## UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

**International General Certificate of Secondary Education** 

## MARK SCHEME for the May/June 2009 question paper for the guidance of teachers

## 0607 CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/04 Paper 4 (Extended), maximum raw mark 120

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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Page 2	age 2 Mark Scheme: Teachers' version		Paper
	IGCSE – May/June 2009	0607	04

M marks are given for a correct method.

A marks are given for an accurate answer following a correct method.

**B** marks are given for a correct statement or step.

**D** marks are given for a clear and appropriately accurate drawing.

**P** marks are given for accurate plotting of points.

E marks are given for correctly explaining or establishing a given result.

## **Abbreviations**

cao correct answer only
cso correct solution only
ft follow through
oe or equivalent
soi seen or implied
ww without working
www without wrong working

Page 3	Mark Scheme: Teachers' version	Syllabus	Paper
	IGCSE – May/June 2009	0607	04

1 (a)	200 (or 2200) ÷ 20 10 (or 200) × 11 oe	M1 M1	Implied by 10 Independent
(b)	57.5(0)	B2	If <b>B0</b> , <b>M1</b> for $\frac{50 \times 5 \times 3}{100}$ oe (Implied by 7.50)
(c)	67.49 as final answer	В3	If <b>B0</b> , <b>M2</b> for $60\left(1 + \frac{4}{100}\right)^3$ oe <b>M1</b> for × 1.04 more than once oe 67.49 or 67.5 imply <b>M2</b>

2 (a)	37.2 (or 37.20 – 37.21)	B1	
<b>(b)</b>	37	B1	
(c)	36	B1	
(d)	36	B1	
(e)	2	B1	[5]

3 (a)	(x+2y)(2+p)	B2	<b>B1</b> for $2(x+2y) + p(x+2y)$ o.e.
(b)	Reasonable sketch of parabola (U shape) cutting <i>x</i> -axis either side of <i>y</i> -axis – dep –2.16, 1.16	M1 M1dep A1, A1	If using formula, <b>M1</b> for $\sqrt{2^2 - 4(2)(-5)}$ seen and if form $\frac{p + (or -)\sqrt{q}}{r}$ then <b>M1</b> for $p = -2$ and $r = 2 \times 2$ $\left(\frac{-2 \pm \sqrt{44}}{4}\right)$ <b>SC1</b> for $-2.2$ , 1.2 or $-2.158$ , 1.158 with or without working <b>SC2</b> for $-2.16$ , 1.16 without working
(c)	$y = k\sqrt{w}$ $4 = k\sqrt{9}$	M1 M1	If using $\frac{y}{4} = \frac{\sqrt{36}}{\sqrt{9}}$ M2
	$(y) = 8 \qquad \text{www3}$	A1	$k = \frac{4}{3}$ implies <b>M2</b>
			[9]

Page 4	Page 4 Mark Scheme: Teachers' version		Paper
	IGCSE – May/June 2009	0607	04

4 (a)	K	B1	
(b)	A C	B2	SC1 for any 4 of the 5 parts shaded
(c)	4	B2	Allow <b>B2</b> for embedded if clear If <b>B0</b> , <b>B1</b> for Venn diagram with universal set containing 2 intersecting sets or 6+10-(20-8) or better seen or $10-x+x+6-x=20-8$ oe [5]

5 (a) (i)	Correct shape Point of inflexion at origin	B1 B1dep	
(ii)	Correct shape Correct position relative to axes	B1 B1dep	
(b)	0, 4 cao	B1,B1	Do not allow any decimals in answers
(c)	(3, -27) cao	B1,B1	Do not allow any decimals in answers
(d)	-2.33 (-2.325), 4.41 (4.407 – 4.408)	B1,B1	SC1 for -2.3 and 4.4 [10]

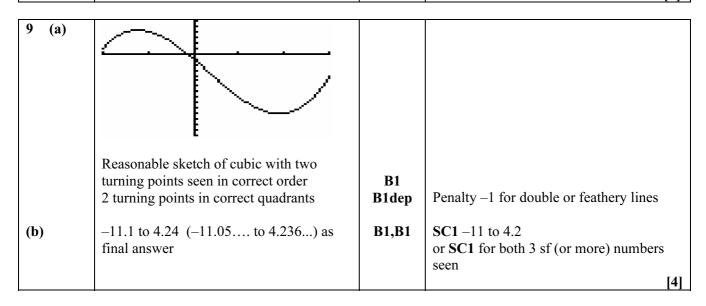
Page 5	Mark Scheme: Teachers' version	Syllabus	Paper
	IGCSE – May/June 2009	0607	04

