

General Certificate of Secondary Education June 2011

Applications of Mathematics (Pilot)
(Specification 9370)
Unit 2: Applications of Mathematics Written Paper (Higher)

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## Glossary for Mark Schemes

GCSE examinations are marked in such a way as to award positive achievement wherever possible. Thus, for GCSE Mathematics papers, marks are awarded under various categories.

M Method marks are awarded for a correct method which could lead to a correct answer.

A Accuracy marks are awarded when following on from a correct method. It is not necessary to always see the method. This can be implied.

B Marks awarded independent of method.
Q Marks awarded for quality of written communication. (QWC)
M Dep A method mark dependent on a previous method mark being awarded.

BDep A mark that can only be awarded if a previous independent mark has been awarded.
ft Follow through marks. Marks awarded following a mistake in an earlier step.

SC Special case. Marks awarded within the scheme for a common misinterpretation which has some mathematical worth.
oe $\quad$ Or equivalent. Accept answers that are equivalent. eg, accept 0.5 as well as $\frac{1}{2}$

## A2 Higher Tier

| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 1 | 4 or 8 | B1 | oe eg, $9-1$ is acceptable for 8 <br> One missing length found correctly <br> May be seen on diagram |
| :---: | :--- | :---: | :--- |
|  | $7+7+$ their $4+2+3+$ their 8 | M1 | oe <br> Allow one error or one omission |
|  | 31 | A1 | SC2 Answer 27 or 32 |


| 2(a) | 70 | B1 | Condone $£ 0.70$ <br> B0 $£ 70$ or $£ 0.7$ or 0.70 or 0.7 |
| :---: | :--- | :---: | :--- |
| 2(b) | Straight line from $(0,4.8)$ to $(5,9.8)$ <br> or <br> Plots all 6 correct points $( \pm 2 \mathrm{~mm})$ <br> $(0,4.8)(1,5.8)(2,6.8)(3,7.8)$ <br> $(4,8.8)$ and (5, 9.8) | B2 | B1 Any line of gradient 1 (or any 6 points <br> that would make a line of gradient 1 <br> if joined) |
| B1 Plots at least 3 correct points $( \pm 2 \mathrm{~mm})$ |  |  |  |


| 3(a) | Draws direction of $A$ correctly ( $\pm 2^{\circ}$ ) | B1 |  |
| :---: | :---: | :---: | :---: |
|  | Draws direction of $B$ correctly ( $\pm 2^{\circ}$ ) | B1 |  |
|  | States that they will not collide with valid reason. <br> eg 1, No collision as $B$ will pass through the place where their paths meet before $A$ gets there <br> eg 2, $A$ takes longer to get to the crossing point than $B$ so no they will not collide | B1 ft | oe <br> ft If two directions drawn |
| 3(b) | Arc, centre $A$, radius $10 \mathrm{~cm}( \pm 2 \mathrm{~mm})$ | B1 |  |
|  | Arc, centre $B$, radius $6 \mathrm{~cm}( \pm 2 \mathrm{~mm})$ | B1 |  |
|  | Point $L$ clearly indicated | B1 ft | Award B0 B0 B1 if no arcs drawn but $L$ indicated in correct position ( $\pm 2 \mathrm{~mm}$ ) <br> ft Two intersecting arcs from centres $A$ and $B$ |


