

### **General Certificate of Education**

## **Mathematics 6360**

MPC1 Pure Core 1

# **Mark Scheme**

2008 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

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#### Key to mark scheme and abbreviations used in marking

| M                          | mark is for method   |     |                            |  |
|----------------------------|--|-----|----------------------------|--|
| m or dM                    | mark is dependent on one or more M marks and is for method         |     |                            |  |
| A                          | mark is dependent on M or m marks and is for accuracy              |     |                            |  |
| В                          | mark is independent of M or m marks and is for method and accuracy |     |                            |  |
| Е                          | mark is for explanation  |     |                            |  |
|                            |  |     |                            |  |
| $\sqrt{\text{or ft or F}}$ | follow through from previous                                       |     |                            |  |
|                            | incorrect result   | MC  | mis-copy                   |  |
| CAO                        | correct answer only  | MR  | mis-read                   |  |
| CSO                        | correct solution only  | RA  | required accuracy          |  |
| AWFW                       | anything which falls within  | FW  | further work               |  |
| AWRT                       | anything which rounds to   | ISW | ignore subsequent work     |  |
| ACF                        | any correct form   | FIW | from incorrect work        |  |
| AG                         | answer given   | BOD | given benefit of doubt     |  |
| SC                         | special case   | WR  | work replaced by candidate |  |
| OE                         | or equivalent  | FB  | formulae book              |  |
| A2,1                       | 2 or 1 (or 0) accuracy marks                                       | NOS | not on scheme              |  |
| −x EE                      | deduct x marks for each error                                      | G   | graph                      |  |
| NMS                        | no method shown  | c   | candidate                  |  |
| PI                         | possibly implied   | sf  | significant figure(s)      |  |
| SCA                        | substantially correct approach                                     | dp  | decimal place(s)           |  |

#### No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

#### MPC1

| Q    | Solution   | Marks | Total | Comments  |
|------|--|-------|-------|---|
| 1(a) | L: straight line with positive gradient and  | B1    |       | Line must cross both axes but need not  |
|      | negative intercept on y-axis   | D 1   |       | reach the curve   |
|      | cutting at $\left(\frac{1}{3},0\right)$ and $\left(0,-1\right)$  | B1    |       | Condone 0.33 or better for $\frac{1}{3}$  |
|      | (intercepts <b>stated</b> or marked on sketch)   |       |       |   |
|      | C: attempt at parabola ∪ or ∩ through (-3,0) and (1,0) or values -3 and 1 stated as intercepts   | В1    |       | y <b>\</b>  |
|      | on <i>x</i> -axis  ∪ shaped graph – vertex below <i>x</i> -axis and cutting <i>x</i> -axis twice   | M1    |       | $ \begin{array}{c c} -3 & \frac{1}{3} & 1 \\ -1 & \chi & 1 \end{array} $                                  |
|      | through $(0,-3)$ and minimum point to left of y-axis   | A1    | 5     | (y-intercept or coordinates marked)   |
| (b)  |  | M1    |       |   |
|      | $x^2 + 3x - x - 3 - 3x + 1 = 0$  |       |       |   |
|      | $x^{2} + 3x - x - 3 - 3x + 1 = 0$<br>$\Rightarrow x^{2} - x - 2 = 0$   | A1    | 2     | AG; must have "= 0" and no errors   |
| (c)  | (x-2)(x+1) = 0   | M1    |       | $(x\pm 1)(x\pm 2)$ or use of formula (one slip)   |
|      | $\Rightarrow x = 2, -1$  | A1    |       | correct values imply M1A1   |
|      | Substitute one value of <i>x</i> to find <i>y</i>  | m1    |       |   |
|      | Points of intersection $(2, 5)$ and $(-1,-4)$  | A1    | 4     | May say $x = 2$ , $y = 5$ etc<br>SC: $(2, 5) \Rightarrow B2$<br>$(-1, -4) \Rightarrow B2$ without working |
|      | Total  |       | 11    | (1, 4) $\rightarrow$ B2 without working   |
| 2(a) | xy = 6   | B1    | 1     | B0 for $\sqrt{36}$ or $\pm 6$   |
| (b)  | $\frac{y}{x} = \frac{2\sqrt{3}}{\sqrt{3}}$ or $\sqrt{\frac{12}{3}}$ or $\sqrt{\frac{4}{1}}$ or $\frac{\sqrt{12}}{\sqrt{3}} \times \frac{\sqrt{3}}{\sqrt{3}}$ | M1    |       | Allow M1 for ±2   |
|      | = 2  | A1    | 2     |   |
| (c)  | $x^{2} + 2xy + y^{2}$ or $(\sqrt{3} + 2\sqrt{3})^{2}$ correct  | M1    |       | or $(\sqrt{3} + \sqrt{12})(\sqrt{3} + \sqrt{12})$ expanded as   |
|      | 2 2  |       |       | 4 terms – no more than one slip   |
|      | <b>Correct</b> with 2 of $x^2$ , $y^2$ , $2xy$ simplified  | A1    |       | Correct but unsimplified – one more step  |
|      | $3 + 2\sqrt{36} + 12$ or $3^2 \times 3$ or $(3\sqrt{3})^2$   |       |       |   |
|      | = 27   | A1    | 3     |   |
|      | Total  |       | 6     |   |

