

General Certificate of Education

Statistics 6380

SS05 Statistics 5

Mark Scheme

2009 examination – June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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Key to mark scheme and abbreviations used in marking

M	mark is for method					
m or dM	mark is dependent on one or more M marks and is for method					
A	mark is dependent on M or m marks and is for accuracy					
В	mark is independent of M or m marks and is for method and accuracy					
E	mark is for explanation					
√or ft or F	follow through from previous					
	incorrect result	MC	mis-copy			
CAO	correct answer only MR mis-read					
CSO	correct solution only RA required accuracy					
AWFW	anything which falls within FW further work					
AWRT	anything which rounds to ISW ignore subsequent work					
ACF	any correct form FIW from incorrect work					
AG	answer given	BOD	given benefit of doubt			
SC	special case WR work replaced by candidate					
OE	or equivalent FB formulae book					
A2,1	2 or 1 (or 0) accuracy marks NOS not on scheme					
–x EE	deduct x marks for each error G graph					
NMS	no method shown c candidate					
PI	possibly implied sf significant figure(s)					
SCA	substantially correct approach dp decimal place(s)					

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

SS05

Q	Solution	Marks	Total	Comments
1(a)	mean $1/0.05 = 20$ s.d. $1/0.05 = 20$	M1		Method for both
		A1	2	20 both, CAO
(b)	$\begin{vmatrix} 1 - e^{-0.05 \times 20} \\ = 1 - e^{-1} \end{vmatrix}$	B1		0.05×20
	$= 1 - e^{-1}$	M1		Method - allow wrong tail
	= 0.632	A1	3	0.6315 ~ 0.6325
	$e^{-0.05 \times 10}$	M1		Attempt to find > or < 10 from exponential parameter 0.05 or equivalent
	$= e^{-0.5}$	m1		Method - allow wrong tail
	= 0.607	A1	3	0.606 ~ 0.607
	Total		8	

Q	Solution	Marks	Total	Comments
2(a)	Range $15g > 10 \times 1.4$	E1		Comparison of range and s.d.
	or $6 \times 1.4 = 8.4 < 15$ Range is too large if $\sigma = 1.4$	E1	2	Full explanation
	Range is too large if $0 - 1.4$	EI	2	run explanation
(b)	s = 4.8033	B1		4.8033 (4.80 ~ 4.81) or 23.07 (23 ~ 23.1) or 161.5 (161 ~ 162)
	$2.167 < 7 \times 4.8033^2 / \sigma^2 < 14.067$	M1		Any correct expression; allow small slip, incorrect χ^2
		m1		Correct expression, allow incorrect χ^2
		B1 B1		7 df
		ы		14.067 (14 ~14.1) and 2.167 (2.16 ~ 2.17)
	$161.5/14.067 < \sigma^2 < 161.5/2.167$	m1		Correct method for interval for σ , or σ^2 provided it is clearly called σ^2 or variance
	$11.481 < \sigma^2 < 74.527$			
	$3.39 < \sigma < 8.63$	A1	7	3.39 (3.385 ~3.395) and 8.63 (8.63 ~8.64)
	or using F $4.8033^2/\sigma^2 < 2.010$ and $\sigma^2/4.8033^2 < 3.230$			
(c)	Statement supported since 1.4 is below lower bound of confidence interval	B1√ E1	2	Statement supported - their c.i. Explanation
(d)	$\overline{x} = 218.75$ 95% confidence interval			
	$218.75 \pm 2.365 \times 4.8033 / \sqrt{8}$	M1		Use of their s.d. $/\sqrt{8}$
	210.75 = 2.505	M1		Attempt at c.i. using t
		m1		Method - allow incorrect <i>t</i> -value
		B1		2.365 (2.36 ~ 2.37)
	218.75 ± 4.02			
	214.7 ~ 222.8	A1	5	214.7 (214.7 ~ 214.8) and 222.8 (222.7 ~ 222.8); allow 215 and 223
(e)	Confidence interval indicates that mean is above 212. Hence mean could be reduced	E1		Statement incorrect
	and the mean could still be greater than 212. However, the fact that one member	E1		Mean could be reduced and still be greater than 212
	of the sample only contains 212g indicates that if the mean were reduced some individual jars would contain less than 212g.	E1	3	If mean were reduced some individual jars would contain less than 212g
	Total		19	

