

As part of CIE’s continual commitment to maintaining best practice in assessment, CIE has begun to use different variants of some question papers for our most popular assessments with extremely large and widespread candidature, The question papers are closely related and the relationships between them have been thoroughly established using our assessment expertise. All versions of the paper give assessment of equal standard.

The content assessed by the examination papers and the type of questions are unchanged.

This change means that for this component there are now two variant Question Papers, Mark Schemes and Principal Examiner’s Reports where previously there was only one. For any individual country, it is intended that only one variant is used. This document contains both variants which will give all Centres access to even more past examination material than is usually the case.

The diagram shows the relationship between the Question Papers, Mark Schemes and Principal Examiner’s Reports.

| <b>Question Paper</b>         | <b>Mark Scheme</b>         | <b>Principal Examiner’s Report</b>         |
|-------------------------------|----------------------------|--|
| Introduction                  | Introduction               | Introduction                               |
| First variant Question Paper  | First variant Mark Scheme  | First variant Principal Examiner’s Report  |
| Second variant Question Paper | Second variant Mark Scheme | Second variant Principal Examiner’s Report |

**Who can I contact for further information on these changes?**

Please direct any questions about this to CIE’s Customer Services team at: [international@cie.org.uk](mailto:international@cie.org.uk)

UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS  
GCE Advanced Subsidiary Level and GCE Advanced Level

**MARK SCHEME for the May/June 2009 question paper  
for the guidance of teachers**

**9709/71**

**9709 MATHEMATICS**

Paper 7, maximum raw mark 50

This mark scheme is published as an aid to teachers and candidates, to indicate the requirements of the examination. It shows the basis on which Examiners were instructed to award marks. It does not indicate the details of the discussions that took place at an Examiners' meeting before marking began, which would have considered the acceptability of alternative answers.

Mark schemes must be read in conjunction with the question papers and the report on the examination.

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### Mark Scheme Notes

Marks are of the following three types:

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**A** Accuracy mark, awarded for a correct answer or intermediate step correctly obtained. Accuracy marks cannot be given unless the associated method mark is earned (or implied).

**B** Mark for a correct result or statement independent of method marks.

- When a part of a question has two or more "method" steps, the M marks are generally independent unless the scheme specifically says otherwise; and similarly when there are several B marks allocated. The notation DM or DB (or dep\*) is used to indicate that a particular M or B mark is dependent on an earlier M or B (asterisked) mark in the scheme. When two or more steps are run together by the candidate, the earlier marks are implied and full credit is given.
- The symbol  $\surd$  implies that the A or B mark indicated is allowed for work correctly following on from previously incorrect results. Otherwise, A or B marks are given for correct work only. A and B marks are not given for fortuitously "correct" answers or results obtained from incorrect working.
- Note: B2 or A2 means that the candidate can earn 2 or 0.  
B2/1/0 means that the candidate can earn anything from 0 to 2.

The marks indicated in the scheme may not be subdivided. If there is genuine doubt whether a candidate has earned a mark, allow the candidate the benefit of the doubt. Unless otherwise indicated, marks once gained cannot subsequently be lost, e.g. wrong working following a correct form of answer is ignored.

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|               |                                       |                 |              |
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|     |   |
|-----|---|
| AEF | Any Equivalent Form (of answer is equally acceptable)   |
| AG  | Answer Given on the question paper (so extra checking is needed to ensure that the detailed working leading to the result is valid)   |
| BOD | Benefit of Doubt (allowed when the validity of a solution may not be absolutely clear)  |
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| CWO | Correct Working Only – often written by a 'fortuitous' answer   |
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| MR  | Misread   |
| PA  | Premature Approximation (resulting in basically correct work that is insufficiently accurate)   |
| SOS | See Other Solution (the candidate makes a better attempt at the same question)  |
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### **Penalties**

