

# Free-Standing Mathematics Qualification June 2011 

Mathematics Advanced Level
(Specification 6990)
Using and Applying Statistics

Mark Scheme

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## Key to mark scheme and abbreviations used in marking

| M | mark is for method |  |  |
| :---: | :---: | :---: | :---: |
| m or dM | mark is dependent on one or more M marks and is for method |  |  |
| A | mark is dependent on M or m marks and is for accuracy |  |  |
| B | mark is independent of M or m marks and is for method and accuracy |  |  |
| E | mark is for explanation |  |  |
| $\checkmark$ or ft or F | follow through from previous |  |  |
|  | incorrect result | MC | mis-copy |
| CAO | correct answer only | MR | mis-read |
| CSO | correct solution only | RA | required accuracy |
| AWFW | anything which falls within | FW | further work |
| AWRT | anything which rounds to | ISW | ignore subsequent work |
| ACF | any correct form | FIW | from incorrect work |
| AG | answer given | BOD | given benefit of doubt |
| SC | special case | WR | work replaced by candidate |
| OE | OE | FB | formulae book |
| A2,1 | 2 or 1 (or 0) accuracy marks | NOS | not on scheme |
| $-x$ EE | deduct $x$ marks for each error | G | graph |
| NMS | no method shown | c | candidate |
| PI | possibly implied | sf | significant figure(s) |
| SCA | substantially correct approach | dp | decimal place(s) |

## Application of Mark Scheme

## No method shown:

Correct answer without working
Incorrect answer without working
More than one method / choice of solution:
2 or more complete attempts, neither/none crossed out
1 complete and 1 partial attempt, neither crossed out

## Crossed out work

Alternative solution using a correct or partially correct method
mark as in scheme
zero marks unless specified otherwise
mark both/all fully and award the mean mark rounded down
award credit for the complete solution only
do not mark unless it has not been replaced
award method and accuracy marks as appropriate

## Free-Standing Mathematics Qualification

## Advanced Level: Using and Applying Statistics (6990/2)

Answers and Marking Scheme - June 2011

## Question 1

| (a) | $\begin{aligned} & 18.3-14.3(=4) \\ & \frac{\text { their } 4}{14.3} \times 100(=27.97 \ldots \%) \end{aligned}$ | B1 <br> B1 | OE |
| :---: | :---: | :---: | :---: |
| (b) | $\frac{18.3}{70} \times 100$ <br> $26.1-18.3=7.8(4 \ldots)$ million | M1 M1 <br> A1 | OE $\frac{18.3}{0.7}$ M2 <br> 7.8 m or better, must have units |
|  | TOTAL | 5 |  |

## Question 2

| (a)(i) | 2008 Q4 and 2009 Q1 | B1 |  |
| :---: | :--- | :---: | :--- |
| (a)(ii) | $1422-1059.9$ | M1ft |  |
|  | $362 .(1)$ thousand | A1 | must have units |
| (b)(i) | positive gradient or increasing | B1 |  |
| (b)(ii) | recession or unemployment rising etc. | B1 |  |
| (c) | recognise compound reduction | M1 | $\times 0.9 \ldots \times 0.9$ etc |
|  | arriving at Q4 2011 $=1275.75$ | A1 |  |
|  | arriving at $($ Q3 2012 $)=930.02$ | A1 | A1 |
| stating Q3 2012 | Correct answer without <br> working $\Rightarrow$ SC2 |  |  |
|  | TOTAL | $\mathbf{9}$ |  |

## Question 3

| (a) | $\begin{aligned} & \text { Obtaining (9.6), 30.6, 51.7, 70.9, 86.9, } 92.5 \text {, } \\ & 95.0,97.3,(100.1) \end{aligned}$ <br> Rounding errors | B1 <br> B1 | Or percentages are to 1 dp |
| :---: | :---: | :---: | :---: |
| (b) | plotting the percentage cumulative frequencies at upper cumulative boundaries <br> their heights ( $\pm 1 \mathrm{sq}$ ) <br> joined by curve or straight lines | M1 <br> A1 <br> A1 | on boundaries <br> must be an increasing <br> function <br> or cumulative bar chart $\Rightarrow$ <br> M1 A1 A0 <br> fully correct |
| (c)(i) | $\text { median } \approx 4.9 \mathrm{~km}(\leq 5)$ <br> For a correct graph accept any value $4.5-5$ | B1ft | part (c)(i) and (c)(ii) and (d)(i) must be from an increasing non-linear function <br> allow tolerance $\pm \frac{1}{2}$ sq |
| (c)(ii) | their $12.5(11-13)$ - their $1.75(<2)$ for correct graphs $\approx 10.75 \quad(9-12)$ | M1 <br> A1ft | correctly locating and attempting to subtract their quartiles |
| (d)(i) | Box and quartiles drawn ft correctly from their graph <br> whiskers to 0 km and 80 km | B1ft B1 | Can only ft drawn cumulative frequency curve <br> (Not cumulative bar chart or single points) <br> both whiskers correct $\pm \frac{1}{2}$ sq |
| (d)(ii) | Positive skew | B1 | Or a good description of positive skew |
| (d)(iii) | (Median of England is greater than the median of Newcastle-upon-Tyne suggesting) people in Newcastle-upon-Tyne do not travel as far to work. <br> The interquartile range of England is much greater than that for Newcastle-upon-Tyne which suggests that people in Newcastle-uponTyne are more consistent in their distances travelled to work. | B1 B2 | Not ft. Do not allow if (c)(i) and (c)(ii) are vastly incorrect eg 50 and 39 km . <br> B1 for just saying greater in England with nothing in context |
|  | TOTAL | 14 |  |

