

### **General Certificate of Education**

## **Statistics 6380**

SS02 Statistics 2

# **Mark Scheme**

2010 examination – January series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

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#### Key to mark scheme and abbreviations used in marking

M	mark is for method				
m or dM	mark is dependent on one or more M marks and is for method				
A	mark is dependent on M or m marks and is for accuracy				
В	mark is independent of M or m marks and is for method and accuracy				
E	mark is for explanation				
√or ft or F	follow through from previous incorrect result	MC	mis-copy		
CAO	correct answer only	MR	mis-read		
CSO	correct solution only	RA	required accuracy		
AWFW	anything which falls within	FW	further work		
AWRT	anything which rounds to	ISW	ignore subsequent work		
ACF	any correct form	FIW	from incorrect work		
AG	answer given	BOD	given benefit of doubt		
SC	special case	WR	work replaced by candidate		
OE	or equivalent	FB	formulae book		
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme		
–x EE	deduct x marks for each error	G	graph		
NMS	no method shown	c	candidate		
PI	possibly implied	sf	significant figure(s)		
SCA	substantially correct approach	dp	decimal place(s)		

#### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

### **SS02**

Q	Solution	Marks	Total	Comments
1(a)	4	B1	1	CAO
	short term variability about upward linear trend	E1 E1 E1	3	short term variability upward linear
		EI	3	allow random variation about upward non-linear trend
(c)	`(-156 -216 -143)/3 = -172	M1		attempt to find mean deviation from line or by calculation
		A1		-172 (-168 ~ -175) ignore sign
		A1	3	negative sign
(d)	880 - 172 = 708	B1		m.a. for Question 3 estimated from trend line
	Estimated expenditure £708m	M1		seasonal effect subtracted from their trend
	s.c. B2 for answer within range with no or	A 1		710 (705 715) -11 700 :
	unclear method	A1	3	$710 (705 \sim 715)$ allow 700 ignore units - disallow if more than 3sf given
	Total		10	and the same of grant
` ' ` '	Although there had been a reduction in	E1		reduction in recorded crime
	recorded crime nearly half the respondents thought there had been a large increase. Only a very small proportion (4%) correctly thought that there had been a decrease.	E1	2	most respondents believe there is at least as much
	The media highlight particularly horrific crimes, giving the impression there is more crime than is actually the case. Stories about crime are passed on from person to person and become exaggerated so that people think there is more crime than is actually the case. People whose friends or relatives experience a crime pay more attention to this than to national statistics. Amount of recorded crime may not accurately reflect the actual amount of crime.	E2(1)	2	E2 (1) Both marks for any valid well explained possible reason. May be earned in (b)(ii)
\ /	The answers are divided into four non-numerical discrete categories.	E1	1	box and whisker requires numerical data
, , , ,	Although only a small proportion of	E1		small proportion of reported crimes are
	crimes reported to the police (6%) are violent in nature the great majority of respondents (78%) believed that over 30% of crime involved violence or the threat of violence.	E1	2	violent majority of respondents overestimate the proportion of crimes which are violent
2(b)(ii)	(ii) as (a)(ii)	E1	1	any valid reason not used in (a)(ii) - may be earned in (a)(ii)
	Total		8	

SS02 (cont)

