MARK SCHEME for the May/June 2010 question paper

for the guidance of teachers

9709 MATHEMATICS

9709/11

Paper 11, maximum raw mark 75

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

• CIE will not enter into discussions or correspondence in connection with these mark schemes.

CIE is publishing the mark schemes for the May/June 2010 question papers for most IGCSE, GCE Advanced Level and Advanced Subsidiary Level syllabuses and some Ordinary Level syllabuses.



Page 2	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2010	9709	11

Mark Scheme Notes

Marks are of the following three types:

- M Method mark, awarded for a valid method applied to the problem. Method marks are not lost for numerical errors, algebraic slips or errors in units. However, it is not usually sufficient for a candidate just to indicate an intention of using some method or just to quote a formula; the formula or idea must be applied to the specific problem in hand, e.g. by substituting the relevant quantities into the formula. Correct application of a formula without the formula being quoted obviously earns the M mark and in some cases an M mark can be implied from a correct answer.
- A Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).
- B Mark for a correct result or statement independent of method marks.
- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol √ implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0. B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

- Wrong or missing units in an answer should not lead to the loss of a mark unless the scheme specifically indicates otherwise.
- For a numerical answer, allow the A or B mark if a value is obtained which is correct to 3 s.f., or which would be correct to 3 s.f. if rounded (1 d.p. in the case of an angle). As stated above, an A or B mark is not given if a correct numerical answer arises fortuitously from incorrect working. For Mechanics questions, allow A or B marks for correct answers which arise from taking *g* equal to 9.8 or 9.81 instead of 10.

Page 3	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2010	9709	11

The following abbreviations may be used in a mark scheme or used on the scripts:

- AEF Any Equivalent Form (of answer is equally acceptable)
- AG Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)
- BOD Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)
- CAO Correct Answer Only (emphasising that no "follow through" from a previous error is allowed)
- CWO Correct Working Only often written by a 'fortuitous' answer
- ISW Ignore Subsequent Working
- MR Misread
- PA Premature Approximation (resulting in basically correct work that is insufficiently accurate)
- SOS See Other Solution (the candidate makes a better attempt at the same question)
- SR Special Ruling (detailing the mark to be given for a specific wrong solution, or a case where some standard marking practice is to be varied in the light of a particular circumstance)

Penalties

- MR –1 A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through √" marks. MR is not applied when the candidate misreads his own figures this is regarded as an error in accuracy. An MR–2 penalty may be applied in particular cases if agreed at the coordination meeting.
- PA –1 This is deducted from A or B marks in the case of premature approximation. The PA –1 penalty is usually discussed at the meeting.

Page 4	Mark Scheme: Teachers' version	Syllabus	Paper
	GCE AS/A LEVEL – May/June 2010	9709	11

1	top u = k		
1	$\tan x = k$		
	(i) $\tan(\pi - x) = -k$	B1 [1]	co. www Mark final answers
	(ii) $\tan\left(\frac{\pi}{2}-x\right) = \frac{1}{k}$	B1 [1]	co. www
	(iii) $\sin x = \frac{k}{\sqrt{1+k^2}}$ from 90° triangle.	M1 A1 [2]	Any valid method – 90° triangle or formulae.
2	$\left(2x-\frac{3}{x}\right)^5$		
	(i) $32x^5 - 240x^3 + 720x$	3 × B1 [3]	co. SC B2 for other 3 terms (i.e. ascending)
	(ii) $\left(1+\frac{2}{x^2}\right)(32x^5-240x^3+720x)$		
	Coeff of $x (1 \times 720) + (2 \times -240)$ $\rightarrow 240$	M1 A1√ [2]	Looks at exactly 2 terms. co from his answer to (i) .
3	9 th term = 22, $S_4 = 49$		
	(i) $a+8d = 22$ 2(2a+3d) = 49 Soln of sim eqns $\rightarrow d = 1.5, a = 10$	B1 B1 M1 A1 [4]	co co Solution of two linear sim eqns. co
	(ii) $a + (n-1)d = 46$ Substitutes for a and $d \rightarrow n = 25$	M1 A1 [2]	Correct formula needed and attempt to solve. co.
4	$y = 6x - x^2$		
	Meets $y = 5$ when $x = 1$ or $x = 5$.	B1	со
	Integral = $3x^2 - \frac{1}{3}x^3$	M1 A1	attempt to integrate. co.
	Their limits (1 to 5) used $\rightarrow 30^{2/3}$ Area of rectangle = 20 Shaded area = $10^{2/3}$	DM1 B1√ A1 [6]	value at top limit – value at lower co to his <i>x</i> values co
	(integral of $6x - x^2 - 5$ B1, M1, A1 DM1 as above, then " $-5x$ " B1 $$ A1)		