Q			Marks	Total	Comments	
3(a)						
	Size	Frequency				
	1	2		M1		Method for frequency distribution
	2	5				
	3	10		A1	2	Frequencies CAO
	4	12				
	5	11				
(b)						
	Size	O	Е	7.1		
	1	2	6	B1		Correct values for E
	2	5	8			
	3	10	12			
	4	12	8			
	5	11	6			
	H ₀ : Probability distribution is adequate					
	model			B1		Hypotheses - may be earned in conclusion
	H ₁ : Probability distribution is not			Di		Trypotheses - may be carried in conclusion
	adequate model					
	- (a) 2					
	$\Sigma(O-E)^2/E$	22/0 + 22/12 +	1210 + 5216	M1		Attempt at $\Sigma(O - E)^2/E$ - their Es and Os
	$\Sigma(O - E)^{2}/E$ = $4^{2}/6 + 3^{2}/8 + 2^{2}/12 + 4^{2}/8 + 5^{2}/6$					
	= 10.3			A 1		10.25 10.25
	- 10.3			A1		10.25 ~ 10.35
	c.v. χ_4^2 is 9.488			B1		4 df
	C.V. χ ₄ 18 9.466			B1√		9.488 - their df
				DIV		7.400 - then th
	Significant evide	ence that the pr	obability	A 1√	7	Conclusion - needs correct method for Es
	distribution does			1111	,	and Os and comparison with upper tail of
	distribution of re					χ^2
		1				~
(c)	Modify order - n	nore large heln	nets, less	E1√		Modify order
	small helmets th					
	probability distribution		E1	2	More large, less small	
					11	

O COIL	Colution	Marks	Total	Comments
Q	Solution	Marks	1 Otal	Comments
4(a)	0.2/6 = 0.0333	M1		Method
		A1	2	$0.0333 (0.033 \sim 0.034) \text{ or } 1/30$
(b)	mean 3	B1		CAO
(6)	mean 5	Di		6/10
	s.d. $6/\sqrt{12} = 1.73$	N/1		Compost mostles d
	s.d. $6/\sqrt{12} - 1.73$	M1	_	Correct method
		A1	3	1.73 (1.73 \sim 1.735) or $\sqrt{3}$
				SC allow B1 instead of M1A1 for
				variance = 3
(c)	(2.1. 2) //1.722 / \(\sqrt{46} \) = 0.202			
(C)	$z_1 = (3.1 - 3)/(1.732/\sqrt{46}) = 0.392$	M1		Use of their s.d./ $\sqrt{46}$
	$z_1 = (3.1-3)/(1.732/\sqrt{46}) = 0.392$ $z_2 = (2.9-3)/(1.732/\sqrt{46}) = -0.392$	IVI 1		Use of their s.d./ $\sqrt{40}$
	22 (2.3 3)/(1.732/ (10) 0.332	1		1 1 1
		m1		z-values - their mean and s.d.
		ml		method for z-values - requires correct
				method for mean and s.d.
	Probability between 2.9 and 3.1			
	= 0.6525 - (1 - 0.6525)	m1		Method
	-0.0323 - (1 - 0.0323)			
	0.205	A 1	~	
	= 0.305	A1	5	0.3 ~ 0.31
			10	

