General Certificate of Secondary Education November 2012

## Mathematics <br> 43602H

Unit 2 Higher tier

## Final

Mark Scheme

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation events which all examiners participate in and is the scheme which was used by them in this examination. The standardisation process ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for standardisation each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed and legislated for. If, after the standardisation process, examiners encounter unusual answers which have not been raised they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A

B

Q
ft

SC

Mdep A method mark dependent on a previous method mark being awarded.

B dep A mark that can only be awarded if a previous independent mark has been awarded.
oe Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$
$[a, b] \quad$ Accept values between $a$ and $b$ inclusive.
3.14... Allow answers which begin 3.14 eg 3.14, 3.142, 3.149.

Use of brackets
It is not necessary to see the bracketed work to award the marks.

Examiners should consistently apply the following principles

## Diagrams

Diagrams that have working on them should be treated like normal responses. If a diagram has been written on but the correct response is within the answer space, the work within the answer space should be marked. Working on diagrams that contradicts work within the answer space is not to be considered as choice but as working, and is not, therefore, penalised.

## Responses which appear to come from incorrect methods

Whenever there is doubt as to whether a candidate has used an incorrect method to obtain an answer, as a general principle, the benefit of doubt must be given to the candidate. In cases where there is no doubt that the answer has come from incorrect working then the candidate should be penalised.

## Questions which ask candidates to show working

Instructions on marking will be given but usually marks are not awarded to candidates who show no working.

## Questions which do not ask candidates to show working

As a general principle, a correct response is awarded full marks.

## Misread or miscopy

Candidates often copy values from a question incorrectly. If the examiner thinks that the candidate has made a genuine misread, then only the accuracy marks (A or B marks), up to a maximum of 2 marks are penalised. The method marks can still be awarded.

## Further work

Once the correct answer has been seen, further working may be ignored unless it goes on to contradict the correct answer.

## Choice

When a choice of answers and/or methods is given, mark each attempt. If both methods are valid then M marks can be awarded but any incorrect answer or method would result in marks being lost.

## Work not replaced

Erased or crossed out work that is still legible should be marked.

## Work replaced

Erased or crossed out work that has been replaced is not awarded marks.

## Premature approximation

Rounding off too early can lead to inaccuracy in the final answer. This should be penalised by 1 mark unless instructed otherwise.

## Unit 2 Higher Tier

| Q | Answer | Mark | Comments |
| :--- | :--- | :---: | :---: |
|  |  |  |  |
| 1a | $8 y+24$ or $24+8 y$ | B1 |  |
| 1 b | $x(4-x)$ | B1 |  |


| 2 | $x+x+50=600$ | M1 | oe (letting $x$ represent Sat) |
| :---: | :---: | :---: | :---: |
|  | $2 x=600-50$ | M1dep |  |
|  | 275 | A1 |  |
|  | Alternative method 1 |  |  |
|  | $x+x-50=600$ | M1 | oe (letting $x$ represent Sun) |
|  | $2 x=600+50(x=325)$ | M1dep |  |
|  | 275 | A1 |  |
|  | Alternative method 2 |  |  |
|  | $x+y=600$ and $y=x \pm 50$ | M1 | oe |
|  | $\begin{aligned} & 2 x=600-50 \quad \text { or } \\ & 2 x=600+50 \quad(x=325) \end{aligned}$ | M1dep |  |
|  | 275 | A1 |  |
|  | Alternative method 3 |  |  |
|  | 600-50 (=550) | M1 |  |
|  | Their $550 \div 2$ | M1dep |  |
|  | 275 | A1 |  |
|  | Alternative method 4 |  |  |
|  | $600+50$ (=650) | M1 |  |
|  | Their $650 \div 2(=325)$ | M1dep | M2 325 seen |
|  | 275 | A1 |  |
|  | Alternative method 5 |  |  |
|  | $600 \div 2(=300)$ and $50 \div 2(=25)$ | M1 | oe |
|  | Their 300 - their 25 | M1dep |  |
|  | 275 | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 3 | $\frac{30}{100} \times 250$ or 75 | M1 | oe eg $3 \times 25$ |
|  | (£) 175 | A1 | Electric Supplies |
|  | $240 \div 3$ or 80 | M1 | Allow 0.33 or better as a multiplier |
|  | (£) 160 | A1 | New Homes |
|  | (£) 170 | B1 | Fridges for Us |
|  | New Homes | Q1 ft | Strand (iii) <br> Must have both method marks and three values to compare <br> ft for a correct decision based on their answers |
| 4 | Any 3 of $\begin{array}{ll} 33=3 \times 11 & 34=2 \times 17 \\ 35=5 \times 7 & 38=2 \times 19 \end{array}$ | B3 | B2 for 2 correct <br> B1 for 1 correct <br> SC1 two or more correct but outside range 30 to 40 |
| 5 | Line drawn across grid through $(0,8)$ and (5, -2) | B3 | B2 part of correct line drawn <br> B2 plotting at least 3 correct points (ignore incorrect points) <br> B1 plotting 2 correct points (ignore incorrect points) <br> B1 line of gradient - 2 <br> B1 line through $(0,8)$ or $(4,0)$ <br> SC1 line $y=-\frac{1}{2} x+4$ from $(0,4)$ to $(5,1.5)$ |