| Q | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 4(a) | $125 \div(21+14)(=3.57 \ldots)$ | M1 | $125 \div(3+2)(=25)$ |
| :---: | :---: | :---: | :---: |
|  | Their $3.57 \ldots \times 21(=75)$ or their $3.57 \ldots \times 14(=50)$ | M1 | $125 \div$ their $(3+2) \times$ their 3 or <br> $125 \div$ their $(3+2) \times$ their 2 |
|  | (small) 75 (large) 50 | A1 | (small) 50 (large) 75 M1 M1 A0 |
| Alt 4(a) | $\frac{21}{35}(=0.6) \text { or } \frac{14}{35}(=0.4)$ | M1 | At least two equivalent ratios for 21 : 14 seen <br> eg, 3:2 $30: 20$ |
|  | Their $0.6 \times 125(=75)$ or their $0.4 \times 125(=50)$ | M1 | Equivalent ratios seen including 75:50 eg, $30: 20 \quad 60: 40 \quad 75: 50$ |
|  | (small) 75 (large) 50 | A1 | (small) 50 (large) 75 M1 M1 A0 |
| 4(b) | $\begin{aligned} & 200 \times 21 \times 0.05(=210) \text { or } \\ & 200 \times 14 \times 0.09(=252) \end{aligned}$ | M1 | oe Allow working in pence |
|  | $200 \times 0.87(=174)$ | M1 | oe Allow working in pence |
|  | Their 210 + their $252+$ their 174 (=636) | M1 | Must be the sum of 2 or 3 amounts of money <br> oe Allow working in pence |
|  | Their $636+0.85 \times$ their 636 (= their $636+540.6(0)$ ) | M1 | oe eg, $1.85 \times$ their 636 <br> Allow working in pence |
|  | 1176.60 | A1 | 1176.6 is A0 <br> Allow 1176 or 1177 or 1180 |
| Alt 4(b) | $\begin{aligned} & 21 \times 0.05(=1.05) \text { or } \\ & 14 \times 0.09(=1.26) \end{aligned}$ | M1 | oe Allow working in pence |
|  | Their $1.05+$ their $1.26+0.87$ (= $=3.18$ ) | M1 | Must be the sum of 2 or 3 amounts of money <br> oe Allow working in pence |
|  | $200 \times$ their 3.18 (= 636) | M1 | oe Allow working in pence |
|  | Their $636+0.85 \times$ their 636 (= their $636+540.6(0)$ ) | M1 | oe eg, $1.85 \times$ their 636 Allow working in pence |
|  | 1176.60 | A1 | 1176.6 is A0 <br> Allow 1176 or 1177 or 1180 |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 5 | Two correct trials [4.65, 4.75] which <br> bracket 172 and 4.7 as final answer | B4 | B3 As B4 response but 4.7 not the final <br> answer or <br> B3Two correct trials [4.65, 4.8] which <br> bracket 172 <br> B2 Two correct trials $4 \leq L<5$ <br> B1 One correct trial $4 \leq L<5$ |
| :---: | :---: | :---: | :---: |


| 6 | Correctly converts one dimension to metres | B1 | eg, 0.8 seen |
| :---: | :---: | :---: | :---: |
|  | $\begin{aligned} & 0.8 \times 0.3(\times 2)+0.3 \times 0.2 \times 2 \\ & +0.8 \times 0.2 \times 2 \quad(=0.68) \end{aligned}$ | M2 | $\begin{gathered} 0.24(\times 2)+0.12+0.32 \\ \text { M1 } 0.8 \times 0.3(\times 2) \text { or } \\ 0.3 \times 0.2(\times 2) \text { or } \\ 0.8 \times 0.2(\times 2) \end{gathered}$ <br> M2 or M1 May be scored even if incorrect conversion factor has been used |
|  | $4.5 \div$ their 0.68 ( $=6.6 \ldots$ ) | M1 |  |
|  | 6 | A1 |  |
| Alt 6 | $\begin{aligned} & 80 \times 30(\times 2)+30 \times 20 \times 2 \\ & +80 \times 20 \times 2 \quad(=6800) \end{aligned}$ | M2 | $\begin{aligned} & 2400(\times 2)+1200+3200 \\ & \text { M1 } 80 \times 30(\times 2) \text { or } \\ & 30 \times 20(\times 2) \text { or } 80 \times 20(\times 2) \end{aligned}$ |
|  | Their 6800 correctly converted to square metres (= 0.68 ) | B1 | 4.5 square metres correctly converted to square centimetres ie, 45000 |
|  | 4.5 - their 0.68 ( $=6.6 \ldots$ ) | M1 | $45000 \div$ their 6800 ( $=6.6 \ldots$ ) |
|  | 6 | A1 |  |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 7(a)(i) | $x+4 x=180$ or $5 x=180$ | M1 | oe Equation |
| :---: | :---: | :---: | :---: |
|  | $(x=) 180 \div 5$ | M1 | ft If their equation uses $x$ and their obtuse angle |
|  | 36 | A1 ft | ft If one method mark gained |
|  | Sets up a linear equation and solves their equation correctly | Q1 | 36 obtained without an algebraic equation seen is M1 M1 A1 Q0 <br> SC1 Angle $4 x$ seen in a correct position on the diagram |
| 7(a)(ii) | $\begin{aligned} & 4 \times \text { their } 36(=144) \text { or } \\ & 180 \text { - their } 36(=144) \end{aligned}$ | M1 | May be seen on diagram $\frac{1}{2} y=\text { their } 36$ |
|  | $360-2 \times$ their 144 | M1 | $2 \times$ their 36 (if this is first step award M2) |
|  | 72 | A1 ft | ft Their 36 in part (a) |
| 7(b) | $\pi \times 15 \times 15 \quad(=225 \pi)$ | M1 | oe [706.5, 707] |
|  | $\frac{250}{360} \times$ their $225 \pi\left(=\frac{625 \pi}{4}\right)$ or $\frac{360-250}{360} \times \text { their } 225 \pi\left(=\frac{275 \pi}{4}\right)$ | M1 | $\begin{aligned} & {[490.6,491]} \\ & {[215.8,216.03]} \end{aligned}$ <br> Their $225 \pi$ can be from any $\pi \times r \times r$ or from $2 \times \pi \times 15(=30 \pi)$ or $2 \times \pi \times 30$ $(=60 \pi)$ |
|  | Their $\frac{625 \pi}{4} \times 3$ | M1 |  |
|  | $\frac{1875 \pi}{4}$ or [1471.8, 1473] | A1 |  |
|  | Uses $\frac{\Theta}{360} \times \pi r^{2}$ and $V=A \times h$ in their solution | Q1 | Must be $\pi r^{2}$ not $2 \pi r$ |


