## GCE 2004 November Series

ASSESSMENT and
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ALLIANCE

## Mark Scheme

## Mathematics and Statistics B MBS1

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## Key to Mark Scheme

| M | mark is for | method |
| :---: | :---: | :---: |
| m | mark is dependent on one or more M marks and is for | method |
| A | mark is dependent on M or m mark and is for | accuracy |
| B | mark is independent of M or m marks and is for | method and accuracy |
| E | mark is for | explanation |
| $\checkmark$ or ft |  | follow through from previous incorrect result |
| cao |  | correct answer only |
| cso |  | correct solution only |
| awfw |  | anything which falls within |
| awrt |  | anything which rounds to |
| acf |  | any correct form |
| ag |  | answer given |
| sc |  | special case |
| oe |  | or equivalent |
| sf |  | significant figure(s) |
| dp |  | decimal place(s) |
| A2,1 |  | 2 or 1 (or 0) accuracy marks |
| $-x$ ee |  | deduct $x$ marks for each error |
| PI |  | possibly implied |
| sca |  | substantially correct approach |

## Abbreviations used in Marking

| MC $-\boldsymbol{x}$ | deducted $x$ marks for mis-copy |
| :--- | :---: |
| MR $-\boldsymbol{x}$ | deducted $x$ marks for mis-read |
| isw | ignored subsequent working |
| bod | gave benefit of doubt |
| wr | work replaced by candidate |
| fb | formulae book |

## Application of Mark Scheme

## Correct answer without working Incorrect answer without working

## mark as in scheme zero marks unless specified otherwise

Award method and accuracy marks as appropriate to an alternative solution using a correct method or partially correct method.

## Mathematics and Statistics B Statistics 1 MBS1 November 2004

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 1(a)(i) <br> (ii) <br> (b) | $\begin{aligned} & 0.2600 \\ & P(14)=0.5704-0.4644=0.106 \\ & 1-0.8272=0.173 \end{aligned}$ | $\begin{aligned} & \hline \text { B1 } \\ & \text { M1 } \\ & \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \hline \end{aligned}$ |  | ```0.2600 ( 0.2595 to 0.2605 ) \(\mathrm{P}(14)=\mathrm{P}(14\) or fewer \()-\mathrm{P}(13\) or fewer \()\) or correct use of formula 0.106 ( 0.1055 to 0.1065 ) 1 - P(17 or fewer) 0.173 ( 0.172 to 0.173 )``` |
|  | Total |  | 5 |  |
| 2 | 1. probably incorrect (B) - would expect negative correlation coefficient <br> 2. Definitely incorrect (C) $-r$ cannot exceed 1 <br> 3. Plausible (A) - probably both related to population of town | $\begin{aligned} & \hline \text { B1 } \\ & \text { E1 } \\ & \text { B1 } \\ & \text { E1 } \\ & \text { B1 } \\ & \text { E1 } \end{aligned}$ | 6 | Probably incorrect <br> Negative expected <br> Definitely incorrect <br> Cannot exceed 1 <br> Plausible <br> Related to population of town |
|  | Total |  | 6 |  |
| 3(a) | Number students 000 to 409 | E1 |  | Valid numbering |
|  | Select 3 digit random numbers | E1 |  | Select 3-digit random numbers |
|  | Ignore repeats | E1 |  | Ignore repeats |
|  | Ignore > 409 | E1 |  | Ignore $>409$ consistent with their numbering |
|  | Continue until 20 obtained and choose corresponding students | E1 | 5 | 20 obtained/select corresponding students |
| (b)(i) | Incomes in 2003 of the 410 students | B1 |  | Incomes |
|  |  | B1 | 2 | 410 students |
| (ii) | Mean income of the sample of 20 students | B1 |  | Mean/s.d/... |
|  |  | B1 | 2 | Sample |
| (c) | Incomes of all mathematics graduates | B1 | 1 | Valid population; must mention incomes |
|  | Total |  | 10 |  |
| 4(a)(i) | $0.8 \times 0.7=0.56$ | B1 |  | 0.56 cao |
| (ii) | $0.2 \times 0.3=0.06$ | M1 |  | Method |
|  |  | A1 |  | 0.06 cao |
| (iii) | $0.8 \times 0.3+0.2 \times 0.7=0.38$ | M1 |  | Method - allow small slip |
|  | (or $1-0.56-0.06=0.38)$ | A1 | 5 | 0.38 cao |
| (b)(i) | $0.8 \times 0.7 \times 0.95=0.532$ | B1 |  | 0.532 cao |
| (ii) | $0.8 \times 0.3 \times 0.95+0.2 \times 0.7 \times 0.15 \ldots$ | M1 |  | Attempt at $\mathrm{P}(2)+\mathrm{P}(3)$ or equivalent |
|  | $\ldots+0.8 \times 0.7 \times 0.05+0.532=0.809$ | M1 |  | Reasonable attempt at evaluating $\mathrm{P}(2)$ (or $\mathrm{P}(1)$ if relevant) |
|  |  | $\begin{gathered} \text { m1 } \\ \text { A1 } \end{gathered}$ | 5 | Completely correct method $0.809 \text { cao }$ |
|  | Total |  | 10 |  |