|       |   |
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| MR –1 | A penalty of MR –1 is deducted from A or B marks when the data of a question or part question are genuinely misread and the object and difficulty of the question remain unaltered. In this case all A and B marks then become "follow through $\sqrt{}$ " marks. MR is not applied when the candidate misreads his own figures – this is regarded as an error in accuracy. An MR–2 penalty may be applied in particular cases if agreed at the coordination meeting. |
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|   |   |  |
|---|---|--|
| <p><b>1</b> <math>H_0 : \mu = 18.5</math><br/> <math>H_1 : \mu &lt; 18.5</math><br/>                     Test statistic <math>z = \frac{18.1 - 18.5}{(1.1/\sqrt{20})}</math><br/> <math>= -1.626</math><br/>                     CV <math>z = \pm 1.96</math></p> <p>Not enough evidence to support the claim that fingers are smaller.</p> | <p>B1<br/><br/>M1<br/><br/>A1<br/>M1<br/><br/>A1ft</p> <p>[5]</p> | <p>Both hypotheses correct</p> <p>Standardising, must have <math>\sqrt{20}</math></p> <p>For correct <math>z</math><br/>                     Correct comparison with correct CV or finding area on LHS of <math>-1.626</math> and comparing with 2.5 % (OR comparison with 2.241 oe if one-tail test set up)</p> <p>Correct conclusion must fit their CV and their <math>z</math>. No contradictions</p> |
| <p><b>2 (i)</b> <math>\hat{\mu} = 227.(1)</math></p> $5 = 2.17 \times \sqrt{\frac{\hat{\sigma}^2}{50}}$ $\hat{\sigma}^2 = 265 \text{ or } 266$  | <p>B1<br/>B1<br/><br/>M1<br/><br/>A1</p> <p>[4]</p>               | <p>Correct mean<br/>                     2.17 seen</p> <p>Solving an equation with 5 or 10 on the LHS and some <math>z</math> value <math>\times \frac{\hat{\sigma}}{\sqrt{n}}</math> on the RHS</p> <p>Correct answer</p>   |
| <p><b>(ii)</b> <math>4 = 2.17 \times \frac{16.3}{\sqrt{n}}</math></p> $n = 78$  | <p>B1ft<br/><br/>M1<br/><br/>A1</p> <p>[3]</p>                    | <p>Correct equation fit their wrong <math>z</math> if the same as in part <b>(i)</b> and their <math>\sigma</math></p> <p>Solving an equation with their <math>z</math> and <math>\sigma</math>, and width 4 or 8</p> <p>Correct answer (whole number)</p>   |
| <p><b>3 (i)</b> <math>\lambda = 2</math><br/> <math>P(X &gt; 3) = 1 - P(0, 1, 2, 3)</math><br/> <math>= 1 - e^{-2} \left( 1 + 2 + \frac{2^2}{2} + \frac{2^3}{3!} \right)</math><br/> <math>= 1 - 0.857 = 0.143</math></p>   | <p>B1<br/><br/>M1<br/><br/>A1</p> <p>[3]</p>                      | <p>Correct mean (used)</p> <p>Poisson <math>1 - P(0,1,2,3)</math> or <math>P(0,1,2)</math> or <math>P(1,2,3)</math></p> <p>Correct answer</p>  |
| <p><b>(ii)</b> <math>\lambda = 16/3</math></p> $P(7) = e^{-16/3} \left( \frac{(16/3)^7}{7!} \right)$ $= 0.118$  | <p>B1<br/><br/>M1<br/><br/>A1</p> <p>[3]</p>                      | <p>Correct new mean</p> <p><math>P(7)</math> using a different mean from <b>(i)</b></p> <p>Correct final answer</p>  |
| <p><b>(iii)</b> <math>X \sim N(160, 160)</math></p> $P(X < 137) = P\left(z < \frac{136.5 - 160}{\sqrt{160}}\right)$ $= P(z < -1.858)$ $= 1 - 0.9684 = 0.0316$   | <p>B1<br/>M1<br/><br/>M1<br/><br/>A1</p> <p>[4]</p>               | <p>Correct mean and variance</p> <p>Standardising attempt with or without cc must have sq rt</p> <p>Cc of 136.5 or 137.5 and area <math>&lt; 0.5</math></p> <p>Correct answer</p>  |