SS02 (cont)			1	,
Q	Solution	Marks	Total	Comments
3(a)	$H_0$ : $\mu = 90$ $H_1$ : $\mu > 90$	B1		one hypothesis correct
	$\bar{x} = 109.56$	B1		both hypotheses correct
	$z = (109.56 - 90)/(55/\sqrt{9})$ $= 1.07$ c.v. for 5% test is 1.6449  Accept H <sub>0</sub> . Conclude no significant evidence that the mean waiting time for	M1 m1 A1 B1		use of $55/\sqrt{9}$ correct method for z - ignore sign $1.07~(1.06\sim1.07)$ $1.6449~(1.64\sim1.65)$ - ignore sign conclusion - must compare correct tail of z
	calls made to Northgas exceeds 90 seconds.  ( p-value 0.143 )	A1√	8	conclusion in context
(b)	H <sub>0</sub> : $\mu = 90$ H <sub>1</sub> : $\mu > 90$ $z = (94 - 90)/(12/\sqrt{85})$ = 3.07	M1 m1		use of $12/\sqrt{85}$ method for z - ignore sign $3.07 (3.07\sim3.08)$
	c.v. for 5% test is $1.6449$ Reject $H_0$ . Conclude there is significant evidence that mean waiting time for calls made to Southgas exceeds 90 seconds. (p-value $0.00107$ )	A1√ A1√	5	conclusion - must compare correct tail of z conclusion in context
	Apply mark scheme for (a) to (b) and vice versa if more favourable to candidate.			
(c)(i)	Sample mean in (a) greater than in (b) but population mean accepted as equal to 90 in (a) but concluded to be greater than 90	E1 E1	2	sample mean greater in (a) than (b) comparison of conclusions
(in)	in (b).		_	T
(ii)	Larger sample in (b) makes any difference from 90 more likely to be detected / More variable sample in (a) makes any difference from 90 less likely to be detected.	E1	1	sample size or variability
	Total		16	

SS02 (cont)

Q       Solution         4(a)       Plot points: $(1, 2166), (2, 2)$ $(3, 2638), (4, 2825), (5, 301)$ $(7, 3402), (8, 3433), (9, 347)$ (b) $y = 2093 + 172.3t$ $t = 0$ $y = 2093$ $t = 10$ $y = 3816$ (c)       Forecast of number of scree 2006 is $2093 + 172.3 \times 11$ (d)       Graph suggests actual figure below the regression line         5(a) $0.8335$ (b)(i) $0.0273$ (ii) $0.3027 - 0.1257 = 0.177$ (iii) $P_0(5)$	7), (6, 3248), (5)	Marks M1 A1 B2 B1 M1 A1 M1	<b>Total</b> 2	method of plotting reasonably accurate plot – by eye  172.3 (172~173) one mark for (170~175) 2093 (2090~2100)
(a) $(3, 2638), (4, 2825), (5, 301), (7, 3402), (8, 3433), (9, 347), (9, 347), (9, 347), (10, 10), (10, 1$	7), (6, 3248), (5)	B2 B1 M1 A1		reasonably accurate plot – by eye  172.3 (172~173) one mark for (170~175) 2093 (2090~2100)
t = 0  y = 2093 t = 10  y = 3816 (c) Forecast of number of screed 2006 is 2093 + 172.3×11 (d) Graph suggests actual figure below the regression line 5(a) 0.8335 (b)(i) 0.0273 (ii) 0.3027 - 0.1257 = 0.177		B1 M1 A1	5	one mark for (170~175) 2093 (2090~2100)
(c) Forecast of number of scree 2006 is $2093 + 172.3 \times 11$ (d) Graph suggests actual figure below the regression line  5(a) 0.8335  (b)(i) 0.0273  (ii) 0.3027 - 0.1257 = 0.177		M1 A1	5	2093 (2090~2100)
(c) Forecast of number of scree 2006 is 2093 + 172.3×11  (d) Graph suggests actual figure below the regression line  5(a) 0.8335  (b)(i) 0.0273  (ii) 0.3027 - 0.1257 = 0.177		M1 A1	5	` /
2006 is 2093 + 172.3×11  (d) Graph suggests actual figure below the regression line  5(a) 0.8335  (b)(i) 0.0273  (ii) 0.3027 - 0.1257 = 0.177		A1	5	method for line - their equation
2006 is 2093 + 172.3×11  (d) Graph suggests actual figure below the regression line  5(a) 0.8335  (b)(i) 0.0273  (ii) 0.3027 - 0.1257 = 0.177				accurate line - by eye
below the regression line  5(a) 0.8335  (b)(i) 0.0273  (ii) 0.3027 - 0.1257 = 0.177	= 3088			attempt to substitute 11 in their equation
below the regression line  5(a) 0.8335  (b)(i) 0.0273  (ii) 0.3027 - 0.1257 = 0.177	- 3700	A1	2	3988 (3980~4000) - disallow if not whole number
(b)(i) 0.0273 (ii) 0.3027 - 0.1257 = 0.177	e will be	M1		forecast reduced by a non-trivial amount
(b)(i) 0.0273 (ii) 0.3027 - 0.1257 = 0.177	- say 3500	A1	2	3500 (3400 ~ 3800)
(b)(i) $0.0273$ (ii) $0.3027 - 0.1257 = 0.177$	Total		11	
(ii) $0.3027 - 0.1257 = 0.177$		B1	1	$0.834 \ (0.833 \sim 0.834)$
		B1	1	0.0273 ( 0.027~0.0274)
(iii) P (5)		M1 A1	2	P (2 or fewer) - P(1 or fewer) 0.177 (0.1765 ~ 0.1775)
		B1		D (5)
P(>6) = 1 - 0.7622 = 0.237	Q	м1		P <sub>o</sub> (5) method - their mean
1 (>0) - 1 - 0.7022 - 0.237	o	A1	3	$0.238 (0.237 \sim 0.238)$
(c) $E(Y) = 0 \times 0.24 + 1 \times 0.27 + 3 \times 0.12 + 4 \times 0.08$		M1		method for $E(Y)$
= 1.53		A1		1.53 CAO
$E(Y^2) = 0^2 \times 0.24 + 1^2 \times 0.22 + 3^2 \times 0.12 + 4^2 \times 0.02 + 3^2 \times 0.12 + 4^2 \times 0.02 + 3^2 \times 0$		M1		method for $E(Y^2)$
$V(Y) = 3.79 - 1.53^2$				
= 1.4491		m1		method for s.d.
s.d. = $\sqrt{1.4491}$ = 1.20		A1	5	1.20 (1.20 $\sim$ 1.21) SC allow max 4 for variance = 1.45 (1.44 $\sim$ 1.46)
(d) s.d. of $Z = \sqrt{2.89} = 1.7$		E1	1	$\sqrt{2.89}$ AG
(e)(i) X		B1		CAO
(ii) s.d. $W = \sqrt{1.4} = 1.18$ , s.d of are all larger	X, Y  and  Z	M1		attempt to compare s.d. or variances
W is least variable		M1		method for s.d. of W or X
		A1	4	W least variable

