### UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS

GCE Advanced Subsidiary Level and GCE Advanced Level

# MARK SCHEME for the October/November 2011 question paper for the guidance of teachers

## 9709 MATHEMATICS

9709/32

Paper 3, maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• Cambridge will not enter into discussions or correspondence in connection with these mark schemes.

Cambridge is publishing the mark schemes for the October/November 2011 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.

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### **Mark Scheme Notes**

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.
  B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

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The following abbreviations may be used in a mark scheme or used on the scripts:

AEF	Any Equivalent Form (of answer is equally acceptable)
AG	Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
BOD	Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
CAO	Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
CWO	Correct Working Only – often written by a 'fortuitous' answer
ISW	Ignore Subsequent Working
MR	Misread
PA	Premature Approximation (resulting in basically correct work that is insufficiently accurate)
sos	See Other Solution (the candidate makes a better attempt at the same question)
SR	Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

## **Penalties**

- MR −1 A penalty of MR −1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR −2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

	•	GCE AS/A LEVEL – October/November 2011 9709	32	
1		as $e^{2x} - e^x - 6 = 0$ , or $u^2 - u - 6 = 0$ , or equivalent	B1 M1	_
	Solve a 3-term quadratic for $e^x$ or for $u$			
		uplified solution $e^x = 3$ or $u = 3$	A1	F 4 7
	Obtain fin	al answer $x = 1.10$ and no other	A1	[4]
2	EITHER:	Use chain rule	M1	
		obtain $\frac{dx}{dt} = 6 \sin t \cos t$ , or equivalent	A1	
		obtain $\frac{dy}{dt} = -6\cos^2 t \sin t$ , or equivalent	A1	
		Use $\frac{dy}{dx} = \frac{dy}{dt} \div \frac{dx}{dt}$	M1	
		Obtain final answer $\frac{dy}{dx} = -\cos t$	A1	
	OR:	Express y in terms of x and use chain rule $\frac{dy}{dx} = x^{-\frac{1}{2}}$	M1	
		Obtain $\frac{dy}{dx} = k(2 - \frac{x}{3})^{\frac{1}{2}}$ , or equivalent	A1	
		Obtain $\frac{dy}{dx} = -(2 - \frac{x}{3})^{\frac{1}{2}}$ , or equivalent	A1	
		Express derivative in terms of <i>t</i>	M1	
		Obtain final answer $\frac{dy}{dx} = -\cos t$	A1	[5]
3	(i) <i>EITH</i>	ER: Attempt division by $x^2 - x + 1$ reaching a partial quotient of $x^2 + kx$	M1	
		Obtain quotient $x^2 + 4x + 3$ Equate remainder of form $lx$ to zero and solve for $a$ , or equivalent Obtain answer $a = 1$	A1 M1	
	OR:	Substitute a complex zero of $x^2 - x + 1$ in $p(x)$ and equate to zero	A1 M1	
	OR.	Obtain a correct equation in $a$ in any unsimplified form	A1	
		Expand terms, use $i^2 = -1$ and solve for $a$	M1	
		Obtain answer $a = 1$	A1	[4]
	[SR: The first M1 is earned if inspection reaches an unknown factor $x^2 + Bx + C$ and an equation in B and/or C, or an unknown factor $Ax^2 + Bx + 3$ and an equation in A and/or B. The second M1 is only earned if use of the equation $a = B - C$ is seen or implied.]			
	(ii) State	answer, e.g. $x = -3$	B1	
		answer, e.g. $x = -1$ and no others	B1	[2]
4	_	ariables and attempt integration of at least one side	M1	
		$m \ln(x+1)$	A1 M1	
	Obtain term $k \ln \sin 2\theta$ , where $k = \pm 1, \pm 2$ , or $\pm \frac{1}{2}$			
	Obtain correct term $\frac{1}{2} \ln \sin 2\theta$			
	Evaluate a constant, or use limits $\theta = \frac{1}{12}\pi$ , $x = 0$ in a solution containing terms $a \ln(x + 1)$ and			
	$b \ln \sin 2\theta$			
			A1√	
	Rearrange	and obtain $x = \sqrt{(2\sin 2\theta)} - 1$ , or simple equivalent	A1	[7]

