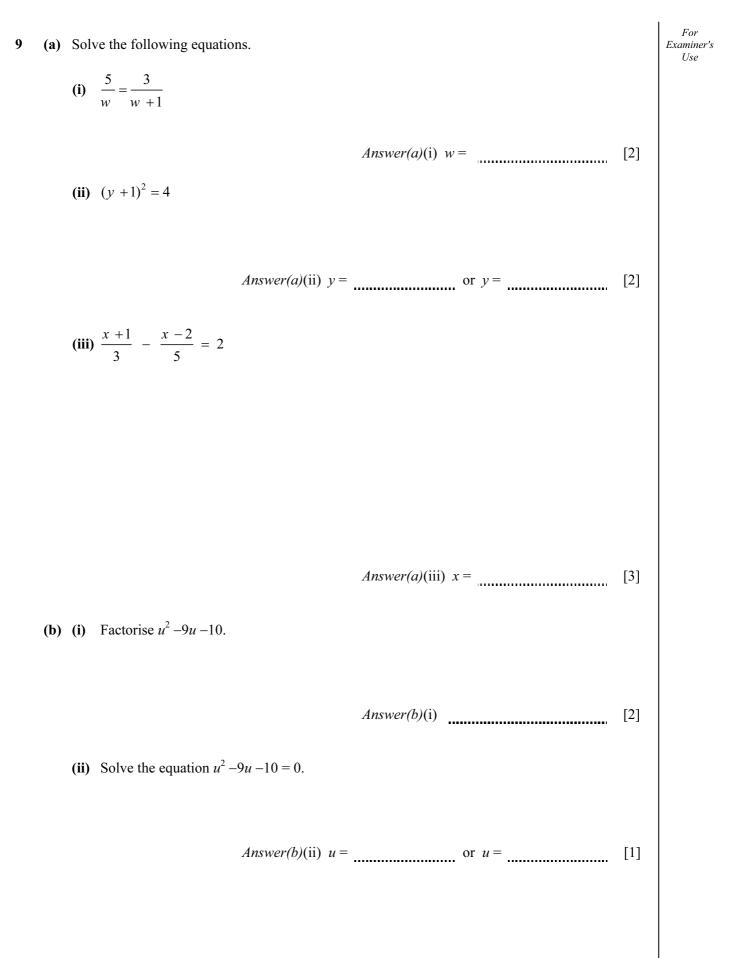
Complete the table.

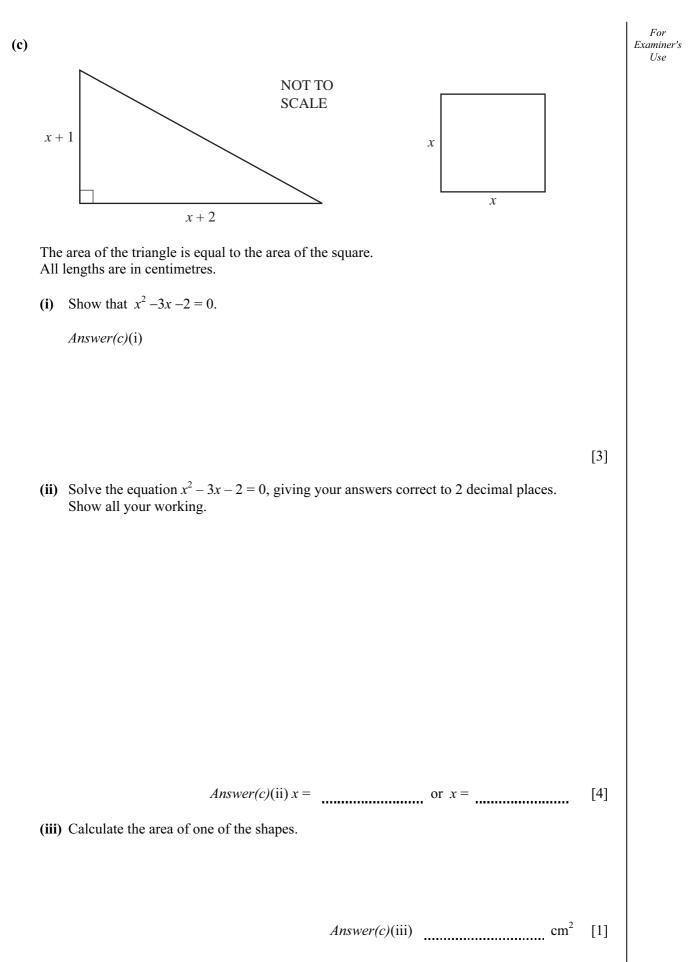
| x | -1 | 0 | 1 | 2 | 3 | 4 |
|---------------------|----|---|---|---|---|---|
| $y = \mathbf{g}(x)$ | | 0 | 3 | | 3 | 0 |

