## AQA ${ }^{2}$

# GCSE <br> MATHEMATICS <br> (8300/3H) 

Paper 3 Higher

## Mark scheme

Specimen 2015

[^0]Principal Examiners have prepared these mark schemes for specimen papers. These mark schemes have not, therefore, been through the normal process of standardising that would take place for live papers.

Further copies of this Mark Scheme are available from aqa.org.uk

## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.
If a student uses a method which is not explicitly covered by the mark scheme the same principles of marking should be applied. Credit should be given to any valid methods. Examiners should seek advice from their senior examiner if in any doubt.

| M | Method marks are awarded for a correct method which could <br> lead to a correct answer. |
| :--- | :--- |
| A | Accuracy marks are awarded when following on from a correct <br> method. It is not necessary to always see the method. This can <br> be implied. |
| B | Marks awarded independent of method. |
| ft | Follow through marks. Marks awarded for correct working <br> following a mistake in an earlier step. |
| SC | Special case. Marks awarded within the scheme for a common <br> misinterpretation which has some mathematical worth. |
| M dep | Awarded. <br> A mark that can only be awarded if a previous independent mark <br> has been awarded. |
| ©e | Or equivalent. Accept answers that are equivalent. <br> eg accept 0.5 as well as $\frac{1}{2}$ |
| [a, b] | Accept values between $a$ and $b$ inclusive. |
| 3.14... | Allow answers which begin 3.14 eg $3.14,3.142,3.1416$ |

Examiners should consistently apply the following principles

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a student has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the student. In cases where there is no doubt that the answer has come from incorrect working then the student should be penalised.

## Questions which ask students to show working

Instructions on marking will be given but usually marks are not awarded to students who show no working.

## Questions which do not ask students to show working

As a general principle, a correct response is awarded full marks.

## Misread or miscopy

Students often copy values from a question incorrectly. If the examiner thinks that the student has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

## Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

## Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

## Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

## Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| $\mathbf{1}$ | $-7 \leqslant x<6$ | B1 |  |
| :---: | :--- | :---: | :--- |


| $\mathbf{2}$ | $\frac{4}{9}$ | B1 |  |
| :--- | :--- | :--- | :--- |


| 3 | $2.5 \mathrm{~cm} / \mathrm{s}$ | B1 |  |
| :--- | :--- | :--- | :--- |


| 4 | $x$ is $\frac{2}{3}$ of $y$ | B 1 |  |
| :---: | :--- | :--- | :--- |


| $\mathbf{5}$ | $3 a(3 a-2)$ | B2 | B1 $a(9 a-6)$ or $3\left(3 a^{2}-2 a\right)$ |
| :---: | :--- | :--- | :--- |


| 6 | $+8,+12,+16$ seen or implied <br> or $40+20$ | M1 |  |
| :--- | :--- | :---: | :--- |
|  | 60 | A1 |  |


| 7(a) | Valid reason <br> Any indication that actual outcomes <br> do not always match theoretical <br> probability | B1 | eg <br> It's just chance <br> Might get two of one number |
| :---: | :--- | :---: | :--- |
| 7(b) | $7+12+9$ <br> or $50-(4+5+13)$ <br> or 28 | M1 | oe |
|  | $\frac{28}{50}$ or $\frac{14}{25}$ or 0.56 | A1 |  |


| 8 | $3 \times 180$ | M1 | oe |
| :---: | :--- | :---: | :--- |
|  | 540 with correct method shown | A1 | SC1 540 without correct method <br> shown |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 9 | Alternative method 1 |  |  |
|  | $60 \times 0.5$ or 30 | M1 | oe |
|  | $\begin{aligned} & (100-60) \times 0.2 \\ & \text { or } 8 \end{aligned}$ | M1 | oe |
|  | 38 | A1 | SC2 0.38 |
|  | Alternative method 2 |  |  |
|  | Implies boys are 40\% and works out $50 \%$ of their girl total | M1 | eg 60 and 40 seen and $\frac{1}{2} \times 60=30$ or 120 and 80 seen and $\frac{1}{2} \times 120=60$ |
|  | Works out 20\% of their boy total | M1dep | $\text { eg } 0.2 \times 40 \text { or } 8$ <br> or $0.2 \times 80$ or 16 |
|  | 38 | A1 | oe |