MPC1 (cont)

| MPC1 (cont   | Solution   | Marks      | Total | Comments   |
|--------------|--|------------|-------|--|
|              |  | M1         | 10441 | Attempt at $V$ in terms of $x$ (condone slip                         |
| ` '          | , ,,,,   |            |       | when rearranging formula for $y = 9 - 3x$ )                          |
|              |  |            |       | or $(9-3x)^2 = 81-54x+9x^2$  |
|              | $V = x(81 - 54x + 9x^2)$   |            |       |  |
|              | $=81x - 54x^2 + 9x^3$  | A1         | 2     | AG; no errors in algebra   |
|              |  |            |       |  |
| (b)(i)       | $\frac{dV}{dx} = 81 - 108x + 27x^2$  | M1         |       | One term correct   |
|              | $\mathrm{d}x$  | A1<br>A1   |       | Another correct All correct (no + $c$ etc)                           |
|              |  | 711        |       | The correct (no + c etc)   |
|              | $=27(x^2-4x+3)$  | A1         | 4     | CSO; all algebra and differentiation                                 |
|              | ,  |            |       | correct  |
| (ii)         | (x-3)(x-1) or $(27x-81)(x-1)$ etc  | M1         |       | "Comment" featons on comment was of formula                          |
| (11)         | $\Rightarrow x = 1, 3$   | M1         | 2     | "Correct" factors or correct use of formula                          |
|              | → x − 1, 3   | A1         | 2     | SC: B1,B1 for $x = 1$ , $x = 3$ found by                             |
|              |  |            |       | inspection (provided no other values)                                |
|              |  |            |       | ,  |
| (c)          | $\frac{d^2V}{dx^2} = -108 + 54x$ (condone one slip)                                | M1         |       | ft their $\frac{dV}{dr}$ (may have cancelled 27 etc)                 |
|              | $dx^2 = 100 + 34x  \text{(condone one ship)}$                                      |            |       | uλ   |
|              |  | A1         | 2     | CSO; all differentiation correct                                     |
|              | $d^2V$ $d^2V$  |            |       | $A^2V$   |
| (d)(i)       | $x=3 \Rightarrow \frac{d^2V}{dx^2} = 54;  x=1 \Rightarrow \frac{d^2V}{dx^2} = -54$ | B1√        | 1     | ft their $\frac{d^2V}{dx^2}$ and their <b>two</b> x-values           |
|              | ux ux  |            |       | u.   |
| (**)         |  | F.1        |       | $d^2V$   |
| (ii)         | (x =) 1 (gives maximum value)  | E1         | 1     | Provided their $\frac{d^2V}{dx^2} < 0$                               |
|              |  |            |       |  |
| (iii)        | $V_{\rm max} = 36$   | B1         | 1     | CAO  |
|              | Total  |            | 13    |  |
| <b>4</b> (a) | $\left(r-\frac{3}{2}\right)^2$   | B1         |       | Must have () <sup>2</sup> $p = 1.5$                                  |
|              | $\left(x-\frac{1}{2}\right)$   | <b>D</b> 1 |       | , , ,  |
|              | +7   | B1         | 2     | q = 1.75   |
|              | 4  |            | _     |  |
|              | 7  |            |       |  |
| <b>(b)</b>   | Minimum value is $\frac{1}{4}$   | B1√        | 1     | ft their $q$ or correct value  |
|              | 4  |            |       |  |
| (c)          | Translation  | E1         |       | ( <b>not</b> shift, move, transformation etc)                        |
|              | (and <b>no other</b> transformation stated)  |            |       |  |
|              | [2]  | M1         |       | M1 for one component correct   |
|              | through $\begin{vmatrix} \frac{3}{2} \\ 7 \end{vmatrix}$ (or equivalent in words)  | 1V1 1      |       | M1 for one component correct or ft their <i>p</i> or <i>q</i> values |
|              | through $\begin{vmatrix} 2 \\ 7 \end{vmatrix}$ (or equivalent in words)            |            |       | or it then p or q values   |
|              | $\left  \frac{1}{4} \right $   | A1         | 3     | CSO; condone 1.5 right and 1.75 up etc                               |
|              |  |            | 6     |  |
|              | Total  |            | 6     |  |