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|  |  |  |
|--|--|--|
| <p><b>4 (i)</b> <math>H_0 : p = 0.36</math><br/> <math>H_1 : p &gt; 0.36</math></p> <p><math>P(7) = {}^8C_7 \times (0.36)^7 (0.64)^1 = 0.00401</math><br/> <math>P(8) = (0.36)^8 = 0.000282</math><br/> <math>\Sigma P = 0.00429 &lt; 0.05</math></p> <p>Accept driving instructor's claim</p> | <p>B1</p> <p>M1<br/>A1<br/>M1</p> <p>B1</p> <p>[5]</p> | <p>Both hypotheses correct</p> <p>Evaluating P(7) or P(8)<br/>                     Correct answer for both<br/>                     Comparing their prob sum to 0.05 oe</p> <p>Correct conclusion cwo no contradictions</p>  |
| <p><b>(ii)</b> Type I error<br/> <math>P(6) = {}^8C_6 \times (0.36)^6 (0.64)^2 = 0.02496</math><br/> <math>P(5) = {}^8C_5 \times (0.36)^5 (0.64)^3 = 0.08876,</math><br/> <math>&gt; 0.05</math></p> <p><math>P(\text{Type I error}) = 0.0292</math> or <math>0.0293</math></p>                | <p>B1<br/>M1<br/>B1</p> <p>A1</p> <p>[4]</p>           | <p>Correct answer<br/>                     Evaluating P(6)<br/>                     Correct P(5) and showing this is not in the CR either by <math>\Sigma P &gt; 0.05</math> or <math>P(5) &gt; 0.05</math></p> <p>Correct answer<br/>                     NB Marks for part <b>(ii)</b> may be awarded in part <b>(i)</b> but not vice versa.</p> |
| <p><b>5 (i)</b> <math>\int_3^6 k(6t - t^2) dt = 1</math><br/> <math>k[3t^2 - t^3/3]_3^6 = 1</math><br/> <math>k([108 - 216/3] - [27 - 9]) = 1</math></p> <p><math>k = 1/18</math> AG</p>   | <p>M1</p> <p>A1</p> <p>A1</p> <p>[3]</p>               | <p>For equating to 1 and a sensible attempt to integrate</p> <p>Correct integration and correct limits</p> <p>Given answer correctly obtained</p>  |
| <p><b>(ii)</b> mean = <math>\int_3^6 k(6t^2 - t^3) dt</math></p> <p><math>= \left[ k(2t^3 - \frac{t^4}{4}) \right]_3^6</math><br/> <math>= k(432 - 324) - k(54 - 81/4)</math><br/> <math>= \frac{33}{8}</math> (4.13)</p>  | <p>M1</p> <p>A1</p> <p>A1</p> <p>[3]</p>               | <p>Attempt to evaluate the integral of <math>tf(t)</math> (<math>t</math> or <math>x</math>)</p> <p>Correct integral and correct limits (condone loss of k)</p> <p>Correct answer</p>  |
| <p><b>(iii)</b> <math>\int_5^6 k(6t - t^2) dt</math></p> <p><math>= k \left[ 3t^2 - \frac{t^3}{3} \right]_5^6 = k \left( 36 - \frac{100}{3} \right)</math></p> <p><math>= \frac{4}{27}</math> (0.148)</p>  | <p>M1</p> <p>A1</p> <p>[2]</p>                         | <p>Attempt to evaluate the integral between 5 and 6 oe</p> <p>Correct answer</p>   |
| <p><b>(iv)</b> the area on the left is <math>&gt; 0.75</math><br/>                     or <b>(iii)</b> is <math>&lt; 0.25</math><br/>                     UQ is less than 5</p>  | <p>M1</p> <p>A1ft</p> <p>[2]</p>                       | <p>sensible reason</p> <p>ft their <b>(iii)</b><br/>                     SR B1ft correct but 0.25/0.75 implied</p>   |