| 8 | $\sin 76$ | B 1 | $\cos 14$ |
| :---: | :--- | :---: | :--- |
|  | $\sin 76=\frac{d}{5.5}$ or $5.5 \times \sin 76$ | M 1 | $\cos 14=\frac{d}{5.5}$ or $5.5 \times \cos 14$ |
|  | $5.3 \ldots$ | A 1 |  |


| Q | Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 9(a) | $24 \div 20 \quad(=1.2)$ | M1 | $30 \div 24(=1.25)$ or $20 \div 24(=0.83 \ldots)$ |
| :---: | :---: | :---: | :---: |
|  | $30 \div$ their 1.2 | M1 | $20 \times$ their 1.25 or $30 \times$ their $0.83 \ldots$ |
|  | 25 | A1 |  |
| Alt 1 <br> 9(a) | $20 \div 4 \quad(=5)$ | M1 |  |
|  | $5 \times$ their 5 | M1 | oe eg, $20+$ their 5 |
|  | 25 | A1 |  |
| Alt 2 <br> 9(a) | $24 \times \frac{60}{20} \quad(=72)$ | M1 | oe |
|  | $\frac{30}{\text { their } 72} \times 60$ | M1 | oe |
|  | 25 | A1 |  |
| 9(b) | Sight of 1.6(....) or 4.5(...) | B1 | oe eg, $8 \mathrm{~km}=5$ miles or $0.6(2 \ldots$ ) or 0.2(2...) |
|  | $48 \times$ their $1.6 \div$ their $4.5 \quad(=17 .(\ldots))$ | M1 | oe eg, $48 \div$ their $4.5 \times$ their $1.6(=17 .(\ldots)$. |
|  | Car A and their 17.(...) | A1 ft | Only ft if B0 M1 <br> ft From any conversion factors |
| Alt 1 <br> 9(b) | Sight of 1.6(...) or 4.5 ...) | B1 | oe eg, $8 \mathrm{~km}=5$ miles or $0.6(2 \ldots$. or 0.2(2...) |
|  | $15 \div$ their $1.6 \times$ their 4.5 (= 42.(...)) | M1 | oe eg, $15 \times$ their $4.5 \div$ their $1.6(=42 .(\ldots)$. |
|  | Car A and their 42.(....) | A1 ft | Only ft if B0 M1 <br> ft From any conversion factors |
| Alt 2 <br> 9(b) | Sight of $1.6(\ldots .$.$) or 4.5(\ldots$. | B1 | oe eg, $8 \mathrm{~km}=5$ miles or $0.6(2 \ldots$ ) or or 0.2(2...) |
|  | $48 \times$ their $1.6(=76(.8)$ or 77$)$ and $15 \times$ their $4.5(=67(.5)$ or 68$)$ | M1 | $\begin{aligned} & 48 \div \text { their } 4.5(=10(.6 \ldots) \text { or } 10.7 \text { or } 11) \\ & \text { and } \\ & 15 \div \text { their } 1.6(=9(.3 \ldots) \text { or } 9.4) \end{aligned}$ |
|  | Car A and their 76(.8) or 77 and their 67(.5) or 68 | A1 ft | Car A and their $10(.6 \ldots)$ or 10.7 or 11 and their $9(.3 \ldots)$ or 9.4 <br> Only ft if B0 M1 <br> ft From any conversion factors |


| Q Answer | Mark | Comments |
| :---: | :---: | :---: | :---: |


| 10 | $40 \div 25$ (= 1.6) | M1 | $25 \div 40 \quad(=0.625)$ |
| :---: | :---: | :---: | :---: |
|  | $15 \times$ their 1.6 | M1 Dep | $15 \div$ their 0.625 |
|  | 24 | A1 |  |
|  | 4.5 | B1 ft | oe <br> $\frac{\text { their } 24-15}{2}$ |
| Alt 10 | $25 \div 15$ (= 1.66 $\ldots$ or 1.7$)$ | M1 | $15 \div 25 \quad(=0.6)$ |
|  | $40 \div$ their $1.66 \ldots$ | M1 Dep | $40 \times$ their 0.6 |
|  | 24 | A1 |  |
|  | 4.5 | B1 ft | oe $\frac{\text { their } 24-15}{2}$ |


