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Applications of Mathematics (Pilot) 93702H

(Specification 9370)

Unit 2: Applications of Mathematics Written Paper (Higher)



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Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

- M Method marks are awarded for a correct method which could lead to a correct answer.
- A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.
- **B** Marks awarded independent of method.
- **Q** Marks awarded for quality of written communication. (QWC)
- **M Dep** A method mark dependent on a previous method mark being awarded.
- **B Dep** A mark that can only be awarded if a previous independent mark has been awarded.
- ft Follow through marks. Marks awarded following a mistake in an earlier step.
- **SC** Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
- **oe** Or equivalent. Accept answers that are equivalent.

eg, accept 0.5 as well as $\frac{1}{2}$

A2 Higher Tier

Q	Answer	Mark	Comments
1	4 or 8	B1	oe eg, 9 – 1 is acceptable for 8 One missing length found correctly May be seen on diagram
	7 + 7 + their 4 + 2 + 3 + their 8	M1	oe Allow one error or one omission
	31	A1	SC2 Answer 27 or 32

2(a)	70	B1	Condone £0.70 B0 £70 or £0.7 or 0.70 or 0.7
2(b)	Straight line from (0, 4.8) to (5, 9.8) or Plots all 6 correct points (± 2 mm) (0, 4.8) (1, 5.8) (2, 6.8) (3, 7.8) (4, 8.8) and (5, 9.8)	B2	 B1 Any line of gradient 1 (or any 6 points that would make a line of gradient 1 if joined) B1 Plots at least 3 correct points (± 2 mm)
2(c)	Valid example eg 1, 4 (toppings cost the) same eg 2, 5 (toppings costs) more	B1 ft	oe ft From their points or line in (b)

-			
3(a)	Draws direction of A correctly $(\pm 2^{\circ})$	B1	
	Draws direction of <i>B</i> correctly ($\pm 2^{\circ}$)	B1	
	 States that they will not collide with valid reason. eg 1, No collision as <i>B</i> will pass through the place where their paths meet before <i>A</i> gets there eg 2, <i>A</i> takes longer to get to the crossing point than <i>B</i> so no they will not collide 	B1 ft	oe ft If two directions drawn
3(b)	Arc, centre <i>A</i> , radius 10 cm (±2mm)	B1	
	Arc, centre <i>B</i> , radius 6 cm (± 2 mm)	B1	
	Point <i>L</i> clearly indicated	B1 ft	Award B0 B0 B1 if no arcs drawn but <i>L</i> indicated in correct position (±2mm) ft Two intersecting arcs from centres <i>A</i> and <i>B</i>

Q	Answer	Mark	Comments
4(a)	125 ÷ (21 + 14) (= 3.57)	M1	125 ÷ (3 + 2) (= 25)
	Their 3.57 × 21 (= 75) or	M1	125 ÷ their (3 + 2) × their 3 or
	their 3.57 × 14 (= 50)		125 \div their (3 + 2) x their 2
	(small) 75 (large) 50	A1	(small) 50 (large) 75 M1 M1 A0
Alt 4(a)	$\frac{21}{35}$ (= 0.6) or $\frac{14}{35}$ (= 0.4)	M1	At least two equivalent ratios for 21 : 14 seen eg, 3 : 2 30 : 20
	Their 0.6 × 125 (= 75) or their 0.4 × 125 (= 50)	M1	Equivalent ratios seen including 75 : 50 eg, 30 : 20 60 : 40 75 :50
	(small) 75 (large) 50	A1	(small) 50 (large) 75 M1 M1 A0
4(b)	$200 \times 21 \times 0.05 (= 210)$ or $200 \times 14 \times 0.09 (= 252)$	M1	oe Allow working in pence
	200 × 0.87 (= 174)	M1	oe Allow working in pence
	Their 210 + their 252 + their 174 (= 636)	M1	Must be the sum of 2 or 3 amounts of money oe Allow working in pence
	Their 636 + 0.85 × their 636 (= their 636 + 540.6(0))	M1	oe eg, 1.85 × their 636 Allow working in pence
	1176.60	A1	1176.6 is A0 Allow 1176 or 1177 or 1180
Alt 4(b)	21 × 0.05 (= 1.05) or	M1	oe Allow working in pence
	14 × 0.09 (= 1.26)		
	Their 1.05 + their 1.26 + 0.87 (= 3.18)	M1	Must be the sum of 2 or 3 amounts of money oe Allow working in pence
	200 × their 3.18 (= 636)	M1	oe Allow working in pence
	Their 636 + 0.85 × their 636 (= their 636 + 540.6(0))	M1	oe eg, 1.85 × their 636 Allow working in pence
	1176.60	A1	1176.6 is A0 Allow 1176 or 1177 or 1180