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|   |                |   |
|---|----------------|---|
| <p><b>6 (i)</b> <math>T_1 + T_2 + T_4 - T_3 \sim N(-0.95, 4.345)</math></p> <p><math>P[(T_1 + T_2 + T_4 - T_3) &gt; 0]</math></p> <p><math>= P\left(z &gt; \frac{0 - (-0.95)}{\sqrt{4.345}}\right) = P(z &gt; 0.4557)</math></p> <p><math>= 1 - 0.6758</math></p> <p><math>= 0.324</math></p> | M1             | Attempt to find mean and var of $T_1 + T_2 + T_4 - T_3$<br>oe   |
|   | B1<br>A1<br>M1 | Correct mean ( $3.75 + 3.1 + 3.2 - 11$ )<br>Correct variance<br>Finding P their $[(T_1 + T_2 + T_4 - T_3) > 0]$ oe        |
|   | M1             | Standardising (appropriate variance involving all 4) and area $< 0.5$   |
|   | A1             | Correct answer  |
| <b>[6]</b>  |                |   |
| <p><b>(ii)</b> <math>\bar{X} \sim N(3.1, 0.785/6)</math></p> <p><math>P(\bar{X} &lt; 4) = P\left(z &lt; \frac{4 - 3.1}{\sqrt{0.785/6}}\right)</math></p> <p><math>= P(z &lt; 2.488)</math></p> <p><math>= 0.994</math></p>  | M1             | Normal distribution mean 3.1, var 0.785/6, can be implied   |
|   | M1             | OR $N(18.6, 4.71)$ if working with totals<br>Standardising with sq rt<br>OR $(24 - 18.6)/\sqrt{4.71}$<br>no mixed methods |
|   | A1             | Correct answer  |
| <b>[3]</b>  |                |   |

