AQA

ASSESSMENT and
QUALIFICATIONS
ALLIANCE

General Certificate of Education

Mathematics 6360

MM1B Mechanics 1B

Mark Scheme

2006 examination – January series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Key To Mark Scheme And Abbreviations Used In Marking

M	mark is for method
m or dM	mark is dependent on one or more M marks and is for method
A	mark is dependent on M or m marks and is for accuracy
B	mark is independent of M or m marks and is for method and accuracy
E	mark is for explanation

√or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
–x EE	deduct x marks for each error	G	graph
NMS	no method shown	c	candidate
PI	possibly implied	sf	significant figure(s)
SCA	substantially correct approach	dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.
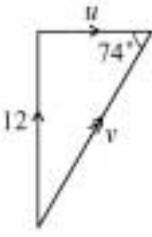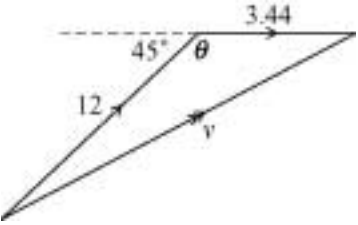
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.
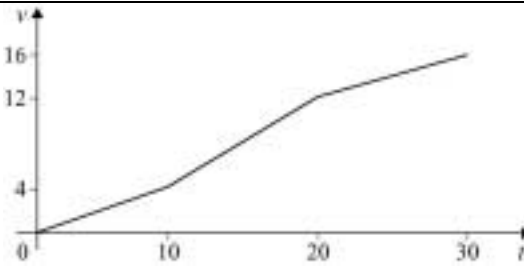
MM1B

Q	Solution	Marks	Total	Comments
1(a)	$\rightarrow 6\text{ms}^{-1}$ 2 kg ◯ ◯ 3 kg $\rightarrow v$ $2 \times 6 \quad = \quad 3 \times v$ $\underline{v = 4\,\text{ms}^{-1}}$	M1 A1 A1	 3	
(b)	$\rightarrow 6\text{ms}^{-1}$ 2 kg ◯ ◯ 3 kg $\leftarrow v \qquad \rightarrow 4v$ $2 \times 6 \quad = \quad -2 \times v + 3 \times 4v$ $12 = 10v$ $\underline{v = 1.2\,\text{ms}^{-1}}$	M1 A1 A1$\checkmark$	 3	all terms $\checkmark$sign error $(v = 0.857)$
	Total		**6**	
2(a)	$\mathbf{v} = 4\mathbf{i} + (-3\mathbf{i} + 12\mathbf{j})t$	M1 A1	2	use of $\mathbf{v} = \mathbf{u} + \mathbf{a}t$
(b)	$t = 0.5, \quad \mathbf{v} = 2.5\mathbf{i} + 6\mathbf{j}$ $\text{Speed} = \sqrt{(2.5^2 + 6^2)}$ $\text{Speed} = 6.5\,\text{ms}^{-1}$	B1$\checkmark$ M1 A1$\checkmark$	 3	$\checkmark$ 2 terms and t subs 2 terms $\checkmark$ 2 terms
	Total		**5**	
3(a)(i)	$s = ut + \dfrac{1}{2}at^2$ $25 = 0 + 4.9t^2$ $t = 2.26\,\text{sec} \quad (2.236)(\text{if } g = 10)$ (2.259)	 M1 A1	 2	full method
(ii)	$v^2 = u^2 + 2as$ $v^2 = 0 + 2 \times 9.8 \times 25$ $v = 22.1\,\text{ms}^{-1} \quad (21.913)$ (22.14)	 M1 A1	 2	
(b)	(Time longer) air resistance slows down motion, links with motion, no contradictions	M1 A1	2	(or Time less) package large so less distance to travel
	Total		**6**	

MM1B (cont)