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**Syllabus** 

**Paper** 

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5	(i)		ognisable sketch of a relevant graph over the given interval e other relevant graph and justify the given statement		B1 B1	[2]
	(ii)	Consider	the sign of sec $x - (3 - \frac{1}{2} x^2)$ at $x = 1$ and $x = 1.4$ , or equivalent	ent	M1	
		Complete	the argument with correct calculated values		A1	[2]
	(iii)	Convert ti	the given equation to $\sec x = 3 - \frac{1}{2}x^2$ or work <i>vice versa</i>		B1	[1]
	(iv)	Obtain fir	rect iterative formula correctly at least once hal answer 1.13 ficient iterations to 4 d.p. to justify 1.13 to 2 d.p., or show t	here is a sign change	M1 A1	
		in the inte	erval (1.125, 1.135) ressive evaluation of the iterative function with $x = 1, 2,$		A1	[3]
6	(i)	Use trig for Obtain α	imply $R = \sqrt{10}$ formulae to find $\alpha$ = 71.57° with no errors seen flow radians in this part. If the only trig error is a sign error	or in $cos(x - a)$ give	B1 M1 A1	[3]
	(ii)	Carry out Obtain an Use an ap Obtain se [Ignore an [Treat ans [SR: The $\cos 2\theta$ , or in the giv	cos <sup>-1</sup> $(2/\sqrt{10})$ correctly to at least 1 d.p. $(50.7684^{\circ})$ (All an appropriate method to find a value of $2\theta$ in $0^{\circ} < 2\theta < 18$ answer for $\theta$ in the given range, e.g. $\theta = 61.2^{\circ}$ propriate method to find another value of $2\theta$ in the above racond angle, e.g. $\theta = 10.4^{\circ}$ , and no others in the given range as swers outside the given range.] swers in radians as a misread and deduct A1 from the answer use of correct trig formulae to obtain a 3-term quadratan $2\theta$ earns M1; then A1 for a correct quadratic, M1 for one range, and A1 + A1 for the two correct answers (candidata spurious roots to get the final A1).]	o° ange angles.] tic in tan $\theta$ , sin $2\theta$ , btaining a value of $\theta$	B1√ M1 A1 M1 A1	[5]

7	(i)		rect method to express $\overrightarrow{OP}$ in terms e given answer	ns of $\lambda$		M1 A1	[2]
	(ii)	EITHER:	Use correct method to express so in terms of $\lambda$ Using the correct method for the moduli and express $\cos AOP = \cos AOP = AOP$	e moduli, divide scal	ar products by products $\lambda$ , or in terms of $\lambda$ and $O$	M1 of <i>P</i> M1*	
		OR1:	Use correct method to express $C$ of $\lambda$ Using the correct method for the product of the relevant moduli a or $\lambda$ and $OP$	e moduli, divide eac	th expression by twice the expression by	M1 he	
		Obtain a c	correct equation in any form, e.g.	$\frac{9+2\lambda}{3\sqrt{(9+4\lambda+12\lambda^2)}} =$	$=\frac{11+14\lambda}{5\sqrt{(9+4\lambda+12\lambda^2)}}$	A1	
		Solve for $\lambda$ Obtain $\lambda$ =			N	M1(dep*) A1	[5]
		[SR: The	M1* can also be earned by equation in $\lambda$	-		_	
		spurious n	t non-exact working giving a value attive root of the quadratic in $\lambda$ w a solution reaching $\lambda = \frac{3}{8}$ after	is rejected.]	_		
		OP to see cases.]	ore 4/5. The marking will run	M1M1A0M1A1, or	M1M1A1M1A0 in su	ch	
	(iii)	Verify the	given statement correctly			B1	[1]
8	(i)	Obtain on Obtain a s	elevant method to determine a core of the values $A = 3$ , $B = 4$ , $C = 0$ second value e third value			M1 A1 A1 A1	[4]
	(ii)	Integrate a Obtain ter	and obtain term $-3 \ln(2-x)$ and obtain term $k \ln(4+x^2)$ rm $2 \ln(4+x^2)$ correct limits correctly in a comp	alete integral of the f	orm	B1√ M1 A1√	
		$a \ln(2-x)$	$(a + b \ln(4 + x^2), ab \neq 0)$	new integral of tile it	J1111	M1	

