

General Certificate of Education

Statistics 6380

SS03 Statistics 3

Mark Scheme

2005 examination – June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Key to mark scheme and abbreviations used in marking

M m or dM A B E	mark is for method mark is dependent on one or more M marks and is for method mark is dependent on M or m marks and is for accuracy mark is independent of M or m marks and is for method and accuracy mark is for explanation					
or ft or F	follow through from previous					
	incorrect result	MC	mis-copy			
CAO	correct answer only	MR	mis-read			
CSO	correct solution only	RA	required accuracy			
AWFW	anything which falls within	FW	further work			
AWRT	anything which rounds to	ISW	ignore subsequent work			
ACF	any correct form	FIW	from incorrect work			
AG	answer given	BOD	given benefit of doubt			
SC	special case	WR	work replaced by candidate			
OE	ŌE	FB	formulae book			
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme			
–x EE	deduct x marks for each error	G	graph			
NMS	no method shown	с	candidate			
PI	possibly implied	sf	significant figure(s)			
SCA	substantially correct approach	dp	decimal place(s)			

Application of Mark Scheme

No method shown:	
Correct answer without working	mark as in scheme
Incorrect answer without working	zero marks unless specified otherwise
More than one method / choice of solution:	
2 or more complete attempts, neither/none crossed out	mark both/all fully and award the mean mark rounded down
1 complete and 1 partial attempt, neither crossed out	award credit for the complete solution only
Crossed out work	do not mark unless it has not been replaced
Alternative solution using a correct or partially correct method	award method and accuracy marks as appropriate

SSO3				
Q	Solution	Marks	Total	Comments
1(a) reverse d 6 13 2 12 3 10.5 1 10.5 4 9 8 8 7 7	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$	M1 M1 A1		Attempt at ranks Tied ranks Reverse ranks acceptable Inconsistent ranks gain M1, 1, 1 Alternative: $d = 7, 10,7\frac{1}{2}, 9\frac{1}{2}, 5, 0, 0, 4, 4, 7,$ 2, 10, 12 $\sum d^2 = 649\frac{1}{2}$ B1 6×640.5
10 6 9 5 11 4 5 3 12 2 13 1	$r_s = -0.787$ (3 sf from calc) sc -0.78/9 no method M1M1A1B1 subtract 1 mark if not negative	B3	6	$r_s = 1 - \frac{6 \times 649.5}{13 \times 168} = -0.784$ M1, A1
(b)	H_o Rank orders number of home runs and batting averages are independent. H_1 Rank orders of home runs and batting averages are not independent. 2 tail 1% $cv = \pm 0.6978$	B1		Generous
	test stat $r_s = -0.787$	B1		For cv – ignore sign (range allowed
	$\mathbf{r}_{s} < \mathbf{cv} \text{ or } \mathbf{r}_{s} > \mathbf{cv} $	M1		B0M1) For comparison ts/cv
	Reject H _o Significant evidence at 1% level to suggest an association between rank orders of number of home runs and	A1		$r_s = -0.787 \text{ or } -0.784$ can be implied +/- cv/ts comparison M0 A1E1 poss
	batting average.	E1		Ft – not if contradictory
	[Results suggests that teams that score more home runs tend to have lower batting averages.]		5	in context – need not be correct but ft in context
	Total		11	
2	H _o pop median, $\eta = 42$ H ₁ pop median, $\eta > 42$ 1 tail 10% Signs - + + + + - + - + + + +	B1		Clear η required or use of 'population'
	n = 12 ts = 8+/4 –	M1		Signs or differences
	Binomial model B (12, 0.5)	A1		for 8+ and 4-
	$P (\ge 8 +) = P(\le 4 -) = 0.1938 > 0.10$ for one tail test	M1 M1		Binomial model used and probability attempted and seen Comparison of Binomial probability 0.1938 (or awrt 0.19 with 0.10)
	Accept H_0 . There is insufficient evidence, at the 10% level, to suggest that the median is greater	A1	7	Alternative – cr identified as {9,10,11,12} with prob 0.0730 used Interpretation in context – need not
	than 42.	E1		be correct but ft in context
	Total		7	

