UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS International General Certificate of Secondary Education

MARK SCHEME for the May/June 2010 question paper

for the guidance of teachers

0607 CAMBRIDGE INTERNATIONAL MATHEMATICS

0607/04 Paper 4 (Extended), maximum raw mark 120

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

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Page 2	Mark Scheme: Teachers' version	Syllabus	Paper
	IGCSE – May/June 2010	0607	04

- M marks are given for a correct method.
- A marks are given for an accurate answer following a correct method.
- **B** marks are given for a correct statement or step.
- **D** marks are given for a clear and appropriately accurate drawing.
- **P** marks are given for accurate plotting of points.
- E marks are given for correctly explaining or establishing a given result.
- ft follow through
- oe or equivalent
- soi seen or implied
- www without wrong working

1	(a)	7.60	B2	[2]	If B0, SC1 for 12.4
	(b)	3.3 (33)	B2	[2]	If B0, SC1 for 3.2 (3.22 – 3.23) or M1 for $\frac{0.05}{1.5} \times 100$ oe
	(c)	0.75	B2	[2]	If B0, M1 for 0.84 ÷ 1.12 oe
	(d)	5 www 3		[3]	B2 for $4.937 - 4.938$ or $\frac{\log(\frac{4}{3})}{\log 1.06}$ or M1 for using 0.75×1.06^n or $1 \div 1.06^n$ oe, <i>n</i> integer >1
2	(a)	$x^{3} - x^{2} + x + x^{2} - x + 1$ = $x^{3} + 1$	M1	[2]	Must see 6 correct terms, condoning one sign error Correct conclusion with no errors or omissions
	(b)	Use of $b^2 - 4ac$ (may be in formula) or sketch of U – shaped parabola or $(x - 0.5)^2 = k$	M1	[3]	
		For $\sqrt{-3}$ or for not touching x – in sketch or $k = -0.75$	A1		
		Correct conclusion (e.g. not real or square root of a negative number or graph does not touch <i>x</i> -axis)	R1		Dependent on M1 A1
	(c) (i)	9	B1	[1]	
	(ii)	0	B1	[1]	
	(iii)	$\sqrt[3]{x-1}$ final answer	B3	[3]	If B0, M1 for $y - 1 = x^3$ (correct re- arrangement)
					M1 for $\sqrt[3]{y-1} = x$ (correct cube root) M1 for interchanging <i>x</i> and <i>y</i> (this may be done first and other 2 M's follow)
	(iv)	28 cao	B1	[1]	

Page 3	Mark Scheme: Teachers' version	Syllabus	Paper
	IGCSE – May/June 2010	0607	04

		D1	
3 (a)	{3, 6, 9, 12}	B1	
	$\{1, 2, 3, 5, 6, 10\}$	B1	
	{6, 7, 8, 9, 10, 11}	B1 [3]	
(b)		B2ft [2]	12 elements must be seen, each only once.
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$		Correct or ft their (a) If B0, B1 for 6 or 7 regions correct or ft their (a)
(c) (i)	3, 6	B1ft [1]	Correct or ft their Venn diagram
(ii)	3, 6, 7, 8, 9, 10, 11, 12	B1ft [1]	Correct or ft their Venn diagram
(iii)	3, 6, 10	B1ft [1]	Correct or ft their Venn diagram
(iv)	4, 7, 8, 9, 11, 12	B1ft [1]	Correct or ft their Venn diagram
(v)	11 cao	B1 [1]	
4 (a)	1005 www 3	M1	M1 for at least 3 correct mid-interval values seen then (985, 995, 1002.5, 1007.5, 1015, 1030)
		M1	M1 for evidence of using $\Sigma fx \div 100$ with values of <i>m</i> in the intervals (3940 + 9950 + 50125 +
		A1 [3]	$\frac{1005.3}{1005.3}$
(b) (i)	0.4, 1, 10, 4, 0.8, 0.4	B3 [3]	If B0, B2 for 4 or 5 correct, B1 for 2 or 3 correct
(ii)	Accurate histogram	M1	6 histogram rectangles with at least 4 correct widths
		A1	6 correct widths
		A2ft [4]	6 correct heights, A1ft for 4 or 5 correct heights