Q	Answer	Mark	Comments
5	Two correct trials [4.65, 4.75] which bracket 172 and 4.7 as final answer	B4	B3 As B4 response but 4.7 not the final answer or
			B3 Two correct trials [4.65, 4.8] which bracket 172
			B2 Two correct trials $4 \le L < 5$
			B1 One correct trial $4 \le L < 5$

6	Correctly converts one dimension to metres	B1	eg, 0.8 seen
	$0.8 \times 0.3 (\times 2) + 0.3 \times 0.2 \times 2 + 0.8 \times 0.2 \times 2 $ (= 0.68)	M2	0.24 (x 2) + 0.12 + 0.32 M1 0.8 x 0.3 (x 2) or 0.3 x 0.2 (x 2) or 0.8 x 0.2 (x 2) M2 or M1 May be scored even if incorrect conversion factor has been used
	4.5 ÷ their 0.68 (= 6.6)	M1	
	6	A1	
Alt 6	$80 \times 30 (\times 2) + 30 \times 20 \times 2 + 80 \times 20 \times 2 (= 6800)$	M2	2400 (x 2) + 1200 + 3200 M1 80 x 30 (x 2) or 30 x 20 (x 2) or 80 x 20 (x 2)
	Their 6800 correctly converted to square metres (= 0.68)	B1	4.5 square metres correctly converted to square centimetres ie, 45000
	4.5 ÷ their 0.68 (= 6.6)	M1	45000 ÷ their 6800 (= 6.6)
	6	A1	

Q	Answer	Mark	Comments
7(a)(i)	x + 4x = 180 or $5x = 180$	M1	oe Equation
	(<i>x</i> =) 180 ÷ 5	M1	ft If their equation uses <i>x</i> and their obtuse angle
	36	A1 ft	ft If one method mark gained
	Sets up a linear equation and solves their equation correctly	Q1	36 obtained without an algebraic equation seen is M1 M1 A1 Q0
			SC1 Angle 4 <i>x</i> seen in a correct position on the diagram
7(a)(ii)	4 × their 36 (= 144) or	M1	May be seen on diagram
	180 – their 36 (= 144)		$\frac{1}{2}y = $ their 36
	360 – 2 × their 144	M1	$2 \times$ their 36 (if this is first step award M2)
	72	A1 ft	ft Their 36 in part (a)
7(b)	$\pi \times 15 \times 15$ (= 225 π)	M1	oe [706.5, 707]
	$\frac{250}{360}$ × their $225\pi \left(=\frac{625\pi}{4}\right)$ or	M1	[490.6, 491]
	360 (4)		[215.8, 216.03]
	$\frac{360-250}{360}$ × their $225\pi \left(=\frac{275\pi}{4}\right)$		Their 225 π can be from any $\pi \times r \times r$ or from 2 × π × 15 (= 30 π) or 2 × π × 30
			(= 60π)
	Their $\frac{625\pi}{4} \times 3$	M1	
	$\frac{1875\pi}{4}$ or [1471.8, 1473]	A1	
	Uses $\frac{\Theta}{360} \times \pi r^2$ and	Q1	Must be πr^2 not $2\pi r$
	$V = A \times h$ in their solution		

8	sin 76	B1	cos 14
	sin 76 = $\frac{d}{5.5}$ or 5.5 × sin 76	M1	$\cos 14 = \frac{d}{5.5}$ or $5.5 \times \cos 14$
	5.3	A1	

Q	Answer	Mark	Comments
9(a)	24 ÷ 20 (= 1.2)	M1	30 ÷ 24 (= 1.25) or 20 ÷ 24 (= 0.83)
	30 ÷ their 1.2	M1	20 × their 1.25 or 30 × their 0.83
	25	A1	
Alt 1	20 ÷ 4 (= 5)	M1	
9(a)	5 × their 5	M1	oe eg, 20 + their 5
	25	A1	
Alt 2 9(a)	$24 \times \frac{60}{20}$ (= 72)	M1	oe
	$\frac{30}{\text{their 72}} \times 60$	M1	oe
	25	A1	
9(b)	Sight of 1.6() or 4.5()	B1	oe eg, 8 km = 5 miles or 0.6(2) or 0.2(2)
	48 × their 1.6 ÷ their 4.5 (= 17.())	M1	oe eg, 48 ÷ their 4.5 × their 1.6 (= 17.())
	Car A and their 17.()	A1 ft	Only ft if B0 M1 ft From any conversion factors
Alt 1 9(b)	Sight of 1.6() or 4.5)	B1	oe eg, 8 km = 5 miles or 0.6(2) or 0.2(2)
	15 ÷ their 1.6 × their 4.5 (= 42.())	M1	oe eg, 15 × their 4.5 ÷ their 1.6 (= 42.())
	Car A and their 42.()	A1 ft	Only ft if B0 M1 ft From any conversion factors
Alt 2 9(b)	Sight of 1.6() or 4.5()	B1	oe eg, 8 km = 5 miles or 0.6(2) or or 0.2(2)
	48 × their 1.6 (= 76(.8) or 77) and 15 × their 4.5 (= 67(.5) or 68)	M1	48 ÷ their 4.5 (= 10(.6) or 10.7 or 11) and 15 ÷ their 1.6 (= 9(.3) or 9.4)
	Car A and their 76(.8) or 77 and their 67(.5) or 68	A1 ft	Car A and their 10(.6) or 10.7 or 11 and their 9(.3) or 9.4 Only ft if B0 M1 ft From any conversion factors