#### SS02 (cont)

Q	Solution	Marks	Total	Comments
6(a)	Number examiners 000 to 399	B1		400 examiners - may be implied
		E1		valid numbering
	Select 3 digit random numbers	E1		select 3 digit random numbers
	Ignore repeats and greater than 399	E1		ignore repeats and out of range
	Continue until 40 selected choose	E1	5	select 40 and choose corresponding
	corresponding examiners			examiners
(b)(i)	Cluster sampling	B1	1	cluster sampling
(ii)	More geographically localised - less travelling	E1	1	less travelling
(iii)	Views will differ between regions e.g.	E1		views likely to be more homogeneous
	examiners from South East likely to prefer London and examiners from North West likely to prefer Manchester	E1	2	in context
(iv)	No - examiners from regions with small	B1		no
	number of examiners e.g. North West			
	more likely to be selected than those from	E1	_	explanation
	regions with a large number of examiners.		2	allow B1 for no, examiners in regions not
				chosen have no
(a)	(i) (b)(ii) no longer velid since no			chance
(c)	(i) (b)(ii) no longer valid since no travelling required	E1		no travelling needed
	(ii) (b)(iii) still valid - using telephone	Li		no navoming needed
	email does not affect it.	E1		views will still differ between regions
			2	allow E1 for (i) no (ii) yes without
				explanation
	Total		13	
	TOTAL		75	