# AQA 

ASSESSMENT and
OUALIFICATIONS
ALLIANCE

## General Certificate of Education

# Mathematics and Statistics 6320 Specification B 

MBP7 Pure 7

## Mark Scheme <br> 2005 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

## Key to Mark Scheme

| M | mark is for | method |
| :---: | :---: | :---: |
| m | mark is dependent on one or more M marks and is for | method |
| A | mark is dependent on M or m marks and is for | accuracy |
| B | mark is independent of M or m marks and is for | accuracy |
| E | mark is for | explanation |
| $\checkmark$ or ft or F |  | follow through from previous incorrect result |
| cao |  | correct answer only |
| cso |  | correct solution only |
| awfw |  | anything which falls within |
| awrt |  | anything which rounds to |
| acf |  | any correct form |
| ag |  | answer given |
| sc |  | special case |
| oe |  | or equivalent |
| sf |  | significant figure(s) |
| dp |  | decimal place(s) |
| A2,1 |  | 2 or 1 (or 0 ) accuracy marks |
| $-x$ ee |  | deduct $x$ marks for each error |
| pi |  | possibly implied |
| sca |  | substantially correct approach |

## Abbreviations used in Marking

MC $-\boldsymbol{x}$
MR $-\boldsymbol{x}$
isw
bod
wr
fb
deducted $x$ marks for mis-copy deducted $x$ marks for mis-read ignored subsequent working given benefit of doubt work replaced by candidate formulae book

## Application of Mark Scheme

## No method shown:

Correct answer without working
Incorrect answer without working
More than one method / choice of solution:
2 or more complete attempts, neither/none crossed out
1 complete and 1 partial attempt, neither crossed out
Crossed out work
Alternative solution using a correct or partially correct method
mark as in scheme
zero marks unless specified otherwise
mark both/all fully and award the mean mark rounded down
award credit for the complete solution only
do not mark unless it has not been replaced
award method and accuracy marks as appropriate

## Mathematics and Statistics B Pure 7 MBP7 June 2005




MBP7 (cont)

| Q | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 5(a) | Evaluating $\left\|\begin{array}{ccc}1 & -1 & 2 \\ 2 & 1 & 3 \\ 4 & 35 & -5\end{array}\right\|$ $=(-5+140-12)-(8+105+10)=0$ <br> ALTERNATIVE: $\left[\begin{array}{ccc\|c} 1 & -1 & 2 & 26 \\ 2 & 1 & 3 & 47 \\ 4 & 35 & -5 & 39 \end{array}\right]$ | M1 <br> A1 <br> (M1) | 2 | $\begin{aligned} \text { E.g. } R_{2}{ }^{*} & =R_{2}-2 R_{1} \\ R_{3}{ }^{*} & =R_{3}-4 R_{1} \end{aligned}$ |
|  | $\rightarrow\left[\begin{array}{ccc\|c} 1 & -1 & 2 & 26 \\ 0 & 3 & -1 & -5 \\ 0 & 39 & -13 & -65 \end{array}\right]$ | (A1) | (2) | N.B. Observing that $R_{3}{ }^{*}=13 R_{2}{ }^{*}$ now gives (a)'s result from here. Etc. |
| (b) | $\begin{aligned} & E_{2}{ }^{*}=E_{2}-2 E_{1} \Rightarrow 3 y-z=-5 \\ & \text { Setting (e.g.) } y=\lambda \\ & \quad \text { so that } z=3 \lambda+5 \text { and } x=16-5 \lambda \end{aligned}$ | $\begin{gathered} \text { M1 A1 } \\ \text { M1 } \\ \text { A1 A1 } \end{gathered}$ | 5 | N.B. Any method acceptable |
|  | $\text { OR: } \begin{aligned} x & =\lambda, y=\frac{16-\lambda}{5}, z=\frac{73-3 \lambda}{5} \\ z & =\lambda, x=\frac{\lambda-5}{3}, z=\frac{73-5 \lambda}{3} \end{aligned}$ |  |  | OR equivalent answers |
| (c) | The line of intersection of three planes | B1 | 1 |  |
|  | Total |  | 8 |  |
| 6(a) | $\left[\begin{array}{ll} 1 & a \\ 0 & 1 \end{array}\right]\left[\begin{array}{ll} 1 & b \\ 0 & 1 \end{array}\right]=\left[\begin{array}{cc} 1 & a+b \\ 0 & 1 \end{array}\right] \Rightarrow \text { Closed }$ | $\begin{gathered} \text { M1 } \\ \text { A1 } \end{gathered}$ |  |  |
|  | The identity, $\left[\begin{array}{ll}1 & 0 \\ 0 & 1\end{array}\right]$ is in $S$ $\left[\begin{array}{ll}1 & a \\ 0 & 1\end{array}\right]^{-1}=\left[\begin{array}{cc}1 & -a \\ 0 & 1\end{array}\right]=$ is in $S$ | B1 B1 | 4 |  |
| (b)(i) | $\left(S, \times_{\mathrm{M}}\right) \cong(\Re,+)$ | B1 |  |  |
|  | Isomorphism $\left[\begin{array}{ll}1 & a \\ 0 & 1\end{array}\right] \rightarrow a$ | B1 | 2 |  |
| (ii) | $\left(S, \times_{\mathrm{M}}\right) \text { not } \cong(\Re, \times)$ <br> Any good reason | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | 2 | E.g. $(\Re, \times)$ not a group or $\mathbf{A B}$ does not map to $a b$ |
|  | Total |  | 8 |  |

