

## **General Certificate of Education**

# Mathematics 6360

MD02 Discrete 2

# Mark Scheme

### 2005 examination – June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

#### Key to mark scheme and abbreviations used in marking

M m or dM A B E	mark is for method mark is dependent on one or more M marks and is for method mark is dependent on M or m marks and is for accuracy mark is independent of M or m marks and is for method and accuracy mark is for explanation						
or ft or F	follow through from previous						
	incorrect result	MC	mis-copy				
CAO	correct answer only	MR	mis-read				
CSO	correct solution only RA required accuracy						
AWFW	anything which falls within FW further work						
AWRT	anything which rounds to	ISW	ignore subsequent work				
ACF	any correct form	FIW	from incorrect work				
AG	answer given	BOD	given benefit of doubt				
SC	special case	WR	work replaced by candidate				
OE	ŌE	FB	formulae book				
A2,1	2 or 1 (or 0) accuracy marks	NOS	not on scheme				
–x EE	deduct x marks for each error	G	graph				
NMS	no method shown	с	candidate				
PI	possibly implied	sf	significant figure(s)				
SCA	substantially correct approach	dp	decimal place(s)				

#### **Application of Mark Scheme**

No method shown:	
Correct answer without working	mark as in scheme
Incorrect answer without working	zero marks unless specified otherwise
More than one method / choice of solution:	
2 or more complete attempts, neither/none crossed out	mark both/all fully and award the mean mark rounded down
1 complete and 1 partial attempt, neither crossed out	award credit for the complete solution only
Crossed out work	do not mark unless it has not been replaced
Alternative solution using a correct or partially correct method	award method and accuracy marks as appropriate

MD02 Q			Solu	tion		Marks	Total	Comments
1(a)	Hung	arian alo		minimis	2es	E1	10041	
1(a)				of questi				
				ninimisi		E1	2	
	conce	t which	necus i	1111111151	ing	LI	2	
(b)	3	1	2	5	4			
(0)	0	2	5	1	3			
	7	3		4	6	B1		Arroy giving 20 x
	8	3 4	3 2	4 5	6	DI		Array giving 20– <i>x</i>
	8 6	4	2 5	3 4	5			
	0	4	3	4	5			
	2	0	1	4	3	M1		Reduce rows
	0	2	5	1	3			
	4	$ \frac{2}{0} $	0	1	3			
	6	2	0	3	4	A1√		ft their $20 - x$ matrix
	2		1	0	1	7 <b>1</b> 1 V		
	2	Ū	1	0	1			
	2	0	1	4	2	M1		Reduce columns
	0	2	5	1	2			
	4	0	0	1	2	A1		CSO
	6	2	0	3	3			
	2	0	1	0	0			or I
		can be justmen		with on	ly 4 lines	M1		
								or
	2	0	1	3	1			1 0 1 3 1
	0	2	5	0	1			$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
	4	0	0	0	1			
	6	2	0	2	2	A1		$\begin{array}{cccccccccccccccccccccccccccccccccccc$
	3	1	2	0	0			$ \begin{array}{cccccccccccccccccccccccccccccccccccc$
	Match	ning on j	particula	ar zeros		M1		If adjustment not done correctly and
		- ·						selection is made
	Les- 7							3 correct matchings B1
		Athletic						rest correct B1
		Swimm						
		Footba	11					Award marks here in whichever way
	Pete-	Golf				A1	9	benefits candidate most.
	ļ				Total		11	
					TUTAL		11	

#### **MD02**

<b>MD02</b>	(cont)
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Q			Solut		Marks	Total	Comments
<b>2(a)</b>				ay journey of T max day journey	M1		Reasonable understanding
	is 10 h	rs			A1	2	with 9 and 10 specifically mentioned
(b)	Stage		Actio	n Value	M1		General idea of stage and state
	1	State D	DT	5*			
		Ε	ET	7*	A1		First stage correct ( may be reversed)
	2	A	AD AE	max(10,5) = 10 max(9,7) = 9*	M1 A1		Idea of minimax One pair of actions correct
		В	BD AE	max(9,5) = 9 max(8,7) = 8*			
		С	CD CE	max(10,5) = 10 max(9,7) = 9*	A1		All values in second stage correct
	3	S	SB	max(7,9) = 9 max(8,8) = 8* max(9,10) = 10	A1		
		ng back		values to find	M1 A1	8	All values correct at all 3 stages
				-			Complete/enumeration or network with each stage and state carefully described if no evidence of minimax Maximum mark M1, A1
							Minimax route <i>SBET</i> marks may also be earned if not finding minimum time through the network. M1 A1
				Total		10	