6 (a)		$\frac{35 + \text{their}(1\frac{3}{4} \times 4)}{2\frac{1}{2} + 1\frac{3}{4}}$		M2	M1 for $1\frac{3}{4} \times 4$ or 7 seen	
		9.88 (9.882)	www3	A1		
(b)	(i)	10 ÷ 12.6 × 60 oe 47.6 (47.61 – 47.62)	www2	M1 A1	10 ÷ 0.21, 0.7936 × 60 Allow 48 also www2	
	(ii)	12.6 ÷ 1.05 oe 12	www2	M1 A1		[7]

7 (a) (i)	+ 1, then ÷ 2 or $\frac{y+1}{2}$ or $x = 2y-1$	M1	
	$\frac{x+1}{2}$ oe www2	A1	$\frac{y+1}{2}$ scores <b>M1</b> only
(ii)		B1	Reasonable sketch to be close to (-1,0), (0, 0.5) and (1, 1) 2 mm accuracy
(b) (i)	$\sqrt[3]{x}$ oe	B1	
(ii)		B1 B1dep	Correct shape. Intersecting $y = x^3$ between $x = 0.5$ and 1.5 and close to $y = x$ .
(iii)	Reflection $y = x$	B1 ft B1 ft	ft only if their graph is a reflection correct or ft [8]

Page 6	Mark Scheme: Teachers' version	Syllabus	Paper
	IGCSE – May/June 2009	0607	04

8 (a)	(i)	2.3.5	M2	M1 for correct implicit equation $7^2 =$ Any other method must be <b>complete</b> and scores M2
		120°	A1	Without any working <b>SC2</b> If <b>M0</b> , but 60° after some working <b>SC1</b> Radians answer 2.09 without working <b>SC1</b>
	(ii)	0.5 × 3 × 5 sin(their 120) oe 6.5(0) (6.495) ft www2	M1 A1 ft	(For Hero's formula s = 7.5) <b>ft</b> their angle with relevant sides
(b)	(i)	(0)40	B1	
	(ii)	280 cao	B2	M1 for 100 (or 220 – their (a)(i)) at <i>P</i> or 80 (or their (a)(i) – 40) at <i>B</i> soi



Page 7 Mark Scheme: Teachers' version		Syllabus	Paper
	IGCSE – May/June 2009	0607	04

10			Throughout the question ratios score zero.  If using decimals, 2 s.f. correct answers – penalty of 1 once Use of words e.g. 5 in 28 or 5 out of 28, correct answers – penalty of one once.  For method marks only accept probabilities between 0 and 1
(a) (i)	$\frac{14}{28}$ oe, $\frac{5}{28}(0.179)$ , $\frac{9}{28}(0.321)$	B1,B1,B1	0.5, 0.1785 – 0.1786, 0.3214
(ii), (iii)			
(b) (i)	$\frac{14}{28} \times \frac{14}{28}$	M1	
	$\frac{196}{784}$ oe $(\frac{1}{4})$ www 2	A1	
(ii)	$2 \times \frac{14}{28} \times \frac{5}{28}$ oe	M1	
	$\frac{140}{784}$ oe $\left(\frac{5}{28}\right)$ , $(0.179)$	<b>A1</b>	0.1785 – 0.1786
(iii)	$1 - \frac{9}{28} \times \frac{9}{28}$ oe	M1	
	$\frac{703}{784}$ oe (0.897) www 2	<b>A1</b>	0.8966 – 0.8967 <b>[9]</b>

11 (a)	Similar	B1	Allow enlargement oe
(b) (i)	$\frac{QT}{2.5} = \frac{6}{3} \qquad \text{oe}$ 5 \qquad \text{www2}	M1 A1	
(ii)	$\left(\frac{6}{3}\right)^2$ or $k^2$ oe 11.2 cao www2	M1 A1	k must be from (i)
(iii)	$\sin X = \frac{\sin 26.5}{3} \times 2.5$	M2	M1 for any correct implicit form e.g. $\frac{\sin X}{2.5} = \frac{\sin 26.5}{3}$
	21.8 (21.82 – 21.83) www3	<b>A1</b>	Radians 0.9546 ww implies <b>M2</b> [8]

