General Certificate of Education June 2009 Advanced Level Examination



AQA

MM03

Wednesday 17 June 2009 9.00 am to 10.30 am

For this paper you must have:

• a 12-page answer book

• the blue AQA booklet of formulae and statistical tables.

You may use a graphics calculator.

Time allowed: 1 hour 30 minutes

Instructions

- Use black ink or black ball-point pen. Pencil should only be used for drawing.
- Write the information required on the front of your answer book. The *Examining Body* for this paper is AQA. The *Paper Reference* is MM03.
- Answer all questions.
- Show all necessary working; otherwise marks for method may be lost.
- The **final** answer to questions requiring the use of calculators should be given to three significant figures, unless stated otherwise.
- Take $g = 9.8 \text{ m s}^{-2}$, unless stated otherwise.

Information

- The maximum mark for this paper is 75.
- The marks for questions are shown in brackets.

Advice

• Unless stated otherwise, you may quote formulae, without proof, from the booklet.

Answer all questions.

1 A ball of mass m is travelling vertically downwards with speed u when it hits a horizontal floor. The ball bounces vertically upwards to a height h.

It is thought that h depends on m, u, the acceleration due to gravity g, and a dimensionless constant k, such that

$$h = km^{\alpha}u^{\beta}g^{\gamma}$$

where α , β and γ are constants.

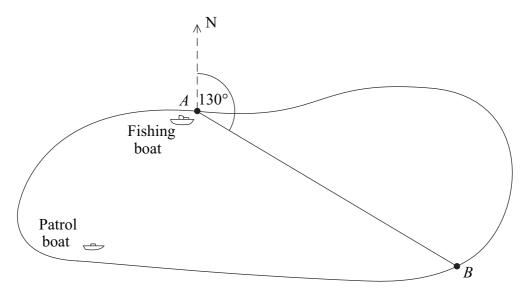
By using dimensional analysis, find the values of α , β and γ . (5 marks)

- 2 A particle is projected from a point O on a horizontal plane and has initial velocity components of 2 m s^{-1} and 10 m s^{-1} parallel to and perpendicular to the plane respectively. At time *t* seconds after projection, the horizontal and upward vertical distances of the particle from the point O are *x* metres and *y* metres respectively.
 - (a) Show that *x* and *y* satisfy the equation

$$y = -\frac{g}{8}x^2 + 5x \tag{4 marks}$$

- (b) By using the equation in part (a), find the horizontal distance travelled by the particle whilst it is more than 1 metre above the plane. (4 marks)
- (c) Hence find the time for which the particle is more than 1 metre above the plane.

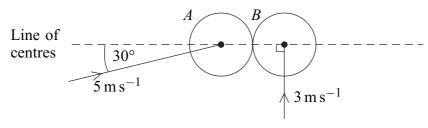
(2 marks)



- (a) Find the velocity of the fishing boat relative to the patrol boat, giving your answer as a speed together with a bearing. (5 marks)
- (b) When the patrol boat is 1500 m due west of the fishing boat, it changes direction in order to intercept the fishing boat in the shortest possible time.
 - (i) Find the bearing on which the patrol boat should travel in order to intercept the fishing boat. (4 marks)
 - (ii) Given that the patrol boat intercepts the fishing boat before it reaches *B*, find the time, in seconds, that it takes the patrol boat to intercept the fishing boat after changing direction. (4 marks)
 - (iii) State a modelling assumption necessary for answering this question, other than the boats being particles. (1 mark)
- 4 A particle of mass 0.5 kg is initially at rest. The particle then moves in a straight line under the action of a single force. This force acts in a constant direction and has magnitude $(t^3 + t)$ N, where t is the time, in seconds, for which the force has been acting.
 - (a) Find the magnitude of the impulse exerted by the force on the particle between the times t = 0 and t = 4. (3 marks)
 - (b) Hence find the speed of the particle when t = 4. (2 marks)
 - (c) Find the time taken for the particle to reach a speed of 12 m s^{-1} . (5 marks)

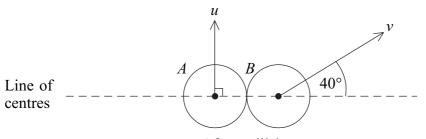
5 Two smooth spheres, *A* and *B*, of equal radii and different masses are moving on a smooth horizontal surface when they collide.

Just before the collision, A is moving with speed 5 m s^{-1} at an angle of 30° to the line of centres of the spheres, and B is moving with speed 3 m s^{-1} perpendicular to the line of centres, as shown in the diagram below.



Before collision

Immediately after the collision, A and B move with speeds u and v in directions which make angles of 90° and 40° respectively with the line of centres, as shown in the diagram below.

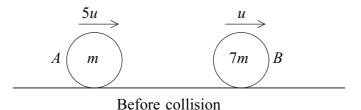


After collision

- (a) Show that $v = 4.67 \,\mathrm{m \, s^{-1}}$, correct to three significant figures. (3 marks)
- (b) Find the coefficient of restitution between the spheres. (3 marks)
- (c) Given that the mass of A is 0.5 kg, show that the magnitude of the impulse exerted on A during the collision is 2.17 Ns, correct to three significant figures. (3 marks)
- (d) Find the mass of *B*.

(3 marks)

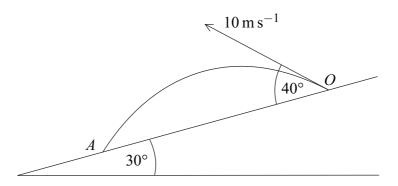
6 A smooth sphere A of mass m is moving with speed 5u in a straight line on a smooth horizontal table. The sphere A collides directly with a smooth sphere B of mass 7m, having the same radius as A and moving with speed u in the same direction as A. The coefficient of restitution between A and B is e.



- (a) Show that the speed of *B* after the collision is $\frac{u}{2}(e+3)$. (5 marks)
- (b) Given that the direction of motion of A is reversed by the collision, show that $e > \frac{3}{7}$. (4 marks)
- (c) Subsequently, *B* hits a wall fixed at right angles to the direction of motion of *A* and *B*. The coefficient of restitution between *B* and the wall is $\frac{1}{2}$. Given that after *B* rebounds from the wall both spheres move in the same direction and collide again, show also that $e < \frac{9}{13}$. (4 marks)

Turn over for the next question

7 A particle is projected from a point O on a smooth plane which is inclined at 30° to the horizontal. The particle is projected down the plane with velocity 10 m s^{-1} at an angle of 40° above the plane and first strikes it at a point A. The motion of the particle is in a vertical plane containing a line of greatest slope of the inclined plane.



(a) Show that the time taken by the particle to travel from O to A is

$$\frac{20\sin 40^{\circ}}{g\cos 30^{\circ}} \qquad (3 marks)$$

- (b) Find the components of the velocity of the particle parallel to and perpendicular to the slope as it hits the slope at *A*. (4 marks)
- (c) The coefficient of restitution between the slope and the particle is 0.5. Find the speed of the particle as it rebounds from the slope. (4 marks)

END OF QUESTIONS

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