	Page 4 Mark Scheme: Teachers' version		Syllabus Paper	•			
			IGCSE – May/June 20	010		0607 04	
5	(a)	Three	e reasonable branches	B1 B1 B1	[3]	Must be above <i>x</i> -axis and always increasing roughly towards $x = -1$ Inverted U shape below <i>x</i> -axis and roughly between $x = -1$ and $x = 3$ Must be above <i>x</i> -axis and always decreasing roughly from $x = 3$	
	(b)	<i>x</i> = -1	1, x = 3, y = 0	B1B	1B1 [3]		
	(c)	(1, -0	0.25)	B1B	1[2]	If B0, allow SC1 for both inexact val of correct answer e.g. (1.0000011, -0.24999)	ues
	(d)	$(x \in R)$	R), $x \neq -1, x \neq 3$ oe	B1B	1ft [2]	B1 for $x \neq -1$ B1 for $x \neq 3$ oe ft (b) or correct. isw limits from grid	r
		<i>y</i> ≤ −(0.25, y > 0	B1B	1ft [2]	B1 for $y \le -0.25$ B1 for $y > 0$ (f(x) Ok for y and condone x for y ft (c) for their -0.25 and (b) for their or correct.	
	(e) (i)	2		B1	[1]		
	(ii)	4		B1	[1]		
6	(a)	250		B2	[2]	If B0, M1 for 100 ÷ 5.6 × 14	
	(b) (i)	20		B2	[2]	If B0, M1 for 72 ÷ 3.6 oe	
	(ii)	0.225	ft	B2ft	[2]	ft 4.5 ÷ their (b)(i). If B0, M1 for 4.5 their (b)(i)	÷
7	(a)	$\frac{x}{5}$		B1	[1]		
	(b) (i)	$\frac{x+1}{4}$	3	B1	[1]		
	(ii)	$\frac{x}{5} + \frac{y}{5}$	$\frac{x+13}{4} = 46$	B1ft	[1]	ft their (a) and (b)(i) if fractions of the form $\frac{x}{l}, \frac{x+p}{q}, q \neq l$ neither = 1	e
	(iii)	95		B3ft dep		ft dependent on B1 in (ii) but if $p = 0$, SC2 for 102.(22) If B0, M1for "4x"+"5x"+"65" o.e. (or better) then M1 (dependent) for "4x"+"5x"+"65" ="920" o.e. (or better) these two M's may still be over comm denominator	
	(c)	4.41 t	ft	B2ft	[2]	ft (2 × their (b)(iii) + 13) ÷ 46 If B0, M1 for (2 × their (b)(iii) + 13) ÷ oe, 4.4, 4.413 imply M1	- 46

	Page	5	Mark Scheme: Teachers'	versi	on		Syllabus	Paper
			IGCSE – May/June 2	010			0607	04
					543	<u> </u>		
8	(a)	Posit	ive	B1	[1]			
		0.0		DI	F 1 1			
	(b) (i)	9.6		B1	[1]			
	(ii)	11		B1	[1]			
	(iii)	1.2(0	r + 1.5(0)	B1B			or $1.2(0)r(1.198) +$	
					[2]		1.5(0) (1.497) wit Allow <i>x</i> for <i>r</i> .	$\operatorname{tn} c, m \operatorname{not}$
							for 1.2(0) and 1.5(0)	seen
9	(a)	1190	(1193) cao www 3	M2 A1	[3]	[3] $\frac{M2 \text{ for correct explicit expression}}{\frac{180}{\sin 8.6} \times \sin 82.5}$ or M1 for implicit sine rule $\frac{AK}{\sin 82.5} = \frac{180}{\sin 8.6}$ SC2 for correct answer by other n if working seen		
	(b)	1199	– 1200 cao www 3	M1 A2	[3]	A1 fo SC2	for $a^2 + 770^2 - 2 \times 1410 \times 1439 990.8$ for correct answer by e of other triangle if y	other method
	(c)	5685	00 – 569400 cao www 3	M2 A1	[3]	82.5 o.e.	for $0.5 \times 180 \times$ their (- 8.6) + 0.5 × 1410 × 1 for area of one triar	770 × sin58.3
	(d)	1490	– 1500 cao www 5	B2 M1 A2	[5]	angle If thi meth M1 f e.g. 1 cos (2	or angle $TDK = 32.96$ e $DKT = 88.36 - 88.6$ s B0, then M1 for con- od for finding one of for correct explicit exp r AT^2 $80^2 + 1410^2 - 2 \times 18$ 82.5 + their angle $TDor 2 235 000 to 2 240$	1 frect full these angles pression for $0 \times 1410 \times \frac{1}{2}$
	(e)	28.2	cm	B2	[2]	If B0	, SC1 for figures 282	2