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Q	Solution	Marks	Total	Comments
3(a)(i)	$H_0 \eta_{\text{difference}} = 0$	B1		H ₀ $\mu_{\text{difference}} = 0 \text{ or } \eta_{1=} \eta_{2}$
	$H_1 \eta_{\text{ difference}} < 0 \qquad 2 \text{ tail} 5\%$			H ₁ $\mu_{\text{difference}} < 0 \text{ or } \eta_1 < \eta_2$ etc or in words
				etc of in words
	Carpet Difference Rank	M1		For differences – ignore signs
	Type 1-2 - +			(1-2 or 2-1)
	A -4 2			
	B - 14 7 C - 15 8	m1		For ranks $(1 = \text{smallest} \text{diff})$
	C - 15 8 D - 11 6	1111		ror ranks (1 – smanest junij)
	E - 45 9			
	F - 7 5			
	G + 6 4			
	H - 5 3			
	I + 3 1			
	Rank totals $T_{-} = 40$ $T_{+} = 5$	m1		For total of + / - ranks
	Test stat $T = 5$	A1		(even if ranked incorrectly)
	critical value = 6	B1		For cv (range allowed B0M1)
	T < cv	DI		Tor ev (Tange anowed Down)
	Reject H ₀ There is significant evidence to suggest			
	that there is a difference in the average	M1	0	For comparison ts/cv
	fixing times for the two adhesives.	A1 E1	9	must be in context and refer to
		LI		average
	Cost of adhesive, size of carpet			
(ii)	Long term reliability			
	Method of application etc	E1		Disallow 'carpets the same'
			1	allow 'surface carpet laid on' any relevant comment
			1	any relevant comment
(b)	By using each adhesive on each type of	B1		For idea of reducing experimental
	carpet, experimental error is reduced and			error For clear explanation in context
	any difference in fixing time detected is	E1	2	disallow 'more accurate' unless in
	due to adhesive used.			explanation
	Total		12	

SS03 (coi	iii)		•				C (
Q		Solut			Marks	Total	Comments
4(a)(i)	 (i) H_o Returns status is independent of when order was placed H₁ Returns status is not independent of when order was placed 1 tail 5% 			B1		Only H_o sufficient – must be clear on independence/no association Condone use of return/order in H_o even if not worded completely correctly	
		Prom	Sale	Stand			concerty
	No items returned	49.2	32.8	82			
	Some items	10.8	7.2	18	M1 m1		E method for 1 correct
	returned	2					For all E correct ft arithmetic error
	$ts = \sum \frac{(O - E)}{E}$	$\frac{E^2}{E}$			ml		ts sum with correct denominators disallow Yates' correction
	$= \frac{5.8^2}{49.2} + \frac{4.8^2}{32.8} + \frac{1^2}{82} + \frac{5.8^2}{10.8} + \frac{4.8^2}{7.2} + \frac{1^2}{18}$				A1		For ts in range 7.70 - 7.80 awfw
	= 7.77 cv df $= 2$ 5% cv $= 5.991$				B1		For cv (4.605, 9.210, 7.378 B0m1)
	ts > 5.991			m1		For comparison ts/cv	
	Reject H _o Sig evidence to suggest returns status is not independent of when order was placed				A1	8	No context required Can imply B1 for H _o
(ii)	Orders place much more being return during the S result in no	likely to a ed wherea ale are fai	result in n as orders j r less like	o items placed ly to	E1,1	2	E1 if inconsistent/inadequate Or greater likelihood of some returns for orders placed during the Sale etc. Must mention promotion and sale for E2. E1 generous if in context
				Total		10	

