

General Certificate of Education

Mathematics 6360

MM1A Mechanics 1A

Mark Scheme

2006 examination – June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Key To Mark Scheme And Abbreviations Used In Marking

M	mark is for method		
m or dM	mark is dependent on one or more M marks and is for method		
A	mark is dependent on M or m marks and is for accuracy		
B	mark is independent of M or m marks and is for method and accuracy		
E	mark is for explanation		
√ or ft or F	follow through from previous incorrect result	MC	mis-copy
CAO	correct answer only	MR	mis-read
CSO	correct solution only	RA	required accuracy
AWFW	anything which falls within	FW	further work
AWRT	anything which rounds to	ISW	ignore subsequent work
ACF	any correct form	FIW	from incorrect work
AG	answer given	BOD	given benefit of doubt
SC	special case	WR	work replaced by candidate
OE	or equivalent	FB	formulae book
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme
-x EE	deduct x marks for each error	G	graph
NMS	no method shown	c	candidate
PI	possibly implied	sf	significant figure(s)
SCA	substantially correct approach	dp	decimal place(s)

No Method Shown

Where the question specifically requires a particular method to be used, we must usually see evidence of use of this method for any marks to be awarded. However, there are situations in some units where part marks would be appropriate, particularly when similar techniques are involved. Your Principal Examiner will alert you to these and details will be provided on the mark scheme.

Where the answer can be reasonably obtained without showing working and it is very unlikely that the correct answer can be obtained by using an incorrect method, we must award **full marks**. However, the obvious penalty to candidates showing no working is that incorrect answers, however close, earn **no marks**.

Where a question asks the candidate to state or write down a result, no method need be shown for full marks.

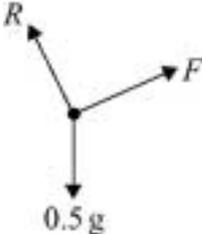
Where the permitted calculator has functions which reasonably allow the solution of the question directly, the correct answer without working earns **full marks**, unless it is given to less than the degree of accuracy accepted in the mark scheme, when it gains **no marks**.

Otherwise we require evidence of a correct method for any marks to be awarded.

MM1A

Q	Solution	Marks	Total	Comments
1(a)	$s = 0 + \frac{1}{2} \times 9.8 \times 4^2$	M1	3	full method correct subs, accept ± 9.8 CAO (need positive)
	$s = 78.4$ metres	A1		
(b)	$v = 0 + 9.8 \times 4$	M1	2	full method CAO (need positive)
	$v = 39.2 \text{ ms}^{-1}$	A1		
Total			5	
2(a)	$v = u + at$	M1	2	Full method with u, v used correctly, Accept ± 0.8 CAO, (correct substitution and answer)
	$0 = 10 + (-0.8) \times t$			
(b)	$t = 12.5$ sec	A1	4	} each line, straight and correct end points } SC first error in times lose B1, subsequent repeated errors, no further penalty SC B1 for 3 lines giving correct shape but no values shown axes labelled, v, t
		B1 B1 B1		
(c)	distance = $\frac{1}{2} \times 10 \times (4 + 22.5)$	M1	3	full correct method (including addition of distances) correct subs, ft graph if final $t = 12.5$
	= 132.5 metres	A1F		
Total			9	

MM1A (cont)

Q	Solution	Marks	Total	Comments
3(a)		B1	1	Accept W or mg (or 4.9) for weight Arrows and labels needed Can replace W with 2 correct components
(b)	$F = 0.5g \sin 16^\circ$ $F = 1.35 \text{ N}$	M1 A1 A1	3	component of <i>weight</i> attempted All correct including signs CAO
(c)	$R = 0.5g \cos 16^\circ$ $R = 4.71 \text{ N}$	M1 A1	2	component of <i>weight</i> attempted CAO (b) and (c): For resolving horizontal/vertical M1 for each equation, A1 one equation correct F A1 R A1
(d)	$F \leq \mu R$ $1.35 \leq \mu \times 4.71$ $\mu \geq 0.287$	M1 A1	2	Use of candidate's R , accept equals sign CAO inequality required
Total			8	
4(a)	$0.3g - T = 0.3a$ $T - 0.2g = 0.2a$ $a = 1.96 \text{ ms}^{-2}$	M1A1 M1A1 A1	5	Consistent reversal of signs in both equations 4 marks; Reversal of signs in one equation, M1 A1 M1 A0 Sign change needs justification (Whole string: Equation, $0.3g - 0.2g = 0.5a$ M1A1, $a = 1.96$ A1) max 3/5
(b)	$0.1g - R = 0.1 \times 1.96$ $R = 0.784 \text{ N}$	M1 A1 A1F	3	all terms all correct ft provided R positive
Total			8	

