

General Certificate of Education  
January 2008  
Advanced Level Examination



**MATHEMATICS**  
**Unit Mechanics 2A**

**MM2A/W**

Tuesday 15 January 2008 9.00 am to 10.15 am

**For this paper you must have:**

- an 8-page answer book
- the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed: 1 hour 15 minutes

**Instructions**

- Use blue or black ink or ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The *Examining Body* for this paper is AQA. The *Paper Reference* is MM2A/W.
- Answer **all** questions.
- Show all necessary working; otherwise marks for method may be lost.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Take  $g = 9.8 \text{ m s}^{-2}$ , unless stated otherwise.

**Information**

- The maximum mark for this paper is 60.
- The marks for questions are shown in brackets.
- Unit Mechanics 2A has a **written paper and coursework**.

**Advice**

- Unless stated otherwise, you may quote formulae, without proof, from the booklet.

---

Answer **all** questions.

---

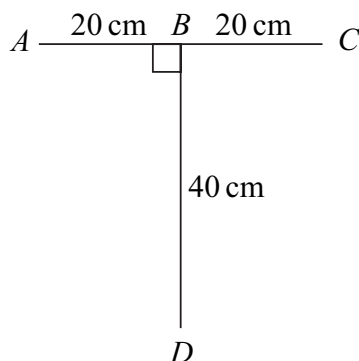
- 1** A ball is thrown vertically upwards from ground level with an initial speed of  $15 \text{ m s}^{-1}$ . The ball has a mass of  $0.6 \text{ kg}$ . Assume that the only force acting on the ball after it is thrown is its weight.
- (a) Calculate the initial kinetic energy of the ball. *(2 marks)*
  - (b) By using conservation of energy, find the maximum height above ground level reached by the ball. *(3 marks)*
  - (c) By using conservation of energy, find the kinetic energy and the speed of the ball when it is at a height of  $3 \text{ m}$  above ground level. *(4 marks)*

- 2** A particle moves in a horizontal plane under the action of a single force,  $\mathbf{F}$  newtons. The unit vectors  $\mathbf{i}$  and  $\mathbf{j}$  are directed east and north respectively. At time  $t$  seconds, the position vector,  $\mathbf{r}$  metres, of the particle is given by

$$\mathbf{r} = (t^3 - 3t^2 + 4)\mathbf{i} + (4t + t^2)\mathbf{j}$$

- (a) Find an expression for the velocity of the particle at time  $t$ . *(2 marks)*
- (b) The mass of the particle is  $3 \text{ kg}$ .
  - (i) Find an expression for  $\mathbf{F}$  at time  $t$ . *(3 marks)*
  - (ii) Find the magnitude of  $\mathbf{F}$  when  $t = 3$ . *(2 marks)*
- (c) Find the value of  $t$  when  $\mathbf{F}$  acts due north. *(2 marks)*

- 3 Two identical uniform rods,  $AC$  and  $BD$ , are rigidly joined together to form a letter  $\Gamma$ , as shown in the diagram. The two rods are perpendicular.



- (a) Explain why the centre of mass of the letter  $\Gamma$  lies on  $BD$ . (1 mark)
- (b) Find the distance of the centre of mass of the letter  $\Gamma$  from  $AC$ . (3 marks)
- (c) The letter  $\Gamma$  is freely suspended from  $A$ .

Find, to the nearest degree, the angle between  $AC$  and the horizontal when the letter  $\Gamma$  hangs in equilibrium. (3 marks)

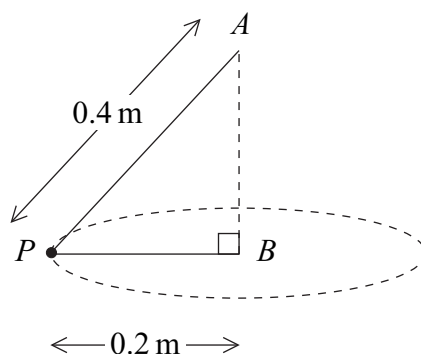
- 4 A light elastic string has natural length 6 metres and modulus of elasticity 300 newtons. It has one end attached to a fixed point,  $A$ , on a rough horizontal plane. The other end of the string is attached to a particle of mass 4 kilograms. The particle is pulled along the plane until it is 8 metres from the point  $A$ . The particle is then released from rest.

- (a) Calculate the elastic potential energy of the string when the particle is 8 metres from the point  $A$ . (2 marks)
- (b) The coefficient of friction between the particle and the plane is 0.3.

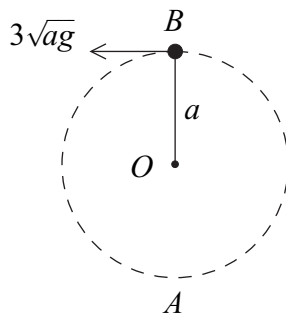
Show that the speed of the particle when the string becomes slack is  $6.18 \text{ m s}^{-1}$ , correct to three significant figures. (6 marks)

**Turn over for the next question**

- 5 Two light inextensible strings, of lengths 0.4 m and 0.2 m, each have one end attached to a particle,  $P$ , of mass 4 kg. The other ends of the strings are attached to the points  $A$  and  $B$  respectively. The point  $A$  is vertically above the point  $B$ . The particle moves in a horizontal circle, centre  $B$  and radius 0.2 m, at a speed of  $2 \text{ m s}^{-1}$ . The particle and strings are shown in the diagram.



- (a) Calculate the magnitude of the acceleration of the particle. (2 marks)
- (b) Show that the tension in string  $PA$  is 45.3 N, correct to three significant figures. (4 marks)
- (c) Find the tension in string  $PB$ . (3 marks)
- 6 A light inextensible string, of length  $a$ , has one end attached to a fixed point  $O$ . A particle, of mass  $m$ , is attached to the other end. The particle is moving in a vertical circle, centre  $O$ . When the particle is at  $B$ , vertically above  $O$ , the string is taut and the particle is moving with speed  $3\sqrt{ag}$ .



- (a) Find, in terms of  $g$  and  $a$ , the speed of the particle at the lowest point,  $A$ , of its path. (4 marks)
- (b) Find, in terms of  $g$  and  $m$ , the tension in the string when the particle is at  $A$ . (4 marks)

- 7 A car of mass 600 kg is driven along a straight horizontal road. The resistance to motion of the car is  $kv^2$  newtons, where  $v \text{ m s}^{-1}$  is the velocity of the car at time  $t$  seconds and  $k$  is a constant.

- (a) When the engine of the car has power 8 kW, show that the equation of motion of the car is

$$600 \frac{dv}{dt} - \frac{8000}{v} + kv^2 = 0 \quad (4 \text{ marks})$$

- (b) When the velocity of the car is  $20 \text{ m s}^{-1}$ , the engine is turned off.

- (i) Show that the equation of motion of the car now becomes

$$600 \frac{dv}{dt} = -kv^2 \quad (1 \text{ mark})$$

- (ii) Find, in terms of  $k$ , the time taken for the velocity of the car to drop to  $10 \text{ m s}^{-1}$ .  
(5 marks)

**END OF QUESTIONS**

**There are no questions printed on this page**

**There are no questions printed on this page**

**There are no questions printed on this page**