	Page 5	Mark Scheme: Teachers' version			Syllabus	Paper
		GCE AS/A LEVEL – May/June 2010		9709	11	
5	$x \mapsto 2\sin^2 x$	$-3\cos^2 r$				
5	(i) $2(1-\cos^{2})$		M1	Uses $s^{2} + c^{2} = 1$		
	$\rightarrow 2-5$	$\cos^2 x \ (a=2, b=-5)$	Al	со		
	(ii) Values a	re -3 and 2	$\begin{bmatrix} 2 \\ B1\sqrt{B1} \\ [2] \end{bmatrix}$			
	(iii) $2-5\cos^2 d$		B1√			
		x = 0.6 5, 2.46 (accept 0.684)	$ \begin{array}{c} \text{B1} \\ \text{B1} \\ \text{B1} \\ \text{[3]} \end{array} $	co $\sqrt{100}$ for π – (first SC B1 for both 39		
6	$\frac{\mathrm{d}y}{\mathrm{d}x} = 3\sqrt{x} - \frac{1}{2}\sqrt{x}$					
	(i) $y = \frac{3x^{\frac{3}{2}}}{\frac{3}{2}}$	-6x(+c)	B2,1	Loses 1 for each er	rror – ignore + c	
	$\begin{array}{c} (9,2) 2 \\ \rightarrow c = 2 \end{array}$	= 54 - 54 + c.	M1 A1 [4]	Uses (9, 2) with in co.	tegration to find <i>c</i> .	
	(ii) $\frac{\mathrm{d}y}{\mathrm{d}x} = 0$		B1	Ignore any <i>y</i> -value		
	$\frac{\mathrm{d}^2 y}{\mathrm{d}^2 x} = \frac{3}{2}$	-	M1 A1	Any valid method.	co.	
7	$y = 2 - \frac{18}{2x+3}$	or ¾) Minimum	[3]			
	(i) <i>A</i> is (3, 0)	B1	Anywhere – but no	ot from given answ	ver
	$\frac{\mathrm{d}y}{\mathrm{d}x} = 18$	$(2x+3)^{-2} \times 2$	B1 B1	B1 for $18(2x+3)^{-2}$	2 , B1 for $\times 2$	
	If $x = 3$,	$m=rac{4}{9}$.				
	<i>m</i> of nor	$mal = -\frac{9}{4}$	M1	Use of $m_1 m_2 = -1$	with <i>m</i> from dy/dx	
	Equation	of normal $y = -\frac{9}{4}(x-3)$	M1	Correct method for	r normal	
	$\rightarrow 4y +$	9x = 27	A1	co (answer was giv	ven)	
	(ii) Normal 1	meets y-axis at $(0, 6^{3/4})$	[6]			
		eets y-axis at $(0, -4)$	M1 A1 [2]	Needs to put $x = 0$ curve. co	in both normal and	d