MM1A (cont)

Q	Solution	Marks	Total	Comments
5(a)	$\mathbf{d} = 3\mathbf{i} - 6\mathbf{j}$	B1	3	Accept $\pm \mathbf{d}$ or displacements of 3, 6 shown on a diagram
	$3\mathbf{i} - 6\mathbf{j} = (\mathbf{i} - 2\mathbf{j})t$	M1		Or equivalent method for t
	$t = 3$	A1		Accept ratio of vectors leading directly to ± 3 CAO
(b)(i)	$\mathbf{r} = (\mathbf{i} - 2\mathbf{j}) \times 4 + \frac{1}{2} \times 2\mathbf{j} \times 16$	M1	4	full method for vector expression giving change in position for correct subs (gives $4\mathbf{i} + 8\mathbf{j}$) ft slip provided obtain vector expression ($\mathbf{u} = 0$ gives $6\mathbf{i} + 12\mathbf{j}$)
	$+6\mathbf{i} - 4\mathbf{j}$	A1		
	$= 10\mathbf{i} + 4\mathbf{j}$	M1		
		A1F		
(ii)	$A(3,2) \quad C(10,4)$		2	Attempt to find vector \mathbf{AC} or \mathbf{CA} (using candidate's C) ft \mathbf{d} provided two non-zero components Accept $\sqrt{53}$
	$\mathbf{d} = 7\mathbf{i} + 2\mathbf{j}$	M1		
	$ \mathbf{d} = \sqrt{7^2 + 2^2}$ $AC = \sqrt{53} = 7.28$	A1F		
	Total		9	

MM1A (cont)

Q	Solution	Marks	Total	Comments
6(a)	$57 = 24 \cos 40^\circ \times t$	M1 A1	3	component attempted and accel'n = 0 all correct CAO
	$t = 3.10 \text{ sec}$	A1		
6(b)	$h = 24 \sin 40^\circ \times 3.1 - \frac{1}{2} \times 9.8 \times 3.1^2$	M1 A1	3	component attempted & accel'n = 9.8 all correct ft one slip eg + 9.8 used Accept 2 SF answer, AWRT 0.71-0.74
	$h = 0.734 \text{ m}$	A1F		
6(c)(i)	horizontal, $u = 24 \cos 40^\circ = 18.39 \text{ ms}^{-1}$	B1	5	Seen anywhere in (c), accept 18.4 component attempted & accel'n = 9.8 (accept -15.0) Use of candidate's u and 'new' v ft use of candidate's u and v
	vertical, $v = 24 \sin 40^\circ - 9.8 \times 3.1$	M1		
	$v = -14.95 \text{ ms}^{-1}$	A1		
	$V = \sqrt{(18.39^2 + (-14.95)^2)}$	M1		
	$V = 23.7 \text{ ms}^{-1}$	A1F		
6(ii)	$\tan \theta = \frac{14.95}{18.39}$	M1	2	Use of candidate's u and v (new) Accept inverted ratio ft use of candidate's u and v and V
	$\theta = 39.1^\circ \text{ or } 39.2^\circ, 140.8^\circ, 140.9^\circ \text{ accept } \pm$	A1		
Total			13	
7(a)	$m(5\mathbf{i} - 3\mathbf{j}) + 0.2(2\mathbf{i} + 3\mathbf{j})$	M1 A1	2	Momentum terms added All correct
7(b)(i)	$(0.2 + m)(k\mathbf{i} + \mathbf{j})$	B1	3	Seen, or used to find m Used with candidate's expressions in 2D equation or used to give one of the 1D equations below <i>Full</i> verification accepted CAO
	use of conservation of momentum	M1		
	$-3m + 0.6 = 0.2 + m$ $m = 0.1$	A1		
7(ii)	$5m + 0.4 = 0.2k + mk$	A1	3	
	substitute m	m1		
	$k = 3$	A1		
Total			8	
TOTAL			60	