| Q | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 6 a | A correct value for the sequence for <br> $n>1$ <br> $(2,4.5,8,12.5,18,24.5,32,40.5,50)$ <br> or $n^{2}>100$ <br> or a value of $n>1$ substituted into <br> $\frac{n^{2}}{2}$ and an attempt to evaluate | M1 |  |
| :---: | :--- | :--- | :--- |
|  | $n=11$ or 60.5 | A1 | oe <br> SC1 $\frac{11^{2}}{2}(11$ embedded with no attempt to <br> evaluate $)$ |
| 6 Bb | $3 n+4$ or $4+3 n$ | B2 $3 n+k$ or $k+3 n \quad k$ any value |  |


| 7 | $280 \div 7 \times 4$ or $280 \div 7 \times 3$ | M1 | oe <br> If a diagram is used: rectangle split into 7 sections with 3 or 4 shaded (or indicated in some way), at least one of which has a 40 in it |
| :---: | :---: | :---: | :---: |
|  | 160 (W) or 120 (M) | A1 |  |
|  | $180 \div 5 \times 3$ or $180 \div 5 \times 2$ | M1 | oe eg $180-(180 \div 5 \times 3)$ <br> If a diagram is used: rectangle split into 5 sections with 3 or 2 shaded (or indicated in some way), at least one of which has a 36 in it. |
|  | 108 (B) or 72 (G) | A1 |  |
|  | 232 (F) and 228 (M) or 232 is more than 230 (half of 460) or 228 is less than 230 (half of 460) | A1 ft | oe allow ft if either M awarded <br> Must add men and boys and/or women and girls otherwise AOft. |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 8 | $3 x$ or $5 x-9$ | M1 | $\frac{3 x+9}{5}$ |
|  | $5 x-9=3 x$ | M1 | oe $\frac{3 x+9}{5}=x$ |
|  | $5 x-3 x=9$ or $2 x=9$ | M1dep | oe dep on M2 |
|  | 4.5 | A1 | oe |
|  | Alternative method |  |  |
|  | 4.5 | B4 | oe <br> B3 correct trial using 4.5 but 4.5 not explicitly given as answer <br> B2 correct trials using 4 and 5 (11 and 16) B1 any correct trial |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 9 | $\frac{17}{8}\left(-\frac{2}{3}\right)$ | M1 | $\text { Or } 1 \frac{9}{8}\left(-\frac{2}{3}\right)$ |
|  | Common denominator with at least one numerator correct | M1 | ft their fractions <br> $\frac{51}{24}(-) \frac{16}{24} \quad$ if correct <br> Or grid method with correct bottom right cell and at least one other cell correct |
|  | $\frac{35}{24}$ or $1 \frac{11}{24}$ | A1 | oe |
|  | Alternative method 1 |  |  |
|  | Common denominator with at least one numerator correct | M1 | eg $2 \frac{3}{24}-\frac{16}{24}$ if fully correct <br> Or grid method with correct bottom right cel and at least one other cell correct |
|  | $1 \frac{27}{24}-\frac{16}{24}$ | M1 | ft their $2 \frac{3}{24}$ |
|  | $\frac{35}{24}$ or $1 \frac{11}{24}$ | A1 |  |
|  | Alternative method 2 |  |  |
|  | Common denominator with at least one numerator correct | M1 | eg $2 \frac{3}{24}-\frac{16}{24}$ if fully correct <br> Or grid method with correct bottom right cel and at least one other cell correct |
|  | 2- $\frac{13}{24}$ | M1 | Award for subtraction of numerators (one may be wrong) |
|  | $\frac{35}{24}$ or $1 \frac{11}{24}$ | A1 |  |
|  | Alternative method 3 |  |  |
|  | $1 \frac{1}{3}+\frac{1}{8}$ | M1 |  |
|  | Common denominator with at least one numerator correct | M1 | eg $\frac{32}{24}+\frac{3}{24}$ if fully correct |
|  | $\frac{35}{24}$ or $1 \frac{11}{24}$ | A1 |  |


| Q Answer | Mark | Comments |  |
| :---: | :--- | :---: | :--- |
| 10 a | $2 a^{5} b^{7}$ | B2 | B1 2 terms correct <br> B1 3 correct terms but the '2' not at front <br> B1 3 correct terms but one or more $\times$ signs <br> remaining in expression or brackets in <br> expression |
| 10 b | $\frac{c^{2}}{2}$ | B2 | oe <br> B1 2 terms correct ie 2 of $\frac{1}{2}, c^{2}$ or 1 <br> eg $2 c^{2}$ |