Page 8 Mark Scheme: Teachers' version		Syllabus	Paper
	IGCSE – May/June 2009	0607	04

12 (a)	$\frac{30}{360} \times \pi \times 24$ oe 6.28 (6.28 – 6.284) www2	M1 A1	Accept $2\pi$
	0.28 (0.28 – 0.284) www2	AI	Accept 2 n
(b)	$\frac{30}{360} \times \pi \times 12^2$	M1	
	37.7 (37.68 – 37.70) www2	A1	Accept $12 \pi$
(c)	their <b>(b)</b> × 3	M1	
	113 (113.0 – 113.1) <b>ft</b> www2	A1ft	Accept $36\pi$
(d)	their <b>(b)</b> × 2	M1	
	$2 \times 3 \times 12$	M1	
	their (a) $\times$ 3	M1	
	166 (166.2 – 166.3) cao www4	<b>A1</b>	Accept $30 \pi + 72$
			[10]

13 (a)	10 correct points	В3	<b>B2</b> for 8 or 9 correct points, <b>B1</b> for 6 or 7 points
(b)	Positive	B1	Ignore any wording which does not spoil answer Accept accurate description linking height to points
(c) (i) (ii)	179.9, 53.2	B1,B1	Accept 180 for 179.9
(d) (i)	(p) = 0.386h - 16.2 $(0.3855 - 0.3856) (-16.16)$	B2	If seen in correct form <b>B1</b> for 0.386, <b>B1</b> for –16.2. (Allow 0.39) <b>SC1</b> if in correct form and both terms correct to 2 sf
(ii)	Line through their (179.9, 53.2) seen to be plotted.	B1	Must be ruled and be from at least 165 to 190
	Would extend to <i>p</i> -axis within 3 squares of 45	<b>B</b> 1	Gradient must be positive SC1 if accurate and not ruled
(iii)	52 or 53 or 54	B1	Must be integer [11]

Page 9 Mark Scheme: Teachers' version		Syllabus	Paper
	IGCSE – May/June 2009	0607	04

14 (a)	y = 2x through (0, 0) and (5, 10) x + y = 10 through (10, 0) and (0, 10) 2x + y = 10 through (5, 0) and (0, 10)	L1 L1 L1	Each straight line ruled Max 2 if not ruled Allow 2 mm accuracy at points indicated
(b)	Correct region unshaded ft	B1 ft	Allow indication by label <i>T</i> if clear ft <b>only</b> $y = \frac{1}{2}x$ for $y = 2x$
(c) (i)	3.2 – 3.4 ft	B1 ft	ft their region in (b) if <b>B1</b> scored (ans 6.6if ft in (b)) or region T <sub>2</sub> if (a) correct (ans 2.5).
(ii)	3	B1	ft their region in <b>(b)</b> if <b>B1</b> scored (ans 6 if ft in <b>(b)</b> ) or region T <sub>2</sub> if <b>(a)</b> correct (ans 2).
(d)	1, 9 2, 7 ft	B1 ft B1 ft	ft their $T$ . Only full ft solutions and at least 2 pairs score <b>B2</b> ft.  Treat as ordered pairs unless labelled $x =, y =$ <b>SC1</b> if all reversed [8]

4 = ( ) (0)			
15 (a) (i)	30	B1	
(ii)	360	B1	Not $x =$
	X		
(iii)	$\frac{360}{x+8}$	B1	Not $x =$
(b) (i)	$\frac{360}{x} - \frac{360}{x+8} = 16$ oe	M2	SC1 for sign errors
	360(x+8) - 360x = 16x(x+8)  oe	M1	Dep on M2 or SC1, for correctly putting all three terms over common denominator or multiplying throughout by $x$ and $x + 8$ .
	$360x + 2880 - 360x = 16x^{2} + 128x$ $16x^{2} + 128x - 2880 = 0$ $x^{2} + 8x - 180 = 0$	E1	Dependent on <b>M2 M1</b> .  At least one of these two lines oe before final conclusion without any errors or omissions. Condone the absence of = 0 only once
(ii)	(x+18)(x-10)	B2	If <b>B0</b> , <b>SC1</b> for $(x \pm p)(x \pm q)$ with values of 10 and 18 for $p$ and $q$
(iii)	-18, 10 ft	B1 ft	Correct or ft SC1
(iv)	10	B1 ft	Can ft a positive root [11]