Q	Solution	Marks	Total	Comments
5(a)(i)	H_0 : $\sigma_s = 0.65$ H_1 : $\sigma_s \neq 0.65$	B1		Both hypotheses
	$s_s = 0.710466 (\overline{x}_s = 15.2143)$			Made d Contact statistics allows
	$\sum (x - \overline{x})^2 / \sigma^2 = 6 \times 0.710466^2 / 0.65^2$	M1 m1		Method for test statistic - allow small slip, eg 7 × 0.710466 ² Correct method for test statistic
	= 7.17	A1		$7.165 \sim 7.175$
	c.v. χ_6^2 are 1.237 and 14.449	B1 B1		6 df 1.237 and 14.449 - allow 1.24 and 14.4
	Accept H ₀ : $\sigma_s = 0.65$, ie accept standard deviation of breaking strength of standard line is 0.65 kg	A1√		Conclusion - must be compared with least one χ^2 value
	Using F, compare 1.19 (1.19 \sim 1.2) with 2.408 (or reciprocals)			
(ii)	H_0 : $\sigma_p = 0.95$ H_1 : $\sigma_p \neq 0.95$	B1		Both hypotheses
	$s_p = 1.30945$ $(\overline{x}_p = 19.7333)$			
	$\sum (x - \overline{x})^2 / \sigma^2 = 5 \times 1.30945^2 / 0.95^2$			
	= 9.50	A1		9.49 ~ 9.505
	c.v. χ_5^2 are 0.831 and 12.833	B1		Allow 0.83 and 12.8
	Accept H ₀ : $\sigma_p = 0.95$, ie accept standard deviation of breaking strength of premium line is 0.95kg	A1	11	Conclusion in context. Needs both c.v. – must mention standard deviation / variance and fishing line or breaking strength
	Using F, compare 1.90 (1.895 \sim 1.905) with 6.02 (or reciprocals)			Use mark scheme for (i) in (ii) and for (ii) in (i) if more favourable to candidate

SS05 (cont) Q	Solution	Marks	Total	Comments
5(cont)	H_0 : $\mu_p = \mu_s + 5$	B1		Hypotheses
(b)	$H_1: \mu_p < \mu_s + 5$	ы		Hypotheses
	$z = \frac{19.7333 - 15.2143 - 5}{\sqrt{(0.95^2/6 + 0.65^2/7)}}$	M1 M1		Method for variance Method for z - their variance
	=-1.05	A1		$-1.04 \sim -1.06$ - ignore sign
	c.v1.2816	B1		$-1.28 \sim -1.282$ - ignore sign
	Accept H ₀ , ie accept mean breaking	A1√		Accept H_0 - must be compared with correct tail of z – needs both M marks
	strength of premium line is at least 5kg greater than that of standard line	A1√	7	Conclusion in context – needs previous $A1$
	p-value 0.148 (0.146 ~ 0.149) compare with 0.1			If t used, maximum B1M0M1A0B1(for 1.363)A0A0
(c)	$H_0: \sigma_p = \sigma_s$ $H_1: \sigma_p \neq \sigma_s$	В1		Hypotheses
	$F = 1.30945^2 / 0.710466^2 = 3.40$	M1 A1		Method for F 3.40 (3.39 ~ 3.4)
	c.v. F _[5,6] is 5.988	B1		5,6 df (or 6,5 if 0.710 ² /1.81 ² calculated)
	(or compare 0.294 with 0.167)	B1		5.988 (5.98 ~ 6)
	Accept H ₀ : accept standard deviations of breaking strengths of two types of line are equal	A1√	6	Conclusion in context - must be compared with correct tail of F
(d)	Not all null hypotheses can be true. At least one Type II error (accepting a false	E1		Not all null hypotheses can be true
	null hypothesis must have been made). Accepting the null hypothesis only shows	E1		Type II error must have been made
	that any evidence against it is not significant, not that it is true. In this case the samples are small, so accepting the	E1	3	Accepting null hypothesis does not prove it is true
	null hypothesis is quite a weak result.			Allow any other sensible comment, eg small samples (max 3)
	Total		27	
	TOTAL		75	