	Pa	ge 6	Mark Scheme: Teachers' version			Syllabus	Paper
			GCE AS/A LE	VEL – May/J	une 2010	9709	11
3	(i)	<i>y</i> -step $\div x$	r-sten = 2	M1	Gradient = y-step	÷ r sten used	
,	(1)	$\rightarrow m = 1$	step 2	Al	co	x step used	
				[2]			
	(ii)	Eqn of AG	y + 2 = -2(x - 3)	M1 A1 $$	Correct form of or	ne of lines. $$ to his	m
		•	C y - 22 = (x - 15)	A1	$\sqrt{1}$ to his <i>m</i>		
		•	y + 2x = 4, $y = x + 7$				
		$\rightarrow C(-1,$, 6)	A1 [4]	со		
	(iii)	<i>M</i> is (9, 1	0)	B1	со		
	()		ient is $-\frac{1}{2}$	M1	Use of $m_1m_2 = -1$		
		$\rightarrow 2y + z$	x = 29, y = x + 7	M1	Solve sim eqns for	r their BC & perp. b	is
		Sim eqns	$\rightarrow D(5, 12)$	A1 [4]	со		
9	(i)	$2x^2 - 12x$	$x+7 = 2(x-3)^2 - 11$	3 × B1	B1 for each value specifically quoted	- accept if <i>a</i> , <i>b</i> , <i>c</i> no d.	ot
	(ii)	Range of	f≥ -11	B1√ [1]	$\sqrt[n]{}$ to his "c". allow		
	(iii)	$2x^2 - 12x$	x + 7 < 21				
		$\rightarrow 2x^2 - 2x^2$	12x - 14 or	M1	3-term quadratic to	o 0 or $2(x-3)^2 < 32$	2
		$2(x-3)^2$	< 32				
			llues of 7 or -1	A1	Correct end-value	S	
		$\rightarrow -1 < x$	c < 7	A1 [3]	со		
	(iv)	gf(x) = 2($(2x^2 - 12x + 7) + k = 0$	M1 A1	Puts f into g. co.		
		Use of b^2		M1	Used correctly with	th quadratic	
			16(14+k)	A1			
		$\rightarrow k = 22$		[4]	co.		
10	\overrightarrow{OA}	= i + 3 j + 3	$3\mathbf{k}, \ \overrightarrow{OC} = 3\mathbf{i} - \mathbf{j} + \mathbf{k}.$				
		\overrightarrow{OP} \overrightarrow{OI}	$+\overrightarrow{OC} = 4\mathbf{i} + 2\mathbf{j} + 4\mathbf{k}$	D1			
	(I)		Ū	B1	co		
		Unit vecto	$\mathbf{br} = \frac{1}{6} (4\mathbf{i} + 2\mathbf{j} + 4\mathbf{k})$	M1 A1√	Divides by the mo	odulus. \vee on OB .	
	(ii)	$\overrightarrow{AC} = \overrightarrow{O}$	$\vec{C} - \vec{OA} = 2\mathbf{i} - 4\mathbf{j} - 2\mathbf{k}$	[3] B1	со		
	(II)		C = 0A - 2I - 4J - 2K = 8 - 8 - 8 = -8	M1	Use of $x_1 x_2 + y_1 y_1$	2 + 7, 7	
			0 0 0 0				
			$\left \overrightarrow{AC}\right = \sqrt{24}$	M1	Correct method fo		
			$\sqrt{24} \times \cos \theta$	M1	Connected correctl	y provided \overrightarrow{OB} , \overrightarrow{AC}	used
		$\theta = 105.8$	$^{\circ} \rightarrow 74.2^{\circ}$	A1	co (accept acute of	r obtuse)	
	(:::)	$04 - \sqrt{10}$	$\overline{9}$ or $OC = \sqrt{11}$	[5] B1	Used as a length.		
	(III)		$y = 2(\sqrt{+\sqrt{3}})$	M1			
		$\rightarrow 15.4$	-(' ')	Al	co (accept 15.3)		
				[3]			