## MBS1 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 5(a) | Question 1: suitable <br> Question 2: not suitable; classes not mutually exclusive <br> Question 3: not suitable; time is continuous | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \\ & \text { B1 } \\ & \text { M1 } \\ & \text { m1 } \\ & \text { B1 } \\ & \text { A1 } \end{aligned}$ | 5 | Suitable <br> Not suitable <br> Not mutually exclusive <br> Not suitable <br> Time continuous variable <br> (Maximum B1 M1 if no valid reasons ) <br> Choose question 3 <br> Method for frequency density <br> Method for histogram <br> Scales, labels, no gaps <br> Reasonably accurate plot, by eye <br> (No marks if questions 1 or 2 chosen) |
|  | Total |  | 10 |  |
| 6(a)(i) | $\left.\begin{array}{l} \text { Binomial } n=6 \quad p=0.5 \\ \mathrm{P}(\text { more than } 4)=1-0.8906 \\ \\ =0.109 \end{array}\right\} \begin{aligned} & \mathrm{P}(6)=1.0000-0.9844=0.0156 \end{aligned}$ <br> 14 out of $900=0.0156$ <br> It appears the proportion of unit trusts outperforming the stock market average over a six-year period is consistent with a random selection of investments | B1 <br> M1 <br> A1 <br> M1 <br> A1 <br> M1 <br> E1 $\checkmark$ <br> E1 | 3 2 | B(6, 0.5) <br> $\mathrm{P}($ more than 4$)=1-\mathrm{P}(4$ or fewer $)$ $0.109(0.109 \text { to } 0.11)$ <br> $\mathrm{P}(6)=1-\mathrm{P}(5$ or fewer $)$ or $\mathrm{P}(6$ or fewer $)-\mathrm{P}(5$ or fewer) or correct use of formula $0.0156 \text { ( } 0.015 \text { to } 0.016 \text { ) }$ <br> Appropriate calculation attempted <br> Conclusion consistent with their earlier results <br> Appropriate conclusion based on correct calculations |
|  | Total |  | 8 |  |

## MBS1 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 7(a)(i) | $z=\frac{75-85}{8}=-1.25$ | M1 |  | Method for $z$; ignore sign |
|  | $\begin{gathered} \mathrm{P}(<75)=1-0.89435 \\ =0.106 \end{gathered}$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 3 | A correct use of normal tables 0.106 ( 0.105 to 0.106 ) |
| (ii) | $z_{2}=\frac{81-85}{8}=-0.5$ | M1 |  | Completely correct method; allow both $z$ 's positive |
|  | Probability between 75 and 85 is $0.89435-0.69146=0.203$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ | 3 | Reasonable attempt, both $z$ 's negative 0.203 ( 0.202 to 0.204 ) |
| (b) | $85+3.0902 \times 8=110$ | B1 <br> M1 <br> m1 <br> A1 | 4 | $\begin{aligned} & 3.09 \text { or } 3.0902 \\ & \text { (their } z) \times 8 \\ & \text { Completely correct method } \\ & 110(109 \text { to } 110) \end{aligned}$ |
| (c)(i) | $z=\frac{81-85}{\frac{8}{\sqrt{4}}}=-1$ | M1 |  | Use of $\frac{8}{\sqrt{4}}$ |
|  | Probability mean less than 81 $=1-0.84134=0.159$ | m1 |  | Completely correct method |
|  |  | A1 | 4 | 0.159 (0.158 to 0.16) |
| (ii) | $1-0.69146=0.309$ | M1 <br> A1 | 2 | Attempt to calculate probability flight time less than 81 minutes 0.309 ( 0.308 to 0.31 ) |
|  | Total |  | 16 |  |
| 8(a)(b) | (see graph on next page) | M1 |  | Method for scatter diagram |
|  |  | A1 | 2 | Reasonably accurate plot by eye, allow one small slip, disallow for joined up points |
|  | $y=-81.4+5.50 x$ | B2 |  | -81.4 ( -81.35 to -81.45), allow M1A1 |
|  |  | B2 |  | 5.50 (5.49 to 5.51), allow M1A1 |
|  | $x=20 \quad y=28.6 \quad x=60 \quad y=248.7$ | M1 |  | Method for line |
|  |  | A1 | 6 | Accurate line |
| (c)(i)(ii) | $\begin{aligned} 147-(-81.4)-5.50 \times 45 & =-19.2 \\ 298-(-81.4)-5.50 \times 65 & =21.8 \end{aligned}$ | M1 |  | Method - ignore sign, allow read from graph |
|  |  | m1 |  | Consistent signs or both correct ignoring signs |
|  |  | A1 | 3 | -19.2 (-19 to -19.4) and 21.8 (21.6 to 22) |
| (d)(i) | 260 | B1 | 1 | 260 (259 to 260) |
| (ii) | Both graph and residuals suggests that in this region the actual time will exceed time predicted by regression equation | E1 | 1 | Reason |
| (e) | Appropriate regression equation would be $x=a+b y$ since number of step-ups now depends on time | $\begin{aligned} & \text { E1 } \\ & \text { E1 } \end{aligned}$ | 2 | $x=a+b y$ <br> Reason |
|  | Total |  | 15 |  |
|  | TOTAL |  | 80 |  |

## MBS1 (cont)

## Graph for Question 8 (a) and (b)