MPC1 (cont)

| MPC1 (cont  |   | Manler         | T-4-1    | Comments  |
|-------------|---|----------------|----------|---|
| Q           | Solution  | Marks          | Total    | Comments  |
| 5(a)        | $\operatorname{Grad} AC = \frac{15}{3} = 5$                               | B1             |          | OE  |
|             | Equation of AC: $y = m(x+2)$<br>or $(y-15) = m(x-1)$                      | M1             |          | Or use of $y = mx + c$ with $(-2, 0)$ or $(1, 15)$ correctly substituted for $x$ and $y$    |
|             | y = 5x + 10   | A1             | 3        | OE eg $y-15=5(x-1)$ , $y=5(x+2)$  |
| (b)(i)      | $\left[16x - \frac{x^5}{5}\right]$  | M1<br>A1<br>A1 |          | Raise one power by 1 One term correct All correct   |
|             | $\left(16 - \frac{1}{5}\right) - \left(-32 + \frac{32}{5}\right)$         | m1             |          | F(1) - F(-2) attempted  |
|             | $=41\frac{2}{5}$ (or 41.4, $\frac{207}{5}$ etc)                           | A1             | 5        | CSO; withhold if $+ c$ added  |
| (ii)        | Area $\Delta = \frac{1}{2} \times 3 \times 15$ or $22\frac{1}{2}$ or 22.5 | B1             |          | Or $\int_{-2}^{1} (5x+10) dx = 22.5$  |
|             | Shaded area = "their (b)(i) answer" – correct triangle                    | M1             |          | Condone "difference" if $\Delta > \int$   |
|             | $\Rightarrow$ shaded area = $18\frac{9}{10}$                              | A1             | 3        | CSO; OE (18.9 etc)  |
|             | Total   |                | 11       |   |
| <b>6(a)</b> | Remainder = $p(1) = 1 + 1 - 8 - 12$                                       | M1             |          | Use of p(1) NOT long division   |
|             | = -18   | A1             | 2        |   |
| (b)(i)      | p(-2) = -8 + 4 + 16 - 12  | M1             |          | NOT long division   |
| (0)(1)      | $p(-2) = -6 + 4 + 16 - 12$ $= 0 \Rightarrow (x+2) \text{ is factor}$      | A1             | 2        | p(-2) shown = 0 <b>and</b> statement  |
|             | $-0 \rightarrow (x+2)$ is factor  | AI             | <i>L</i> | p(2) shown = 0 and statement  |
| (ii)        | Quad factor by comparing coefficients or $(x^2 + kx \pm 6)$ by inspection | M1             |          | Or full long division or attempt at Factor Theorem using f (±3)                             |
|             | $p(x) = (x+2)(x^2 - x - 6)$   | A1             |          | Correct quadratic factor or $(x-3)$ shown to be factor by Factor Theorem                    |
|             | $p(x) = (x+2)^2(x-3)$ or $(x+2)(x+2)(x-3)$                                | A1             | 3        | CSO; SC: B1 for $(x+2)(x^{***})(x-3)$ by inspection or without working                      |
| (c)(i)      | (k =) -12   | B1             | 1        | Condone $y = -12$ or $(0, -12)$   |
| (ii)        | <b>∆</b> y  | M1             |          | Cubic shape (one max and one min)   |
|             |   | A1             |          | Maximum at $(-2,0)$ and through $(3,0)$ – at least one of these values marked               |
|             | -2 $3/x$  | A1             | 3        | "correct" graph as shown (touching smoothly at –2, 3 marked and minimum to right of y-axis) |
|             | Total   |                | 11       |   |
|             |   |                |          |   |