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Obtain given answer following full and correct working

[5]

A1

(ii) Attempt integration by parts reaching $kx^2 \ln x \pm k \int x^3 \cdot \frac{1}{x} dx$ Obtain $\frac{1}{3}x^3 \ln x - \frac{1}{3} \int x^2 dx$ , or equivalent  Integrate again and obtain $\frac{1}{3}x^3 \ln x - \frac{1}{9}x^3$ , or equivalent  Use limits $x = 1$ and $x = e$ , having integrated twice  Obtain answer $\frac{1}{9}(2e^3 + 1)$ , or exact equivalent  [SR: An attempt reaching $ax^2(x \ln x - x) + b \int 2x(x \ln x - x) dx$ scores M1. Then give the first A1 for $I = x^2(x \ln x - x) - 2I + \int 2x^2 dx$ , or equivalent.]  10 (a) EITHER: Square $x + iy$ and equate real and imaginary parts to 1 and $-2\sqrt{6}$ respectively M1*  Obtain $x^2 - y^2 = 1$ and $2xy = -2\sqrt{6}$ A1  Eliminate one variable and find an equation in the other  Obtain $x^2 - x^2 - 6 = 0$ or $y^4 + y^2 - 6 = 0$ , or 3-term equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ A1  OR: Denoting $1 - 2\sqrt{6}i$ by $R c is\theta$ , state, or imply, square roots are $\pm \sqrt{R} c is(\frac{1}{2}\theta)$ and find values of $R$ and either $\cos \theta$ or $\sin \theta$ or $\tan \theta$ Obtain $\pm \sqrt{5}(\cos \frac{1}{2}\theta + i \sin \frac{1}{2}\theta)$ , and $\cos \theta = \frac{1}{5}$ or $\sin \theta = -\frac{2\sqrt{6}}{5}$ or $\tan \theta = -2\sqrt{6}$ Use correct method to find an exact value of $\cos \frac{1}{2}\theta$ or $\sin \frac{1}{2}\theta$ M1(dep*)  Obtain $\cos \frac{1}{2}\theta = \pm \sqrt{\frac{3}{5}}$ and $\sin \frac{1}{2}\theta = \pm \sqrt{\frac{2}{5}}$ , or equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent  [Condone omission of $\pm$ except in the final answers.]		Page 7		Mark Scheme: Teachers' version	Syllabus	Paper	•
Obtain correct derivative in any form Equate derivative to zero and solve for $x$ MI Obtain answer $x = e^{\frac{1}{2}}$ , or equivalent  (ii) Attempt integration by parts reaching $kx^3 \ln x \pm k \int x^3 \cdot \frac{1}{x} dx$ M1*  Obtain $\frac{1}{3}x^3 \ln x - \frac{1}{3} \int x^2 dx$ , or equivalent  A1 Integrate again and obtain $\frac{1}{3}x^3 \ln x - \frac{1}{9}x^3$ , or equivalent  Use limits $x = 1$ and $x = e$ , having integrated twice Obtain answer $\frac{1}{9}(2e^3 + 1)$ , or exact equivalent  [SR: An attempt reaching $ax^2 (x \ln x - x) + b \int 2x(x \ln x - x) dx$ scores M1. Then give the first A1 for $I = x^2 (x \ln x - x) - 2I + \int 2x^2 dx$ , or equivalent.]  10 (a) EITHER: Square $x + iy$ and equate real and imaginary parts to 1 and $-2\sqrt{6}$ respectively M1* Obtain $x^2 - y^2 = 1$ and $2xy = -2\sqrt{6}$ Eliminate one variable and find an equation in the other Obtain $x^3 - y^2 = 1$ and $2xy = -2\sqrt{6}$ Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ OR: Denoting $1 - 2\sqrt{6}i$ by $Rcis\theta$ , state, or imply, square roots are $\pm \sqrt{R}cis(\frac{1}{2}\theta)$ and find values of $R$ and either $\cos \theta$ or $\sin \theta$ or $\tan \theta$ Obtain $\pm \sqrt{5}(\cos \frac{1}{2}\theta + i \sin \frac{1}{2}\theta)$ , and $\cos \theta = \frac{1}{5}$ or $\sin \theta = -\frac{2\sqrt{6}}{5}$ or $\tan \theta = -2\sqrt{6}$ Use correct method to find an exact value of $\cos \frac{1}{2}\theta$ or $\sin \frac{1}{2}\theta$ M1(dep*) Obtain $\cos \frac{1}{2}\theta = \pm \sqrt{\frac{3}{5}}$ and $\sin \frac{1}{2}\theta = \pm \sqrt{\frac{2}{5}}$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A1 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A2 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A3 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent A4 Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equi				GCE AS/A LEVEL – October/November 2011	9709	32	
(ii) Attempt integration by parts reaching $kx^3 \ln x \pm k \int x^3 \cdot \frac{1}{x} dx$ Obtain $\frac{1}{3}x^3 \ln x - \frac{1}{3} \int x^2 dx$ , or equivalent  Integrate again and obtain $\frac{1}{3}x^3 \ln x - \frac{1}{9}x^3$ , or equivalent  Use limits $x = 1$ and $x = e$ , having integrated twice  Obtain answer $\frac{1}{9}(2e^3 + 1)$ , or exact equivalent  [SR: An attempt reaching $ax^2 (x \ln x - x) + b \int 2x(x \ln x - x) dx$ scores M1. Then give the first A1 for $I = x^2 (x \ln x - x) - 2I + \int 2x^2 dx$ , or equivalent.]  10 (a) EITHER: Square $x + iy$ and equate real and imaginary parts to 1 and $-2\sqrt{6}$ respectively M1*  Obtain $x^2 - y^2 = 1$ and $2xy = -2\sqrt{6}$ A1  Eliminate one variable and find an equation in the other  Obtain $x^3 - x^2 - 6 = 0$ or $y^4 + y^2 - 6 = 0$ , or $3$ -term equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ A1  OR: Denoting $1 - 2\sqrt{6}i$ by $R cis\theta$ , state, or imply, square roots are $\pm \sqrt{R} cis(\frac{1}{2}\theta)$ and find values of $R$ and either $\cos \theta$ or $\sin \theta$ or $\tan \theta$ Obtain $\pm \sqrt{5}(\cos \frac{1}{2}\theta + i \sin \frac{1}{2}\theta)$ , and $\cos \theta = \frac{1}{5}$ or $\sin \theta = -\frac{2\sqrt{6}}{5}$ or $\tan \theta = -2\sqrt{6}$ Use correct method to find an exact value of $\cos \frac{1}{2}\theta$ or $\sin \frac{1}{2}\theta$ Obtain $\cos \frac{1}{2}\theta = \pm \sqrt{\frac{1}{3}}$ and $\sin \frac{1}{2}\theta = \pm \sqrt{\frac{2}{3}}$ , or equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent  [Condone omission of $\pm$ except in the final answers.]	9	(i)	Obtain co Equate de Obtain an	erivative in any form erivative to zero and solve for $x$ as $e^{-\frac{1}{2}}$ , or equivalent		A1 M1 A1	F.63
Obtain $\frac{1}{3}x^3 \ln x - \frac{1}{3}\int x^2 dx$ , or equivalent  Integrate again and obtain $\frac{1}{3}x^3 \ln x - \frac{1}{9}x^3$ , or equivalent  Use limits $x = 1$ and $x = e$ , having integrated twice  Obtain answer $\frac{1}{9}(2e^3 + 1)$ , or exact equivalent  [SR: An attempt reaching $ax^2(x \ln x - x) + b\int 2x(x \ln x - x) dx$ scores M1. Then give the first A1 for $I = x^2(x \ln x - x) - 2I + \int 2x^2 dx$ , or equivalent.]  