[2]

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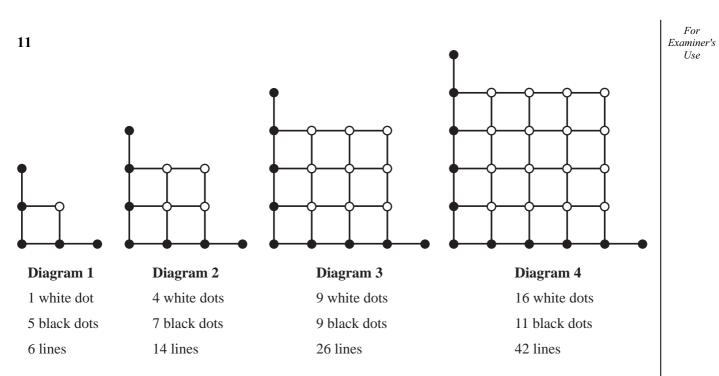
For 10 A company has a vehicle parking area of 1200 m² with space for x cars and y trucks. Examiner's Use Each car requires 20 m² of space and each truck requires 100 m² of space. (a) Show that $x + 5y \le 60$. Answer(a) [1] (b) There must also be space for (i) at least 40 vehicles, (ii) at least 2 trucks. Write down two more inequalities to show this information. Answer(b)(i) [1] Answer(b)(ii) [1] (c) One line has been drawn for you. On the grid, show the three inequalities by drawing the other two lines and shading the unwanted regions. y 40 30 20 10 х 10 20 30 40 50 0 60 [4]

| (d) | Use your graph to find the largest possible number of trucks. | For Examiner's Use |
|-----|--|--------------------------|
| | Answer(d) [1] | |
| (e) | The company charges \$5 for parking each car and \$10 for parking each truck. Find the number of cars and the number of trucks which give the company the greatest possible income. | |
| | Calculate this income. | |
| | | |
| | | |
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| | | |
| | Answer(e) Number of cars = | |
| | Number of trucks = | |

Greatest possible income = \$

.....

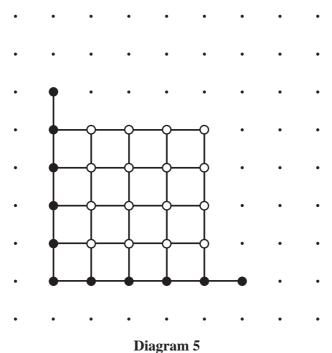
[3]



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The four diagrams above are the first four of a pattern.

(a) Diagram 5 has been started below.Complete this diagram and write down the information about the numbers of dots and lines.



Diagrame

..... white dots

..... black dots

..... lines

| (b) | Complete the information about the number of dots and lines in Diagram 8. | | | For Examiner's Use |
|-----|---|------------|-----|--------------------------|
| | Answer(b) | white dots | | |
| | | black dots | | |
| | | lines | [3] | |
| (c) | Complete the information about the number of dots in Diagram n . Give your answers in terms of n . | | | |
| | Answer(c) | white dots | | |
| | | black dots | [2] | |
| (d) | The number of lines in diagram <i>n</i> is $k(n^2 + n + 1)$. | | | |
| | Find | | | |
| | (i) the value of k , | | | |
| | (ii) the number of lines in Diagram 100. $Answer(d)(i) k =$ | | [1] | |
| | Answer(d)(ii) | | [1] | |

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