| $\mathbf{Q}$ | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 12a | $1(.0) \times 10^{-6}$ | B1 |  |
| :---: | :---: | :---: | :---: |
| 12b | 50000000000000 | B1 |  |
| 12c | $4^{3}=2^{6}$ | M1 | $2^{10}=4^{5}$ |
|  | their $2^{6} \times 2 \times 2 \times 2 \times 2$ | M1 | $4^{5} \div 4 \div 4$ <br> For this mark the correct number of 2 s or 4 s needed for their $2^{6}$ or their $4^{5}$ |
|  | 5 | A1 | SC1 answer only |
|  | Alternative method 1 |  |  |
|  | 64 and 128 | M1 | Allow one arithmetical slip when multiplying by 2 . |
|  | 64, 128, 256, 512 and 1024 | M1dep |  |
|  | 5 | A1 | If one arithmetical slip then A0 SC1 answer only |
|  | Alternative method 2 |  |  |
|  | 64 and 1024 | M1 |  |
|  | $1024 \div 64=16$ | M1 | oe |
|  | 5 | A1 | SC1 answer only |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 13a | $2 x^{2}+x-4 x-2$ | M1 | 4 terms, allow one error but must have a term in $x^{2}$ |
|  | $2 x^{2}+x-4 x-2$ | A1 |  |
|  | $2 x^{2}-3 x-2$ | A1 ft | oe ft their 4 terms if M1 awarded SC1 answer of $\begin{aligned} & 2 x^{2}-5 x-2 \text { or } 2 x^{2}+3 x-2 \text { or } \\ & 2 x^{2}-3 x+2 \end{aligned}$ <br> without working worth at least M1 |
| 13b | $3\left(x^{2}-16 y^{2}\right)$ | M1 |  |
|  | (3) $(x+a y)(x+b y)$ | M1 | where $a b=-16$ |
|  | $3(x-4 y)(x+4 y)$ | A1 | oe |
|  | Alternative method |  |  |
|  | $(3 x+a y)(x+b y)$ | M1 | where $a b=-48$ |
|  | $(3 x+12 y)(x-4 y)$ <br> or $(3 x-12 y)(x+4 y)$ | M1 |  |
|  | $3(x-4 y)(x+4 y)$ | A1 | oe |

14

| $w-x=y(2 x-3)$ | M1 | oe multiplying through by $y$ |
| :--- | :--- | :--- |
| $w-x=2 x y-3 y$ | M1 | oe multiplying out bracket <br> (this line gets M2 even if $1^{\text {st }}$ line not seen) |
| $w+3 y=2 x y+x$ | M1 | oe collecting terms |
| $x=\frac{w+3 y}{2 y+1}$ | A1 | oe |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 15a | $\sqrt{25 \times 3}$ or $\sqrt{25} \sqrt{3}$ | M1 | oe |
|  | $(a=) 5$ | A1 | Accept $5 \sqrt{3}$ |
|  | Alternative method |  |  |
|  | $\frac{\sqrt{75}}{\sqrt{3}}=\sqrt{\frac{75}{3}}(=\sqrt{25})$ | M1 |  |
|  | $(a=) 5$ | A1 | Accept $5 \sqrt{3}$ |
| 15b | $\begin{aligned} & \frac{1}{27^{\frac{2}{3}}} \text { or } \frac{1}{\sqrt[3]{27^{2}}} \text { or } 3^{-2} \\ & \text { or } \sqrt[3]{27}=3 \end{aligned}$ | M1 | Do not allow any marks for 9 or $\frac{1}{9}$ from inappropriate working eg $27 \div 3=9$ |
|  | $\frac{1}{3^{2}} \text { or } 9^{-1}$ <br> or $3^{2}=9$ | M1dep |  |
|  | $\frac{1}{9}$ | A1 |  |


| Q | Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |
| 16a | use of $(x-4)^{2}$ | M1 |  |
|  | $(x-4)^{2}-16(+20)$ | A1 |  |
|  | $(x-4)^{2}-16+20=(x-4)^{2}+4$ | Q1 | Strand (ii) <br> Complete and correct algebraic explanation |
|  | Alternative method 1 |  |  |
|  | use of $(x-4)^{2}$ | M1 |  |
|  | $=x^{2}-8 x+16$ | A1 |  |
|  | $(x-4)^{2}+4=x^{2}-8 x+20$ | Q1 | Strand (ii) <br> Complete and correct algebraic explanation |
|  | Alternative method 2 |  |  |
|  | $x^{2}-a x-a x+a^{2}(+a)$ | M1 |  |
|  | $a=4$ | A1 |  |
|  | Also $4^{2}+4=20$ | Q1 | Strand (ii) <br> Complete and correct algebraic explanation |
| 16b | explains that a square is always positive (or zero) | B1 | oe |
|  | and a positive number is added so is always positive | B1 | oe |

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