# AQA 

ASSESSMENT and
OUALIFICATIONS

## General Certificate of Education

## Mathematics 6360

## MPC3 Pure Core 3

## Mark Scheme <br> 2005 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

# Key to mark scheme and abbreviations used in marking 

| M | mark is for method |  |  |
| :---: | :---: | :---: | :---: |
| m or dM | mark is dependent on one or more M marks and is for method |  |  |
| A | mark is dependent on M or m marks and is for accuracy |  |  |
| B | mark is independent of M or m marks and is for method and accuracy |  |  |
| E | mark is for explanation |  |  |
| $\checkmark$ or ft or F | follow through from previous incorrect result | MC | mis-copy |
| CAO | correct answer only | MR | mis-read |
| CSO | correct solution only | RA | required accuracy |
| AWFW | anything which falls within | FW | further work |
| AWRT | anything which rounds to | ISW | ignore subsequent work |
| ACF | any correct form | FIW | from incorrect work |
| AG | answer given | BOD | given benefit of doubt |
| SC | special case | WR | work replaced by candidate |
| OE | OE | FB | formulae book |
| A2,1 | 2 or 1 (or 0) accuracy marks | NOS | not on scheme |
| $-x$ EE | deduct $x$ marks for each error | G | graph |
| NMS | no method shown | c | candidate |
| PI | possibly implied | sf | significant figure(s) |
| SCA | substantially correct approach | dp | decimal place(s) |

## Application of Mark Scheme

## No method shown:

Correct answer without working
Incorrect answer without working

## More than one method / choice of solution:

2 or more complete attempts, neither/none crossed out
1 complete and 1 partial attempt, neither crossed out

## Crossed out work

Alternative solution using a correct or partially correct method
mark as in scheme zero marks unless specified otherwise
mark both/all fully and award the mean mark rounded down
award credit for the complete solution only
do not mark unless it has not been replaced
award method and accuracy marks as appropriate

MPC3


MPC3 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 3(a) | $\frac{1}{4} e^{4 x}$ | B1 | 1 |  |
| (b) | $\begin{array}{lr} \int \mathrm{e}^{4 x}(2 x+1) \mathrm{d} x & \\ u=2 x+1 & \mathrm{~d} v=\mathrm{e}^{4 x} \\ \mathrm{~d} u=2 & v=\frac{1}{4} \mathrm{e}^{4 x} \end{array}$ | M1 |  | by parts |
|  | $\begin{aligned} & =\frac{1}{4}(2 x+1) \mathrm{e}^{4 x}-\frac{1}{2} \int \mathrm{e}^{4 x} \mathrm{~d} x \\ & =\frac{1}{4}(2 x+1) \mathrm{e}^{4 x}-\frac{1}{8} \mathrm{e}^{4 x}(+c) \end{aligned}$ | M1 <br> A1 | 3 | Their $\left(u v-\int v \mathrm{~d} u\right)$ |
| (c) | $\begin{aligned} & u=1+\ln x \\ & \frac{\mathrm{~d} u}{\mathrm{~d} x}=\frac{1}{x} \text { or } \frac{\mathrm{d} x}{\mathrm{~d} u}=\mathrm{e}^{u-1} \\ & \int=\int u \mathrm{~d} u=\frac{u^{2}}{2}(+c) \\ & =\frac{(1+\ln x)^{2}}{2}(+c) \end{aligned}$ | B1 <br> M1 <br> A1 <br> A1 | 4 | in terms of $u$ only |
|  | Total |  | 8 |  |
| 4(a) | $\begin{aligned} & \tan ^{2} x=\sec x+11 \\ & \sec ^{2} x-1=\sec x+11 \\ & \sec ^{2} x-\sec x-12=0 \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \end{aligned}$ | 2 | Or attempt to form quadratic in $\cos ^{2}$ $\tan ^{2} x=\sec ^{2} x-1$ <br> AG |
| (b) | $(\sec x-4)(\sec x+3)=0$ | M1 |  | attempt at solving quadratic |
|  | $\begin{aligned} & \sec x=4,-3 \\ & \therefore \cos x=\frac{1}{4},-\frac{1}{3} \end{aligned}$ | $\begin{gathered} \text { A1F } \\ \text { A1 } \end{gathered}$ | 3 | AG; (A0 if no use of $\cos x=\frac{1}{\sec x}$ ) |
| (c) | $\begin{aligned} & x=76^{\circ}, 284^{\circ} \\ & x=109^{\circ}, 251^{\circ}(\text { or better }) \end{aligned}$ | $\begin{gathered} \mathrm{B} 1 \\ \mathrm{~B} 1, \mathrm{~B} 1 \end{gathered}$ | 3 | ```2 correct other answers (-1 each extra in range )``` |
|  |  |  |  | If radians $\quad x=1.32,4.97$ $1.91,4.37$ <br> B1 any 2 correct <br> B1 other 2 correct |
|  | Total |  | 8 |  |

MPC3 (cont)


MPC3 (cont)


MPC3 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 7(a) | $\frac{\pi}{2}$ |  |  |  |
|  |  | B1 |  | shape |
|  |  | B1 | 2 | asymptotes (shown or stated) $\left(\frac{\pi}{2}\right.$ seen $)$ |
| (b)(i) | $\dagger$ / |  |  |  |
|  | , | B1 |  | sketch of $2 x-1$ |
|  |  | B1 | 2 | correct |
| (ii) | $\tan ^{-1} x-2 x+1=0$ |  |  |  |
|  | $\mathrm{f}(0.8)=0.07$ | M1 |  |  |
|  | $f(0.9)=-0.07$ |  |  |  |
|  | change of sign $\therefore$ root | A1 | 2 | allow +ve, -ve |
|  |  |  |  | A0 if $f(0.8), \mathrm{f}(0.9)$ wrong |
| (c) | $\left(x_{1}=0.8\right)$ | M1 |  | attempt at $x_{2}$ |
|  | $x_{2}=0.837(37) \ldots$ | A1 |  | for $x_{2}$ |
|  | $x_{3}=0.85$ | A1 | 3 | for $x_{3}$ |
|  | Total |  | 9 |  |

MPC3 (cont)


