UNIVERSITY OF CAMBRIDGE INTERNATIONAL EXAMINATIONS General Certificate of Education Advanced Subsidiary Level and Advanced Level

MATHEMATICS 9709/06

Paper 6 Probability & Statistics 1 (S1)

May/June 2006

1 hour 15 minutes

Additional Materials: Answer Booklet/Paper

Graph paper

List of Formulae (MF9)

READ THESE INSTRUCTIONS FIRST

If you have been given an Answer Booklet, follow the instructions on the front cover of the Booklet.

Write your Centre number, candidate number and name on all the work you hand in.

Write in dark blue or black pen on both sides of the paper.

You may use a soft pencil for any diagrams or graphs.

Do not use staples, paper clips, highlighters, glue or correction fluid.

Answer all the questions.

Give non-exact numerical answers correct to 3 significant figures, or 1 decimal place in the case of angles in degrees, unless a different level of accuracy is specified in the question.

The use of an electronic calculator is expected, where appropriate.

You are reminded of the need for clear presentation in your answers.

The number of marks is given in brackets [] at the end of each question or part question.

The total number of marks for this paper is 50.

Questions carrying smaller numbers of marks are printed earlier in the paper, and questions carrying larger numbers of marks later in the paper.

At the end of the examination, fasten all your work securely together.

This document consists of 4 printed pages.

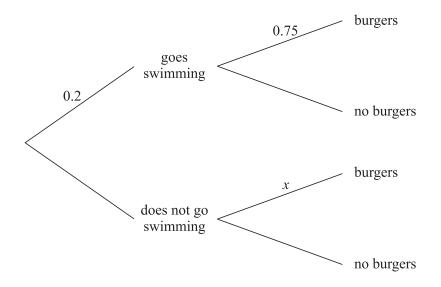


[Turn over

1 The salaries, in thousands of dollars, of 11 people, chosen at random in a certain office, were found to

Choose and calculate an appropriate measure of central tendency (mean, mode or median) to summarise these salaries. Explain briefly why the other measures are not suitable. [3]

2 The probability that Henk goes swimming on any day is 0.2. On a day when he goes swimming, the probability that Henk has burgers for supper is 0.75. On a day when he does not go swimming the probability that he has burgers for supper is x. This information is shown on the following tree diagram.

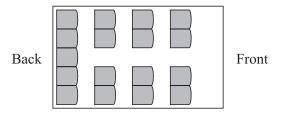


The probability that Henk has burgers for supper on any day is 0.5.

(i) Find
$$x$$
. [4]

- (ii) Given that Henk has burgers for supper, find the probability that he went swimming that day. [2]
- 3 The lengths of fish of a certain type have a normal distribution with mean 38 cm. It is found that 5% of the fish are longer than 50 cm.
 - (i) Find the standard deviation. [3]
 - (ii) When fish are chosen for sale, those shorter than 30 cm are rejected. Find the proportion of fish rejected.
 - (iii) 9 fish are chosen at random. Find the probability that at least one of them is longer than 50 cm.

4



The diagram shows the seating plan for passengers in a minibus, which has 17 seats arranged in 4 rows. The back row has 5 seats and the other 3 rows have 2 seats on each side. 11 passengers get on the minibus.

- (i) How many possible seating arrangements are there for the 11 passengers? [2]
- (ii) How many possible seating arrangements are there if 5 particular people sit in the back row? [3]

Of the 11 passengers, 5 are unmarried and the other 6 consist of 3 married couples.

- (iii) In how many ways can 5 of the 11 passengers on the bus be chosen if there must be 2 married couples and 1 other person, who may or may not be married? [3]
- 5 Each father in a random sample of fathers was asked how old he was when his first child was born. The following histogram represents the information.

Frequency density (fathers per year)

6

5

4

3

2

1

0

10

20

30

40

50

60

70

(years)

- (i) What is the modal age group?
- (ii) How many fathers were between 25 and 30 years old when their first child was born? [2]
- (iii) How many fathers were in the sample? [2]
- (iv) Find the probability that a father, chosen at random from the group, was between 25 and 30 years old when his first child was born, given that he was older than 25 years. [2]

[1]

- 6 32 teams enter for a knockout competition, in which each match results in one team winning and the other team losing. After each match the winning team goes on to the next round, and the losing team takes no further part in the competition. Thus 16 teams play in the second round, 8 teams play in the third round, and so on, until 2 teams play in the final round.
 - (i) How many teams play in only 1 match? [1]
 - (ii) How many teams play in exactly 2 matches? [1]
 - (iii) Draw up a frequency table for the numbers of matches which the teams play. [3]
 - (iv) Calculate the mean and variance of the numbers of matches which the teams play. [4]
- A survey of adults in a certain large town found that 76% of people wore a watch on their left wrist, 15% wore a watch on their right wrist and 9% did not wear a watch.
 - (i) A random sample of 14 adults was taken. Find the probability that more than 2 adults did not wear a watch. [4]
 - (ii) A random sample of 200 adults was taken. Using a suitable approximation, find the probability that more than 155 wore a watch on their left wrist. [5]

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