10 (a) EITHER: Square $x + iy$ and equate real and imaginary parts to 1 and $-2\sqrt{6}$ respectively M1*  Obtain $x^2 - y^2 = 1$ and $2xy = -2\sqrt{6}$ A1  Eliminate one variable and find an equation in the other  Obtain $x^4 - x^2 - 6 = 0$ or $y^4 + y^2 - 6 = 0$ , or $3$ -term equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ A1  OR: Denoting $1 - 2\sqrt{6}i$ by $Rcis\theta$ , state, or imply, square roots are $\pm \sqrt{R}cis(\frac{1}{2}\theta)$ and find values of $R$ and either $\cos \theta$ or $\sin \theta$ or $\tan \theta$ Obtain $\pm \sqrt{5}(\cos \frac{1}{2}\theta + i\sin \frac{1}{2}\theta)$ , and $\cos \theta = \frac{1}{5}$ or $\sin \theta = -\frac{2\sqrt{6}}{5}$ or $\tan \theta = -2\sqrt{6}$ Use correct method to find an exact value of $\cos \frac{1}{2}\theta$ or $\sin \frac{1}{2}\theta$ M1(dep*)  Obtain $\cos \frac{1}{2}\theta = \pm \sqrt{\frac{3}{5}}$ and $\sin \frac{1}{2}\theta = \pm \sqrt{\frac{2}{5}}$ , or equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent  [Condone omission of $\pm \exp$ in the final answers.]			Obtain an	iswer $y = -\frac{1}{2}e^{-x}$ , or equivalent		Al	[5]
Integrate again and obtain $\frac{1}{3}x^3 \ln x - \frac{1}{9}x^3$ , or equivalent  Use limits $x = 1$ and $x = e$ , having integrated twice  Obtain answer $\frac{1}{9}(2e^3 + 1)$ , or exact equivalent  [SR: An attempt reaching $ax^2 (x \ln x - x) + b \int 2x(x \ln x - x) dx$ scores M1. Then give the first A1 for $I = x^2 (x \ln x - x) - 2I + \int 2x^2 dx$ , or equivalent.]  10 (a) EITHER: Square $x + iy$ and equate real and imaginary parts to 1 and $-2\sqrt{6}$ respectively M1*  Obtain $x^2 - y^2 = 1$ and $2xy = -2\sqrt{6}$ A1  Eliminate one variable and find an equation in the other  Obtain $x^4 - x^2 - 6 = 0$ or $y^4 + y^2 - 6 = 0$ , or 3-term equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ OR: Denoting $1 - 2\sqrt{6}i$ by $R cis\theta$ , state, or imply, square roots are $\pm \sqrt{R} cis(\frac{1}{2}\theta)$ and find values of $R$ and either $\cos \theta$ or $\sin \theta$ or $\tan \theta$ Obtain $\pm \sqrt{5}(\cos \frac{1}{2}\theta + i\sin \frac{1}{2}\theta)$ , and $\cos \theta = \frac{1}{5}$ or $\sin \theta = -\frac{2\sqrt{6}}{5}$ or $\tan \theta = -2\sqrt{6}$ Obtain $\cos \frac{1}{2}\theta = \pm \sqrt{\frac{3}{5}}$ and $\sin \frac{1}{2}\theta = \pm \sqrt{\frac{2}{5}}$ , or equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent  [Condone omission of $\pm$ except in the final answers.]		(ii)	Attempt i	ntegration by parts reaching $kx^3 \ln x \pm k \int x^3 \cdot \frac{1}{x} dx$		M1*	
Use limits $x = 1$ and $x = e$ , having integrated twice Obtain answer $\frac{1}{9}(2e^3 + 1)$ , or exact equivalent A1  [SR: An attempt reaching $ax^2(x \ln x - x) + b \int 2x(x \ln x - x) dx$ scores M1. Then give the first A1 for $I = x^2(x \ln x - x) - 2I + \int 2x^2 dx$ , or equivalent.]  