Q	Soluti	on		Marks	Total	Comments
4(b)(i)		First time	Repeat			
	No items returned	20 (17.64)	43 (45.36)	B1		For raw data numbers correct For contingency table headings, data all correct
	Some items returned	8 (10.36)	29 (26.64)		2	(E values bracketed)
(ii)	H_o Returns statu of customer H_1 Returns statu type of customer	s is not in		B1		Only H_o sufficient – must be clear on independence/no association Condone use of order/customer in H_o even if not worded completely correctly
		o n ²		M1		For E values method
	$ts = \sum \frac{(O - E)}{E}$ $\frac{1.86^2}{17.64} + \frac{1.86^2}{45.36}$		$\frac{1.86^2}{26.64}$	M1 m1		For ts for Yates' corr attempt include: O-E-0.5 or (O-E) ² - 0.5
	= 0.736			A1		For ts 0.730 -0.750 awft Condone if not 3 sf
	cv df = 1 5% ts < 3.84	cv =3.84	l	B1 m1		For cv CAO For comparison ts/cv ft
	Accept H _o No sig evidence status is indepen New customers return items.	dent of typ	be of customer		8	Allow A1 if H_0 fully correct and stated earlier In context
			Tota	al	10	

SS03 (co)				C t
Q	Solution	Marks	Total	Comments
5(a)	H_0 Samples from identical populations	B1		Or $H_0 \eta_A = \eta_B = \eta_C$
B1	H_1 Samples not from identical	D1		H ₁ at least two of η_A, η_B, η_C
Only if	populations 5% sig level	B1		do differ
μ				B1,0 if no 'population' used
	Ranks			H ₀ No difference
	Fertiliser A Fertiliser B Fertiliser C			H ₁ Difference In context used B1,0(B1 generous)
	1 9 3	M1		
	2 11 4			$A1 \ge 10$
	5 13 7	A2		A2 all correct
	6 15 8			
	10 16 12			
	17 14			
		1		T (1
	$T_A = 24 \qquad T_B = 81 \qquad T_C = 48$	ml		Totals
	$n_A = 5 \qquad n_B = 6 \qquad n_C = 6$	A1		Any one correct
	$\sum_{i=1}^{m} \frac{T_i^2}{n_i} = \frac{24^2}{5} + \frac{81^2}{6} + \frac{48^2}{5} = 1592.7$	m1		
	$\sum \frac{1}{n} = \frac{24}{5} + \frac{61}{6} + \frac{45}{5} = 1592.7$	m1		
	$_{i=1}$ n_i 3 0 3			
	12	m1		ft for test stat H with previous
	$H = \frac{12}{17 \times 18} \times 1592.7 - (3 \times 18) = 8.46$	1111		result substituted
	1/×18	A1		AWFW 8.40 – 8.50
		ΠΙ		1101 0.10 0.50
	Critical value from $\chi_2^2 = 5.99$	B1		
	H > 5.99			For cv (range allowed B0M1)
		M1		
	Sig evidence to reject H_0 and conclude	A1	13	Can imply B1,B0 at start of solution
	that samples are not from identical			1 5 7
	populations			
(b)(i)	There is significant evidence that at least	E1		Ft for E1
	two of the median yields (from plants fed			Difference in context
	with Fertilisers A, B or C) do differ.	E1	2	Mention of 'at least two'
	Medians 26, 42, $28\frac{1}{2}$			
(ii)	It would appear that those plants that were			
	fed Fertiliser B produced a significantly	B1	1	Identification of B
	higher yield on average.			
	Total		16	
L	I otar	I	10	

Q	Solution	Marks	Total	Comments
6(a)	H_o Samples are taken from identical populations H_1 Samples are not taken from identical populations 2 tail 5%	B1		Or $H_0 \eta_H = \eta_C$ $H_1 \eta_H \neq \eta_C$ need both or population average used – need both
	$U_{\rm H} = 66 - \frac{7 \times 8}{2} = 38$	M1		For attempt at U
	$U_{\rm C} = 70 - \frac{9 \times 10}{2} = 25$	A1		For either correct
	U = 25 cv = 13 for n = 7, m = 9 5% U > 13 Accept H ₀	B1 B1 M1		For correct U and consistent cv For cv (range allowed B0M1) For comparison ts/cv
	No significant evidence of any difference between the two techniques.	A1	7	
(b)	A Type II error would be to conclude that H_0 is true, that is there is no difference between the two techniques, when in fact	B1		Concept of Type II correct
	H _o is not true and the techniques do differ	E1	2	In context
	Total		9	
	Total		75	