| 11 | $\frac{2}{3} \times \pi \times 3^{3} \quad(=18 \pi)$ M1 | $[56.5,56.6]$ <br> Allow $\frac{4}{3} \times \pi \times 3^{3}$ <br> $(=36 \pi=[113,113.112])$ |  |
| :---: | :--- | :---: | :--- |
|  | $\pi\left(\times 1^{2}\right) \times 2 \quad(=2 \pi)$ | M1 | $[6.28,6.3]$ |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 12 | $10 \times 4(+) \frac{1}{2} \times 2 \times 4$ | M1 | oe eg, $\frac{1}{2} \times(10+12) \times 4$ |
| :---: | :---: | :---: | :---: |
|  | 44 | A1 |  |
|  | $4 \times 5(+) \frac{1}{2} \times 8 \times 5$ | M1 | oe eg, $\frac{1}{2} \times(12+4) \times 5$ |
|  | 40 | A1 |  |
|  | Gives a valid reason <br> eg 1, Amy won as she travelled a greater distance <br> eg 2, (Amy) $44 \div 12=3.7$ <br> (Sue) $40 \div 12=3.3$ <br> Amy won as she travelled at a faster (average) speed | B1 ft | oe Must include reference to distances unless average speeds are calculated and reference to speeds made <br> ft Their two areas <br> SC2 Amy 48 and Sue 60 and valid reason (eg Sue travelled further) <br> SC2 Any two correct partial areas calculated (one for each person) and valid reason given on ft <br> (eg, $10 \times 4=40$ and $4 \times 5=20$ and Amy travelled further) <br> SC1 At least one correct partial area calculation (eg $4 \times 5$ ) |


| 13(a) | 1.5 to 1.6 inclusive | B1 | Allow fractions eg, $1 \frac{1}{2}$ |
| :---: | :---: | :---: | :---: |
| 13(b) | 3.3 to 3.4 inclusive | B1 | Allow fractions eg, $3 \frac{3}{10}$ |
| 13(c) | 2.5 (-) 0.5 | M1 | Two points indicated on graph where $h=3$ eg, horizontal line drawn at $y=3$ |
|  | 2 | A1 |  |
| 13(d)(i) | Tangent drawn at $t=1$ | B1 |  |
|  | Attempt at $\frac{y_{2}-y_{1}}{x_{2}-x_{1}}$ from any tangent drawn | M1 | Allow M1 if tangent drawn at incorrect $t$ value |
|  | [0.8, 1.6] | A1 | No tangent drawn B0 M0 A0 |
| 13(d)(ii) | Speed or velocity | B1 | Rate of change of height <br> B0 Average speed |


| Q Answer | Mark | Comments |
| :--- | :---: | :---: | :---: |


| 14(a) | tan used | B1 |  |
| :---: | :---: | :---: | :---: |
|  | $\tan x=\frac{40}{400}$ | M1 | oe eg, $\tan x=0.1$ |
|  | 5.7.... | A1 | Allow 6 with correct working |
| 14(b) | $700^{2}+400^{2} \quad(=650000)$ | M1 |  |
|  | $\sqrt{\text { their } 650000}$ | M1 dep |  |
|  | 806 (.2....) | A1 |  |
|  | $\tan (y)=\frac{40}{\text { their } 806(.2 \ldots . .)}$ | M1 | Their $5.7 \ldots \div 2 \quad(=2.85 \ldots$ or 2.86$)$ and evaluates tan their $2.85 \ldots$. and evaluates $\frac{40}{\text { their } 806(.2 \ldots .)}$ |
|  | 2.8.... | A1 | Obtains $0.049 \ldots$ or 0.05 for both evaluations |
| Alt 14(b) | $\begin{aligned} & 40^{2}+400^{2} \quad(=161600) \text { and } \\ & \text { their } 161600+700^{2} \quad(=651600) \end{aligned}$ | M1 |  |
|  | $\sqrt{\text { their } 651600}$ | M1 dep |  |
|  | 807(.2....) | A1 |  |
|  | $\sin (y)=\frac{40}{\text { their } 807(.2 \ldots .)}$ | M1 | Their $5.7 \ldots \div 2 \quad(=2.85 \ldots$ or 2.86$)$ and evaluates sin their $2.85 \ldots$. and evaluates $\frac{40}{\text { their 807(.2...) }}$ |
|  | 2.8.... | A1 | Obtains $0.049 \ldots$ or 0.05 for both evaluations |