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**9709/72**

**9709 MATHEMATICS**

Paper 7, maximum raw mark 50

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|   |  |  |
|---|--|--|
| <p><b>1</b> <math>H_0 : \mu = 1.746</math><br/> <math>H_1 : \mu \neq 1.746</math></p> <p>Test statistic <math>z = \frac{1.765 - 1.746}{0.149 / \sqrt{230}}</math><br/> <math>\pm -1.93(4)</math></p> <p>CV <math>z = \pm 1.645</math></p> <p>Evidence of a difference</p> | <p>B1</p> <p>M1</p> <p>A1</p> <p>M1</p> <p>A1ft</p> <p>[5]</p> | <p>Both hypotheses correct</p> <p>Standardising, must have <math>\sqrt{230}</math></p> <p>For correct <math>z</math></p> <p>Correct comparison with correct CV or finding area on RHS of their <math>z</math> and comparing with 0.05 (must be 0.05)</p> <p>OR if one tail test comparison with 1.282 oe</p> <p>Correct conclusion must fit their CV and their <math>z</math>. No contradictions</p> |
| <p><b>2 (i)</b> <math>\hat{\mu} = 227.(1)</math></p> <p><math>5 = 2.17 \times \sqrt{\frac{\hat{\sigma}^2}{50}}</math></p> <p><math>\hat{\sigma}^2 = 265</math> or <math>266</math></p>  | <p>B1</p> <p>B1</p> <p>M1</p> <p>A1</p> <p>[4]</p>             | <p>Correct mean</p> <p>2.17 seen</p> <p>Solving an equation with 5 or 10 on the LHS and some <math>z</math> value <math>\times \frac{\hat{\sigma}}{\sqrt{n}}</math> on the RHS</p> <p>Correct answer</p>   |
| <p><b>(ii)</b> <math>4 = 2.17 \times \frac{16.3}{\sqrt{n}}</math></p> <p><math>n = 78</math></p>  | <p>B1ft</p> <p>M1</p> <p>A1</p> <p>[3]</p>                     | <p>Correct equation fit their wrong <math>z</math> if the same as in part <b>(i)</b> and their <math>\sigma</math></p> <p>Solving an equation with their <math>z</math> and <math>\sigma</math>, and width 4 or 8</p> <p>Correct answer (whole number)</p>   |
| <p><b>3 (i)</b> <math>\lambda = 4.5</math><br/> <math>P(\text{at most } 2) = P(0, 1, 2)</math><br/> <math>= e^{-4.5} \left( 1 + 4.5 + \frac{4.5^2}{2!} \right)</math><br/> <math>= 0.174</math></p>   | <p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>                       | <p>Correct mean (used)</p> <p>Poisson (0, 1, 2) or P(0, 1) or P(1, 2)</p> <p>Correct answer</p>  |
| <p><b>(ii)</b> <math>\lambda = 7.5</math><br/> <math>P(6) = e^{-7.5} \left( \frac{7.5^6}{6!} \right)</math><br/> <math>= 0.137</math></p>   | <p>B1</p> <p>M1</p> <p>A1</p> <p>[3]</p>                       | <p>New mean (1.5 + 6) used</p> <p>P(6) using a different mean from <b>(i)</b></p> <p>Correct answer</p>  |
| <p><b>(iii)</b> <math>X \sim N(90, 90)</math></p> <p><math>P(X &gt; 100) = P\left(z &gt; \frac{100.5 - 90}{\sqrt{90}}\right)</math><br/> <math>= P(z &gt; 1.107)</math><br/> <math>= 1 - 0.8657 = 0.134</math></p>  | <p>B1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[4]</p>             | <p>Correct mean and variance</p> <p>Standardising attempt with or without cc must have sq rt</p> <p>Cc of 100.5 or 99.5 and area &lt; 0.5</p> <p>Correct answer</p>  |