10 (a) EITHER: Square $x + iy$ and equate real and imaginary parts to 1 and $-2\sqrt{6}$ respectively M1*  Obtain $x^2 - y^2 = 1$ and $2xy = -2\sqrt{6}$ A1  Eliminate one variable and find an equation in the other M1(dep*)  Obtain $x^4 - x^2 - 6 = 0$ or $y^4 + y^2 - 6 = 0$ , or 3-term equivalent A1  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ OR: Denoting $1 - 2\sqrt{6}i$ by $R$ cis $\theta$ , state, or imply, square roots are $\pm \sqrt{R}$ cis $(\frac{1}{2}\theta)$ and find values of $R$ and either $\cos \theta$ or $\sin \theta$ or $\tan \theta$ M1*  Obtain $\pm \sqrt{5}(\cos \frac{1}{2}\theta + i \sin \frac{1}{2}\theta)$ , and $\cos \theta = \frac{1}{5}$ or $\sin \theta = -\frac{2\sqrt{6}}{5}$ or $\tan \theta = -2\sqrt{6}$ A1  Use correct method to find an exact value of $\cos \frac{1}{2}\theta$ or $\sin \frac{1}{2}\theta$ M1(dep*)  Obtain $\cos \frac{1}{2}\theta = \pm \sqrt{\frac{3}{5}}$ and $\sin \frac{1}{2}\theta = \pm \sqrt{\frac{2}{5}}$ , or equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent  [Condone omission of $\pm$ except in the final answers.]			Obtain $\frac{1}{3}$	$x^3 \ln x - \frac{1}{3} \int x^2 dx$ , or equivalent		A1	
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Obtain $\cos \frac{1}{2}\theta = \pm \sqrt{\frac{3}{5}}$ and $\sin \frac{1}{2}\theta = \pm \sqrt{\frac{2}{5}}$ , or equivalent  Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent  [Condone omission of $\pm$ except in the final answers.]  (b) Show point representing 3i on a sketch of an Argand diagram  Show a circle with centre at the point representing 3i and radius 2  B1						A1	
Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent [Condone omission of $\pm$ except in the final answers.]  (b) Show point representing 3i on a sketch of an Argand diagram B1 Show a circle with centre at the point representing 3i and radius 2 B1 $$				Use correct method to find an exact value of $\cos \frac{1}{2}\theta$ or si	$n\frac{1}{2}\theta$	M1(dep*)	
[Condone omission of ± except in the final answers.]  (b) Show point representing 3i on a sketch of an Argand diagram  Show a circle with centre at the point representing 3i and radius 2  B1  B1				Obtain $\cos \frac{1}{2}\theta = \pm \sqrt{\frac{3}{5}}$ and $\sin \frac{1}{2}\theta = \pm \sqrt{\frac{2}{5}}$ , or equivalent		A1	
(b) Show point representing 3i on a sketch of an Argand diagram  Show a circle with centre at the point representing 3i and radius 2  B1  B1  B1  B1				Obtain answers $\pm (\sqrt{3} - i\sqrt{2})$ , or equivalent		A1	
Show a circle with centre at the point representing 3i and radius 2 B1 $\sqrt{}$				[Condone omission of $\pm$ except in the final answers.]			
Show a circle with centre at the point representing 3i and radius 2 B1 $\sqrt{}$							
		<b>(b)</b>	_	· · · · · · · · · · · · · · · · · · ·			
SHAUE THE HIRCHOLOL HIS CHAIS				ircle with centre at the point representing 3i and radius 2 interior of the circle		B1√ B1√	
Carry out a complete method for finding the greatest value of arg $z$ M1  Obtain answer 131 8° or 2.30 (or 2.3) radions			Carry out	a complete method for finding the greatest value of arg $z$			

Obtain answer 131.8° or 2.30 (or 2.3) radians

[The f.t. is on solutions where the centre is at the point representing –3i.]

**A**1

[5]