MBP7 (cont)

\begin{tabular}{|c|c|c|c|c|}
\hline Q \& Solution \& Marks \& Total \& Comments \\
\hline 7(a) \& \begin{tabular}{l}
(i) \(\ln \left(1+\frac{1}{3} \theta\right)=\frac{1}{3} \theta-\frac{1}{18} \theta^{2}+\ldots\) \\
Expansion valid for \(-3<\theta \leq 3\)
\[
\begin{aligned}
\& \text { (ii) } r \approx \frac{4}{9}+\frac{1}{3} \theta-\frac{1}{18} \theta^{2}+\ldots \\
\& \quad \Rightarrow \frac{\mathrm{d} r}{\mathrm{~d} \theta} \approx \frac{1}{3}-\frac{1}{9} \theta \\
\& \begin{aligned}
r^{2} \& +\left(\frac{\mathrm{d} r}{\mathrm{~d} \theta}\right)^{2} \\
\& \approx\left(\frac{16}{81}+2 \cdot \frac{4}{9} \cdot \frac{1}{3} \theta \ldots\right)+\left(\frac{1}{9}-2 \cdot \frac{1}{3} \cdot \frac{1}{9} \theta \ldots\right) \\
\& =\frac{1}{81}(25+18 \theta) \\
L \& =\int \frac{1}{9}(25+18 \theta)^{1 / 2} \mathrm{~d} \theta \\
\& =\frac{1}{243}(25+18 \theta)^{3 / 2} \\
= \& 0.251 \text { (to } 3 \text { d.p.) }
\end{aligned}
\end{aligned}
\]
\end{tabular} \& \begin{tabular}{l}
M1 A1 \\
B1 \\
B1」 \\
M1 \\
Al \(\sqrt{ }\) \\
A1 \\
B1 \\
M1 \\
A1 \\
A1
\end{tabular} \& 3
1
1
3

4 \& | ft |
| :--- |
| Attempt at both |
| ft either correct, unsimplified (relevant terms only) |
| Answer given |
| Correct power of $(25+18 \theta)$ |
| Correct multiple |
| Exactly this (but allow $\frac{61}{243}$ ) | <br>

\hline \& Total \& \& 11 \& <br>
\hline 8(a)

(b)(i)

(ii) \& \begin{tabular}{l}
$$
\frac{\mathrm{d} y}{\mathrm{~d} x}=\frac{\frac{1}{2} \cos \theta}{-2 \sin \theta}
$$ <br>
Eqn. tgt. is
$$
y-\frac{1}{2} \sin \theta=-\frac{\cos \theta}{-4 \sin \theta}(x-2 \cos \theta)
$$ <br>
$4 y \sin \theta-2 \sin ^{2} \theta=-x \cos \theta+2 \cos ^{2} \theta$ $\Rightarrow x \cos \theta+4 y \sin \theta=2$
$$
x^{2}=\frac{4-16 y \sin \theta+16 y^{2} \sin ^{2} \theta}{\cos ^{2} \theta}
$$ <br>
Use of $\mathrm{c}^{2}=1-\mathrm{s}^{2}$ at any stage <br>
Subst ${ }^{\text {g }}$. for $x$ into $x^{2}-9 y^{2}=9$
$$
\left(25 \mathrm{~s}^{2}-9\right) y^{2}-16 \mathrm{~s} y+\left(9 \mathrm{~s}^{2}-5\right)=0
$$ <br>
Considering the discriminant <br>
Equate to zero + attempt to solve
$$
\begin{aligned}
& \Rightarrow \quad 256 \mathrm{~s}^{2}=4\left(9 \mathrm{~s}^{2}-5\right)\left(25 \mathrm{~s}^{2}-9\right) \\
& \Rightarrow \quad 0=m\left(5 \mathrm{~s}^{4}-6 \mathrm{~s}^{2}+1\right) \\
& \left(5 \mathrm{~s}^{2}-1\right)\left(\mathrm{s}^{2}-1\right)=0 \\
& \Rightarrow \sin \theta= \pm \frac{1}{\sqrt{5}} \text { and } \pm 1
\end{aligned}
$$

 \& 

M1 A1 <br>
M1 <br>
A1 <br>
B1 <br>
B1 <br>
M1 <br>
A1 <br>
M1 <br>
m1 <br>
A1 <br>
A1 <br>
M1 <br>
A1
\end{tabular} \& 4

4

6 \& | Or $y=-\frac{\cos \theta}{-4 \sin \theta} \quad x+C$ with $\left(2 \cos \theta, \frac{1}{2} \sin \theta\right)$ substd. to find $C$ |
| :--- |
| Answer given |
| N.B. There is a quoteable form for the tgt. if the ellipse eqn. can be identified. This is fine. |
| Getting given answer legitimately |
| $\mathrm{Or} \equiv$ with factors cancelled |
| ft quadratic in $\mathrm{s}^{2}$ |
| cao | <br>

\hline \& Total \& \& 14 \& <br>
\hline \& TOTAL \& \& 60 \& <br>
\hline
\end{tabular}