Page 6	Mark Scheme: Teachers' version	Syllabus	Paper
	IGCSE – May/June 2010	0607	04

10 ()	D.:	D1	F 4 7	
10 (a)	Prism	B1	[1]	
(b) (i)	5.25	B2	[2]	If B0, M1 for 0.5 $(3 + 4) \times 1.5$ oe
(ii)	810.6 (or 811)	B3ft	[3]	ft their (b)(i) \times 154.4. If B0 then M2 for their (b)(i) \times 8 \times 19.3 or M1 for their (b)(i) \times 8.
(iii)	91.78 – 91.8 cao www 4	M3 A1	[4]	M1 for $(BC^2) = 1.5^2 + 0.5^2$ (implied by 1.58 or 2.5) may be on diagram or near to diagram M1 for 2 × their (b)(ii) M1 for (3 + 4 + 2 × their <i>BC</i>) × 8 (<i>BC</i> must be from Pythagoras or trigonometry)
(c)	24 ft	M1 A2ft	[3ft]	ft 20 000 ÷ their (b)(ii) M1 for mass of box ÷ mass of one bar (implied figs 2466 to 2467) A1 for 24.66 – 24.67 or 24.6 or 24.7 (i.e. 1 dp) ft Answers less than 1 can only have M1
11 (a)	$\frac{1}{6}$ oe	B1	[1]	Penalty of –1 for 2 sf decimals or percentages. Do not accept ratio or worded forms.
(b) (i)	2 then 4 branch tree diagram 3 pairs of correct probabilities $\frac{5}{6}, \frac{1}{6}$ and $\frac{7}{8}, \frac{1}{8}$ and $\frac{1}{4}, \frac{3}{4}$ on a 2 then 4 branch tree diagram	B1 B1 B1 B1	[4]	B1 each correct pair with correct orientation If incorrect orientation check labelling for the three pairs
(ii)	$\frac{37}{48}(0.7708)$ cao	В3	[3]	If B0, M2 for $\frac{5}{6} \times \frac{7}{8} + \frac{1}{6} \times \frac{1}{4}$
(iii)	0.00063 cao	B2	[2]	or M1 for one of the above products. If B0, M1 for $(1 - \text{their } (\mathbf{b})(\mathbf{ii}))^5$ or $\left(\frac{5}{6} \times \frac{1}{8} + \frac{1}{6} \times \frac{3}{4}\right)^5$ ft their tree oe
(iv)	148	B1ft	[1]	0.000632 implies M1

Page 7	Mark Scheme: Teachers' version	Syllabus	Paper
	IGCSE – May/June 2010	0607	04

12 (a)	$\begin{array}{c} 192\\ 3 \times 2^n \end{array} \text{ oe} \end{array}$	B1 B2	[1] [2]	e.g. $6 \times 2^{n-1}$ If B0, B1 for 2^k , $k \in \mathbb{Z}$ in final answer
(b)	24 $n^2 - 2n$ or $(n-1)^2 - 1$ oe	B1 B3	[1] [3]	If B0, M2 for recognising form $an^2 + bn + c$, $a \neq 0$, b and c not both zero Allow other variables If B0 M0, M1 for reaching second differences of 2