MPC1 (cont)

| MPC1 (cont | Solution   | Marks    | Total | Comments  |
|------------|--|----------|-------|---|
| 7(a)       | $(x-8)^2 + (y-13)^2$   | B1       | 10001 | Exactly this with + and squares   |
| , ,        | $=13^{2}$  | B1       | 2     | Condone 169   |
| (b)(i)     | $\operatorname{grad} PC = \frac{12}{5}$                      | B1       | 1     | Must simplify $\frac{-12}{-5}$  |
| (ii)       | grad of tangent $=\frac{-1}{\text{grad }PC} = -\frac{5}{12}$ | B1√      |       | Condone $-\frac{1}{2.4}$ etc  |
|            | tangent has equation $y-1 = -\frac{5}{12}(x-3)$              | M1<br>A1 |       | ft gradient but M0 if using grad <i>PC</i> Correct – but not in required final form |
|            | 5x + 12y = 27 OE   | A1       | 4     | MUST have integer coefficients  |
| (iii)      | half chord = 5   | B1       |       | Seen or stated  |
|            | $D = \frac{13}{5} Q  \text{(provided } r > 5)$               | M1       |       | Pythagoras used correctly $d^2 = 13^2 - 5^2$  |
|            | Distance = 12  | A1       | 3     | CSO   |
| 2()        | Total  |          | 10    |   |
| 8(a)       | $b^2 - 4ac = 16k^2 - 36(k+1)$                                | M1       |       | Condone one slip  |
|            | Real roots: discriminant ≥ 0                                 | B1       |       |   |
|            | $\Rightarrow 16k^2 - 36k - 36 \geqslant 0$                   |          |       |   |
|            | $\Rightarrow 4k^2 - 9k - 9 \geqslant 0$                      | A1       | 3     | AG (watch signs)  |
| (b)        | (4k+3)(k-3)  | M1       |       | Or correct use of formula (unsimplified)  |
|            | critical points $(k =) -\frac{3}{4}, 3$                      | A1       |       | Not in a form involving surds Values may be seen in inequalities etc                |
|            | $\frac{3}{4}$ sketch   | M1       |       | Or sign diagram   |
|            | $k \geqslant 3,  k \leqslant -\frac{3}{4}$                   | A1       | 4     | NMS full marks  |
|            |  |          |       | Condone use of word "and" but final   |
|            |  |          |       | answer in a form such as $3 \le k \le -\frac{3}{4}$                                 |
|            | m 4 1  |          | 7     | scores A0   |
|            | Total TOTAL  |          | 75    |   |
|            | IOTAL  |          | 13    |   |