| $\mathbf{1 0 ( a )}$ | $(2,16)$ | B1 |  |
| :--- | :--- | :---: | :--- |
| $\mathbf{1 0 ( b )}$ | 12 | B1 |  |
| $\mathbf{1 0 ( c )}$ | -2 and 6 | B1 |  |


| 11 | $9.83 \times 7$ or 68.81 | M1 |  |
| :---: | :--- | :---: | :--- |
|  | their $68.81-9.75-9.79-9.80-$ <br> $9.88-9.94-9.98$ <br> or 9.67 | M1dep | oe |
|  | 9.67 and Yes | A1 |  |


| 12 | $7 x-3=3 x+3$ | B1 |  |
| :--- | :--- | :---: | :--- |
|  | $7 x-3 x=3+3$ <br> or $4 x=6$ | M1 | oe isolating $x$ and number terms |
|  | $x=1.5$ | A1 |  |
|  | 7.5 or $7 \frac{1}{2}$ | B1ft | ft $7 \times$ their $1.5-3$ <br> or $3($ their $1.5+1)$ |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 13 | 2 | B1 |  |
| :--- | :--- | :--- | :--- |

14 Any two sets of
$a=5, b=3, c=13$
$a=7, b=11, c=5$
$a=5, b=2, c=17$

B2 for any one set
B1 $a=5, b=5, c=5$
or $b$ and $c$ prime and $a$ non-prime integer and $a=\sqrt{4 b+c}$

| 15 | $64 x^{6} y^{10}$ | B2 | B1 for two terms correct |
| :---: | :--- | :--- | :--- |


| 16 | $20-12$ or 8 seen | M1 |  |
| :---: | :--- | :---: | :--- |
|  | $\sqrt{17^{2}-8^{2}}$ or 15 | M1 | oe |
|  | $\frac{1}{2}(12+20) \times 15$ or 240 | M1dep | oe <br> Dependent on 2nd M1 |
|  | their $240 \div 90$ or $2.66 \ldots$ or $2 \frac{2}{3}$ | M1dep |  |
|  | $(3 \times 19.25=) 57.75$ | A1 |  |

17

| $6 x^{2}-16 x y+15 x y-40 y^{2}$ | M1 | Allow one error |
| :--- | :---: | :--- |
| $6 x^{2}-16 x y+15 x y-40 y^{2}$ | A1 | Fully correct |
| $6 x^{2}-x y-40 y^{2}$ | A1ft | ft their four terms |


| Q | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 18 | Alternative method 1 |  |  |
| :---: | :---: | :---: | :---: |
|  | $a: b$ or $\frac{a}{b}$ equivalent to $3: 4$ with $a$ and $b>10$ and $a-6: b$ or $\frac{a-6}{b}$ seen | M1 |  |
|  | $30: 48 \text { or } \frac{30}{48}$ | A1 |  |
|  | 48 | A1 |  |
|  | Alternative method 2 |  |  |
|  | $3 x-6$ and $4 x$ | M1 |  |
|  | $\frac{3 x-6}{4 x}=\frac{5}{8}$ or $x=12$ | M1 | oe |
|  | 48 | A1 |  |
| 19(a) | Median at 37 | B1 |  |
|  | Quartiles at 24 and 56 | B1 |  |
|  | Ends at 0 and 107 and correct boxplot presentation | B1 |  |
| 19(b) | Correct comment about average | B1 | eg the median age of the population will go up by 7 years, so average age will rise |
|  | Correct comment about spread | B1 | eg the inter-quartile range will have increased by 8 years, so ages are more spread out |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 20(a) | Tom is using simple interest instead <br> of compound interest | B1 | oe <br> He has assumed the interest is the <br> same each year |
| :---: | :--- | :---: | :--- |
| $\mathbf{2 0 ( b )}$ | Use of 1.025 | B1 |  |
|  | $\frac{11696.67}{1.025^{8}}$ | M1 |  |
|  | 9600 | A1 |  |