Q	Solution	Marks	Total	Comments
4(a)(i)	$v = 12.5$ (12.48)	M1		$\dfrac{12}{\sin \text{ or } \cos \text{ of } 74° \text{ or } 16°}$
		A1	2	or Pythagoras with 3.44 **SC** if Pythagoras used in circular solution M1 (1$^{\text{st}}$ use) A1 A1 each answer (3 max)
(ii)	$\tan 74° = \dfrac{12}{u}$ $u = 3.44$	M1A1F A1	3	$\sqrt{\ }$incorrect v if used cao
(b)	 $\theta = 135°$ $v^2 = 3.44^2 + 12^2 - 2 \times 12 \times 3.44 \cos 135°$ $v = 14.6$	B1 M1 A1$\sqrt{\ }$ A1$\sqrt{\ }$	4	Alt: 12 cos or sin 45° B1 Full method $v^2 = (12 \sin 45)^2 + (3.44 + 12 \sin 45)^2$ M1 (8.485) (11.925) A1 14.6 A1 subs all correct $\sqrt{\ }$ incorrect subtraction $\rightarrow 135°$
	Total		**9**	
5(a)	$s = ut + \dfrac{1}{2} at^2$ $0 = 2\dfrac{1}{2} ut - \dfrac{1}{2} gt^2$ $0 = t\left(2\dfrac{1}{2}u - \dfrac{1}{2} gt \right)$ $t = \dfrac{5u}{g}$	 M1 A1 m1 A1	4	full method required for time (equation of motion, or standard result) (if $g = 9.8$ used, lose last A1)
(b)	$OA = 6u \times \dfrac{5u}{g}$ $= \dfrac{30u^2}{g}$	M1 A1	2	cao
(c)	$\text{speed}^2 = (6u)^2 + \left(2\dfrac{1}{2}u \right)^2$ $\text{speed} = 6\dfrac{1}{2}u$	M1 A1	2	cao
(d)	Least speed, at top, $= 6u$	B1	1	
	Total		**9**	

MM1B (cont)

Q	Solution	Marks	Total	Comments
6(a)(i)		B1 B1 B1	3	3 straight lines correct end points sensible scales + labelled *v/t*
(ii)	$s = \frac{1}{2} \times 10 \times 4 + \frac{1}{2} \times (4+12) \times 10 +$ $\frac{1}{2}(12+16) \times 10$ $s = 240$ metres	M1 m1 A1 A1√	4	area attempt Or full method equation attempted equation correct full method all correct √ one slip √ one slip
(iii)	Average speed $= \dfrac{240}{30}$ $= 8\,\text{ms}^{-1}$	M1 A1√	2	√distance
(iv)	Greatest acceleration $= 2^{\text{nd}}$ stage $= \dfrac{12-4}{10}$ $= 0.8\,\text{ms}^2$	M1 A1	2	cao
(b)(i)	Less area below curve < area below line/velocity lower	B1 B1	2	no additional incorrect statements
(ii)	Change in velocity more gradual oe	B1	1	
	Total		**14**	

MM1B (cont)

Q	Solution	Marks	Total	Comments
7(a)(i)	$T = 0.6 \times 9.8 = 5.88N$ Or $0.6g$	B1	1	
(ii)	Force $= 2T = \downarrow 11.76N$ Or 11.8 N	B1		Magnitude
	Or $1.2g$	B1	2	Direction
(b)(i)	$Q : 0.8g - T = 0.8a$	M1		Either equation
		A1		
	$T - 0.6g = 0.6a$	A1		
	$0.2g = 1.4a$	m1		Alternative for m1 A1 if solving for T
	$a = 1.4$	A1		m1 method for solving, A1 accurate attempt
	$T = 6.72N$	A1	6	cao $\quad$ SC whole string to find a :$0.2g = 1.4a$ M1 $a = 1.4$ A1
(ii)	Force $= 2T = 13.44N$	B1	1	cao $\quad$ to find T :M1 A1
	Total		**10**	
8(a)(i)	$R = 80\cos 25°$	M1		component attempted
		A1		correct component
	$R = 72.5N$	A1	3	cao
(ii)	$F = 0.32 \times 72.5$	M1		condone inequality
	$F = 23.2N$	A1	2	cao
(iii)	$T + F = 80\cos 65°$	M2		3 forces direction correct, component attempted
		A1		component
	$T = 10.6N$	A1√	4	√ friction
(iv)	$T = F + 80\cos 65°$	M1		3 forces, direction correct, component attempted
		A1		component
	$T = 57.0N$ (57N)	A1√	3	√ friction
(iv)	Mass $= \dfrac{80}{g} = (8.16\text{kg})$	B1	1	
(b)	$80\cos 65° - F = \text{mass} \times \text{acceleration}$	M1		3 terms, component attempted
	$10.6 = \dfrac{80}{g} \times \text{acc}$	A1		all correct
	$\text{acc} = 1.30\,\text{ms}^{-2}$ $\left(1.3\,\text{ms}^{-2}\right)$	A1	3	cao
	Total		**16**	
	Total		**75**	