MD02 (co		ſ							
Q 3	Solution	Marks	Total	Comments					
5	$\begin{array}{c} A \\ 0 & 6 \\ \hline \\ 0 & 6 \\ \hline \\ 6 & 13 \\ \hline \\ \\ B \\ 0 & 6 \\ \hline \\ \\ B \\ 0 & 6 \\ \hline \\ \\ B \\ 0 & 6 \\ \hline \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\ \\$								
(a)	Network	M1 A3	4	SCA -1 ee					
(b)	Forward pass All correct	M1 A1	2						
(c)	Backward pass All correct	M1 A1	2						
(d)(i)	Project completion time 36 hours	B1√	1						
(ii)	Critical path BCEGHJ	M1 A1		SCA All correct					
	Earliest start + activity duration = latest finish time	E1	3						
(e)(i)	<i>I</i> now has new earliest time 29+3	M1		Extra 3 hours on edge <i>HI</i> or new activity between <i>H</i> and <i>I</i> of duration 3					
	= 32	A1	2						
(ii)	I now becomes critical and increases $J$ earliest start time to 35	M1							
	New completion time is 37 hours	A1	2						
	Total		16						

MD02 (	Cont)
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Q	Solution	Marks	Total	Comments
<b>4(a)</b>	$4x + 5y \leqslant 36$	M1		SCA at LHS and RHS
	$2x + y \le 12$ $5x + 2y \le 35$	A1	2	All correct with correct inequalities
(b)(i)	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1		Identifying pivot and possibly dividing by 2
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	m1 A1		Row operations Correct tableau
	Next y pivot on 3	M1		
	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	m1 A1		Row operations Correct tableau
	Optimal since no negative numbers in top row	B1	7	
(ii)	P = 20 x = 4, y = 4	B1√ B1√	2	<b>FT</b> ONLY if no negs in top row
(iii)	r = 0,  s = 0,  t = 7 at optimum	B1√	1	
	Total		12	

#### MD02 (cont)

Q	Solution	Marks	Total	Comments
5(a)	$\begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1 A1		Either marginal row or column all values correct
	Since $3 \neq 4 \Rightarrow$ no stable solution	A1	3	
(b)	$P_1$ dominates $P_3$ ; (1,2,3) < (4,3,5)	E1	1	
	So it is unwise to play P <sub>3</sub>			
(c)	P chooses $P_1$ with probability $p$ So chooses $P_2$ with probability $1-p$			
	Expected gains when Q plays $Q_1: 4p - (1-p) = 5p - 1$	M1		Attempt at at least 2
	$Q_2: 3p +5 (1-p) = 5 - 2p Q_3: 5p -2 (1-p) = 7p - 2$	A1		All 3 correct (simplified)
	Plot expected gains against $p$ for $0 \le p \le 1$	M1		
	5 0 $1$ $p$	A1		
	Choose highest point of region below lines			
	5p - 1 = 5 - 2p	M1		
	leading to $p = \frac{6}{7}$	A1		
	Therefore P plays P <sub>1</sub> with probability $\frac{6}{7}$			
	and plays $P_2$ with probability $\frac{1}{7}$	<b>B</b> 1√	7	
	Total		11	

#### MD02 (cont)

Q	Solution	Marks	Total	Comments
6(a)(i)	9+7+0+9+13=38	B1	1	
(ii)	Maximum flow is less than or equal to 38	M1		< their value of cut
		A1√	2	≤38
				M0 for "equals" their cut
(b)		B1	2	
	<i>SXYZT</i> flow of 13	B1	2	
(c)(i)	Indicating flows from (b) on network	M1		Preferably as backward flows
	with a spin matter loading to sense thing such as			
	Route Flow			
	SUYWT 9			
	SXYZT 13			
	SUVWT 7			
	SXVZT 7			
	SXVWZT 1			
	Flow augmentation (many possibilities)			
	SUVWT 7	M1A1		
	SXVZT 7	m1A1		
	SXVWZT 1	A1	6	
	Network showing maximum flow			
(ii)	Several possibilities	B1		
		21		
	39 No No 16			
				Or $\{S, U, X \mid V, W, Y, Z, T\}$
	x x ii z	D1	2	(~, ~,, , , , , , , , , , , , , , , ,
	Maximum flow is 37	B1	2	
(iii)	Attempt to find out through saturated area	N # 1		
(III)	Attempt to find cut through saturated arcs Cut through UV, UY, XV, XY	M1 A1	2	
	-	AI		
	Total		15	
	Total		75	

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