| $\mathbf{2 1 ( a )}$ | 511 | B1 |  |
| :---: | :--- | :---: | :--- |
|  | $7 \times 73$ <br> or 7 is a factor <br> or 73 is a factor | B1 |  |
| $\mathbf{2 1 ( b ) ~}$ | Incorrect and $2^{5}-1: 2^{7}-1 \neq 5: 7$ <br> or $31: 127$ shown | B1 |  |


| 22 | $\frac{y}{\sin 35}=\frac{15}{\sin 70}$ | M1 | oe |
| :---: | :--- | :---: | :--- |
|  | $[9.15,9.16]$ or 9.2 | A1 | Accept 9 with working |


| 23 | $a=2$ | B1 |  |
| :---: | :--- | :---: | :--- |
|  | $x^{2}-b x-b x+b^{2}$ <br> or $x^{2}-2 b x+b^{2}$ <br> or $-2 a b=-20$ <br> or $-a b=-10$ <br> or $b=5$ | M1 | oe |
|  | $2(x-5)^{2}+15$ | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 24 | False - angle in semicircle $=90^{\circ}$ <br> (not 92) | B1 |  |
| :---: | :--- | :---: | :---: |
|  | True - opposite angles in cyclic quad <br> total $180^{\circ}$ | B1 |  |
|  | True - alternate angles $A C D$ and <br> $C A B=50^{\circ}$ <br> or $92+88=180$ (allied) | B1 | $50^{\circ}$ angles may be on diagram - need <br> not say angle sum of a triangle $=180^{\circ}$ |
|  | False - angle $C A D=42^{\circ}$, should be <br> $32^{\circ}$ if $D E$ is a tangent by alternate <br> segment | B1 |  |


| 25 | Any one of $155,165,7.15,7.25$ | B1 |  |
| :---: | :---: | :---: | :---: |
|  | $\frac{155}{7.25} \text { or } \frac{165}{7.15}$ | M1 |  |
|  | $\begin{aligned} & 21.3 \ldots \text { or } 21.4 \\ & \text { or } 23.0 \ldots \text { or } 23.1 \end{aligned}$ | A1 |  |
|  | Upper bound is 23.1 <br> Lower bound is 21.4 | A1 |  |
| 26(a) | $(x-5)^{2}+1$ | M1 |  |
|  | $\begin{aligned} & x^{2}-5 x-5 x+25+1 \\ & =x^{2}-10 x+26 \end{aligned}$ | A1 |  |
| 26(b) | $x^{2}+1-5$ or $x^{2}-4$ | B1 |  |
|  | $x^{2}-10 x+26=$ their $\left(x^{2}-4\right)$ | M1 |  |
|  | $\begin{aligned} & -10 x=-4-26 \\ & \text { or }-10 x=-30 \\ & \text { or } 10 x=30 \end{aligned}$ | M1 | oe |
|  | 3 | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 27 | $\frac{1}{3} \times 14 \times 8 \times h=336$ | M1 | oe |
| :---: | :---: | :---: | :---: |
|  | $h=\frac{336 \times 3}{14 \times 8}$ or $h=9$ | M1 | oe |
|  | $\begin{aligned} & B X^{2}=7^{2}+4^{2} \\ & \text { or } B D^{2}=14^{2}+8^{2} \\ & \text { or } B X=\sqrt{65} \text { or } B D=2 \sqrt{65} \\ & \text { or } V B=\sqrt{146} \end{aligned}$ | M1 | oe |
|  | Identifies V $\hat{B} X$ | M1 | oe |
|  | $\tan V \hat{B} X=\frac{\text { their } 9}{\text { their } \sqrt{65}}$ | M1 | $\begin{aligned} & \cos V \hat{B} X=\frac{\text { their } \sqrt{65}}{\text { their } \sqrt{146}} \\ & \text { or } \sin V \hat{B} X=\frac{\text { their } 9}{\text { their } \sqrt{146}} \end{aligned}$ |
|  | 48 or 48.1... | A1 |  |


[^0]:    Version 2.0