## Question 4

| (a) | The mean number of days is +9 meaning that the Oak first leafed on average around the $29^{\text {th }}$ April each year | B2 | B1 for +9 |
| :---: | :---: | :---: | :---: |
| (b) | $\begin{aligned} & \bar{x}=-12.3 \\ & \sum\left(x_{i}-\bar{x}\right)^{2}=412.06 \\ & \sigma_{n}=6.42 \end{aligned}$ | $\begin{gathered} \text { B1 } \\ \text { M1 A1 } \\ \text { A1 } \end{gathered}$ | accept $\sigma_{n-1}=6.77$ |
| (c) | On average, the Oak is first leafing about April $8^{\text {th }}$ in the 90 s which is 3 weeks before it was first leafing in the 50s <br> The sd is less in the 90 s compared to the 50 s <br> The numbers are more consistent in the 90 s than in the 50 s | B1 <br> B1 <br> B1 | Leaves appear much earlier in the 90s <br> Or 21.(3) days difference <br> Can imply second B1 |
| (d) | These data seem to support the idea of global warming in that the Oak first leaves are much earlier because of the warmer weather | B1 | OR The claim appears to be correct but it may not be correct it could just be natural variation <br> OR There is not enough evidence |
|  | TOTAL | 10 |  |

## Question 5

| (a)(i) | $\bar{x}=11.8$ | B1 | 3 sf or better |
| :---: | :---: | :---: | :---: |
| (a)(ii) | $\bar{y}=75.5$ | B1 |  |
| (b)(i) | $r=0.996$ | B1 | 3sf or better from 0.99557863 |
| (b)(ii) | $r$ is very high and positive suggesting that there is strong positive correlation between the foot length and height of these boys. | B1 | Do not accept perfect positive correlation |
| (c)(i) | $y=5.77 x+7.41$ | B2 | B1 if both correct but either not to 2dp <br> $a, b$ interchanged $=\mathrm{SC} 1$ |
| (c)(ii) | $a=5.77$ which is the regression coefficient it tells us the gradient of the regression line it means as foot length increases by 1 cm height increases by 5.77 cm | B1 <br> B1ft | ft their $a$ |
| (c)(iii) | calculate and plot two points within the grid using their equation ( $x$-intercept $>7.2,<7.5$ ) if no $x$-intercept check for $(9,59.3-<60)$ point <br> draw line through their two points | M1 <br> M1 <br> A1ft | or use their $(\bar{x}, \bar{y})$ as one point <br> correctly calculated points plotted incorrectly implies SC1 <br> SC1 line drawn through ( $\bar{x}, \bar{y}$ ) with positive gradient $\pm \frac{1}{2} \mathrm{sq}$ |
| (d) | Use their equation with $x=13.8$; $" y=5.77 \times 13.8+7.41 "$ $87 \mathrm{~cm}$ | M1 <br> A1ft | can use the correct drawn line not an incorrectly drawn line <br> NB $108.0(a, b$ interchanged) |
|  | TOTAL | 13 |  |

## Question 6

| (a) | $\begin{aligned} & \mathrm{P}\left(\mathrm{M}>27 \equiv P\left(Z<\frac{27-24.9}{1.05}\right) \text { or } P(Z>2)\right. \\ & 1-\Phi(2) \\ & 1-0.9772 \\ & 0.0228 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { M1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | penalise 1 mark for incorrect standardising |
| :---: | :---: | :---: | :---: |
| (b) | $\begin{aligned} & P(22<W<25)=P\left(\frac{22-22.8}{0.89}<Z<\frac{25-22.8}{0.89}\right) \\ & P(-0.899<Z<2.47) \\ & \Phi(2.47)-[1-\Phi(.899)] \\ & (=0.9932-[1-0.8156]) \times 100 \\ & 82 \% \text { or } 81 \% \end{aligned}$ | M1 <br> A1,A1 <br> M1 <br> A1 | $\begin{aligned} & \frac{22.8-22}{0.89}<Z<\frac{22.8-25}{0.89} \\ & 0.899,-2.47 \\ & \text { penalise } 1 \text { mark for } \\ & \text { incorrect standardising } \\ & \text { allow no interpolation } \\ & \Phi(2.47)-[1-\Phi(0.90)] \\ & (=0.9932-[1-0.8159]) \\ & \times 100 \\ & \text { from } 81.88 \% \text { or } 80.91 \% \end{aligned}$ |
|  | TOTAL | 9 |  |
|  | TOTAL MARK FOR PAPER | 60 |  |