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|--|--|---|
| <p><b>4 (i)</b> <math>H_0 : p = 0.36</math><br/> <math>H_1 : p &gt; 0.36</math></p> <p><math>P(7) = {}^8C_7 \times (0.36)^7 (0.64)^1 = 0.00401</math><br/> <math>P(8) = (0.36)^8 = 0.000282</math><br/> <math>\Sigma P = 0.00429 &lt; 0.05</math></p> <p>Accept driving instructor's claim</p> | <p>B1</p> <p>M1<br/>A1<br/>M1</p> <p>A1</p> <p>[5]</p> | <p>Both hypotheses correct</p> <p>Evaluating P(7) or P(8)<br/>                     Correct answer for both P(7) and P(8)<br/>                     Comparing their prob sum to 0.05 oe</p> <p>Correct conclusion cwo. No contradictions</p>  |
| <p><b>(ii)</b> Type I error<br/> <math>P(6) = {}^8C_6 \times (0.36)^6 (0.64)^2 = 0.02496</math><br/> <math>P(5) = {}^8C_5 \times (0.36)^5 (0.64)^3 = 0.08876,</math><br/> <math>&gt; 0.05</math></p> <p><math>P(\text{Type I error}) = 0.0292</math> or <math>0.0293</math></p>                | <p>B1<br/>M1<br/>B1</p> <p>A1</p> <p>[4]</p>           | <p>Correct answer<br/>                     Evaluating P(6)<br/>                     Correct expression for P(5) and showing this is not in the CR either by <math>\Sigma P &gt; 0.05</math> or <math>P(5) &gt; 0.05</math><br/>                     Correct answer<br/>                     NB Marks for part (ii) may be awarded in part (i) but not vice versa.</p> |
| <p><b>5 (i)</b> <math>\int_0^2 kx^2(2-x)dx = 1</math></p> <p><math>\left[ \frac{2kx^3}{3} - \frac{kx^4}{4} \right]_0^2 = 1</math></p> <p><math>\frac{16k}{3} - \frac{16k}{4} = 1</math></p> <p><math>k = 3/4</math> AG</p>   | <p>M1</p> <p>A1</p> <p>A1</p> <p>[3]</p>               | <p>For equating to 1 and a sensible attempt to integrate</p> <p>Correct integration and correct limits</p> <p>Given answer correctly obtained</p>   |
| <p><b>(ii)</b> mean = <math>\int_0^2 2kx^3 - kx^4 dx</math></p> <p><math>= \left[ \frac{2kx^4}{4} - \frac{kx^5}{5} \right]_0^2</math></p> <p><math>= \frac{32k}{4} - \frac{32k}{5}</math></p> <p><math>= 1.2</math> m</p>  | <p>M1</p> <p>A1</p> <p>A1</p> <p>[3]</p>               | <p>Attempt to evaluate the integral of <math>xf(x)</math></p> <p>Correct integral and correct limits (condone loss of <math>k</math>)</p> <p>Correct answer</p>   |
| <p><b>(iii)</b> <math>\int_{1.3}^2 kx^2(2-x)dx</math></p> <p><math>= \left[ \frac{2kx^3}{3} - \frac{kx^4}{4} \right]_{1.3}^2</math></p> <p><math>= 1 - 0.563</math><br/> <math>= 0.437</math></p>  | <p>M1</p> <p>A1</p> <p>[2]</p>                         | <p>Attempt to evaluate the integral between 1.3 and 2 or equivalent</p> <p>Correct answer</p>   |
| <p><b>(iv)</b> the area on the right is <math>&lt; 0.5</math> oe median is less than 1.3 m</p>   | <p>M1<br/>A1ft</p> <p>[2]</p>                          | <p>Sensible reason<br/>                     ft their (iii)<br/>                     SR B1ft if correct but 0.5 implied</p>  |

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|---|--|---|
| <p><b>6 (i)</b> <math>T_1 + T_2 + T_4 - T_3 \sim N(-0.95, 4.345)</math></p> <p><math>P[(T_1 + T_2 + T_4 - T_3) &gt; 0]</math></p> <p><math>= P\left(z &gt; \frac{0 - (-0.95)}{\sqrt{4.345}}\right) = P(z &gt; 0.4557)</math></p> <p><math>= 1 - 0.6758</math></p> <p><math>= 0.324</math></p> | <p>M1</p> <p>B1</p> <p>A1</p> <p>M1</p> <p>M1</p> <p>A1</p> <p>[6]</p> | <p>Correct method to find mean and var of <math>T_1 + T_2 + T_4 - T_3</math> oe</p> <p>Correct mean <math>(3.75 + 3.1 + 3.2 - 11)</math></p> <p>Correct variance</p> <p>Finding P their <math>[(T_1 + T_2 + T_4 - T_3) &gt; 0]</math> oe</p> <p>Standardising (appropriate variance involving all 4) and area <math>&lt; 0.5</math></p> <p>Correct answer</p> |
| <p><b>(ii)</b> <math>\bar{X} \sim N(3.1, 0.785/6)</math></p> <p><math>P(\bar{X} &lt; 4) = P\left(z &lt; \frac{4 - 3.1}{\sqrt{0.785/6}}\right)</math></p> <p><math>= P(z &lt; 2.488)</math></p> <p><math>= 0.994</math></p>  | <p>M1</p> <p>M1</p> <p>A1</p> <p>[3]</p>                               | <p>Normal distribution mean 3.1, var 0.785/6, can be implied</p> <p>OR <math>N(18.6, 4.71)</math> if working with totals</p> <p>Standardising with sq rt</p> <p>OR <math>(24 - 18.6)/\sqrt{4.71}</math></p> <p>no mixed methods</p> <p>Correct answer</p>   |