Q	Answer	Mark	Comments
10	40 ÷ 25 (= 1.6)	M1	25 ÷ 40 (= 0.625)
	15 × their 1.6	M1 Dep	15 ÷ their 0.625
	24	A1	
	4.5	B1 ft	oe
			ft $\frac{\text{their } 24-15}{2}$
Alt 10	25 ÷ 15 (= 1.66 or 1.7)	M1	15 ÷ 25 (= 0.6)
	40 ÷ their 1.66	M1 Dep	40 × their 0.6
	24	A1	
	4.5	B1 ft	ое
			ft $\frac{\text{their } 24-15}{2}$
11		N44	
11	$\frac{2}{3} \times \pi \times 3^3 \qquad (= 18\pi)$	M1	[56.5, 56.6]
			Allow $\frac{4}{3} \times \pi \times 3^3$
			(= 36π = [113, 113.112])
	π (x 1 ²) x 2 (= 2 π)	M1	[6.28, 6.3]
	Their 18π — their 2π	M1	Must subtract two volumes
	16π or [50.2, 50.3]	A1	SC2 136π or [427, 427.312]

Q	Answer	Mark	Comments
12	$10 \times 4 (+) \frac{1}{2} \times 2 \times 4$	M1	oe eg, $\frac{1}{2} \times (10 + 12) \times 4$
	44	A1	
	$4 \times 5 (+) \frac{1}{2} \times 8 \times 5$	M1	oe eg, $\frac{1}{2} \times (12 + 4) \times 5$
	40	A1	
	Gives a valid reason eg 1, Amy won as she travelled a greater distance eg 2, (Amy) 44 ÷ 12 = 3.7 (Sue) 40 ÷ 12 = 3.3 Amy won as she travelled at a faster (average) speed	B1 ft	 oe Must include reference to distances unless average speeds are calculated and reference to speeds made ft Their two areas SC2 Amy 48 and Sue 60 and valid reason (eg Sue travelled further) SC2 Any two correct partial areas calculated (one for each person) and valid reason given on ft (eg, 10 × 4 = 40 and 4 × 5 = 20 and Amy travelled further) SC1 At least one correct partial area calculation (eg 4 × 5)

13(a)	1.5 to 1.6 inclusive	B1	Allow fractions eg, $1\frac{1}{2}$
13(b)	3.3 to 3.4 inclusive	B1	Allow fractions eg, $3\frac{3}{10}$
13(c)	2.5 (–) 0.5	M1	Two points indicated on graph where $h = 3$ eg, horizontal line drawn at $y = 3$
	2	A1	
13(d)(i)	Tangent drawn at $t = 1$	B1	
	Attempt at $\frac{y_2 - y_1}{x_2 - x_1}$ from any tangent drawn	M1	Allow M1 if tangent drawn at incorrect t value
	[0.8, 1.6]	A1	No tangent drawn B0 M0 A0
13(d)(ii)	Speed or velocity	B1	Rate of change of height B0 Average speed

Q	Answer	Mark	Comments
14(a)	tan used	B1	
	$\tan x = \frac{40}{400}$	M1	oe eg, tan $x = 0.1$
	5.7	A1	Allow 6 with correct working
14(b)	$700^2 + 400^2$ (= 650000)	M1	
	$\sqrt{\text{their 650 000}}$	M1 dep	
	806 (.2)	A1	
	$\tan(y) = \frac{40}{\text{their } 806(.2)}$	M1	Their 5.7 ÷ 2 (= 2.85 or 2.86) and evaluates tan their 2.85
			and evaluates $\frac{40}{\text{their 806}(.2)}$
	2.8	A1	Obtains 0.049 or 0.05 for both evaluations
Alt 14(b)	$40^2 + 400^2$ (= 161 600) and their 161 600 + 700 ² (= 651 600)	M1	
	$\sqrt{\text{their } 651600}$	M1 dep	
	807(.2)	A1	
	$sin(y) = \frac{40}{their 807(.2)}$	M1	Their 5.7 ÷ 2 (= 2.85 or 2.86)
			and evaluates sin their 2.85
			and evaluates $\frac{40}{\text{their 807(.2)}}$
	2.8	A1	Obtains 0.049 or 0.05 for both evaluations