

# GCE 2004

## *June Series*



# Mark Scheme

## Mathematics and Statistics B

### *MBM5*

---

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.

Further copies of this Mark Scheme are available from:

Publications Department, Aldon House, 39, Heald Grove, Rusholme, Manchester, M14 4NA  
Tel: 0161 953 1170

or

download from the AQA website: [www.aqa.org.uk](http://www.aqa.org.uk)

Copyright © 2004 AQA and its licensors

#### COPYRIGHT

AQA retains the copyright on all its publications. However, registered centres for AQA are permitted to copy material from this booklet for their own internal use, with the following important exception: AQA cannot give permission to centres to photocopy any material that is acknowledged to a third party even for internal use within the centre.

Set and published by the Assessment and Qualifications Alliance.

The Assessment and Qualifications Alliance (AQA) is a company limited by guarantee registered in England and Wales 3644723 and a registered charity number 1073334. Registered address AQA, Devas Street, Manchester. M15 6EX.

*Dr Michael Cresswell Director General*

**Key to Mark Scheme**

<b>M</b>	mark is for	method
<b>m</b>	mark is dependent on one or more M marks and is for	method
<b>A</b>	mark is dependent on M or m marks and is for	accuracy
<b>B</b>	mark is independent of M or m marks and is for	accuracy
<b>E</b>	mark is for	explanation
<b>✓ or ft or F</b>		follow through from previous incorrect result
<b>cao</b>		correct answer only
<b>cso</b>		correct solution only
<b>awfw</b>		anything which falls within
<b>awrt</b>		anything which rounds to
<b>acf</b>		any correct form
<b>ag</b>		answer given
<b>sc</b>		special case
<b>oe</b>		or equivalent
<b>sf</b>		significant figure(s)
<b>dp</b>		decimal place(s)
<b>A2,1</b>		2 or 1 (or 0) accuracy marks
<b>-x ee</b>		deduct $x$ marks for each error
<b>pi</b>		possibly implied
<b>sca</b>		substantially correct approach

**Abbreviations used in Marking**

<b>MC – <math>x</math></b>	deducted $x$ marks for mis-copy
<b>MR – <math>x</math></b>	deducted $x$ marks for mis-read
<b>isw</b>	ignored subsequent working
<b>bod</b>	given benefit of doubt
<b>wr</b>	work replaced by candidate
<b>fb</b>	formulae book

**Application of Mark Scheme**

No method shown:

<b>Correct answer without working</b>	<b>mark as in scheme</b>
<b>Incorrect answer without working</b>	<b>zero marks unless specified otherwise</b>

More than one method / choice of solution:

<b>2 or more complete attempts, neither/none crossed out</b>	<b>mark both/all fully and award the mean mark rounded down</b>
<b>1 complete and 1 partial attempt, neither crossed out</b>	<b>award credit for the complete solution only</b>

Crossed out work	<b>do not mark unless it has not been replaced</b>
------------------	----------------------------------------------------

Alternative solution <b>using a correct or partially correct method</b>	<b>award method and accuracy marks as appropriate</b>
-------------------------------------------------------------------------	-------------------------------------------------------

## Mathematics and Statistics B Mechanics 5 MBM5 June 2004

Question Number and Part	Solution	Marks	Total	Comments
1	<p><math>R</math> is <math>(1, 5, 5)</math></p> $\vec{PR} = \mathbf{r} - \mathbf{p} = \begin{pmatrix} -2 \\ 1 \\ 4 \end{pmatrix}$ <p>Moment is <math>(\mathbf{r} - \mathbf{p}) \times \mathbf{F} = \begin{vmatrix} i &amp; j &amp; k \\ -2 &amp; 1 &amp; 4 \\ 7 &amp; -5 &amp; 2 \end{vmatrix}</math></p> $= 22\mathbf{i} + 32\mathbf{j} + 3\mathbf{k}$	<p>M1</p> <p>A1</p> <p>M1 A1</p> <p>A1</p>	5	M2 A2 for $- [22\mathbf{i} + 32\mathbf{j} + 3\mathbf{k}]$
<b>Total</b>			<b>5</b>	
2(a)	$I = \int F dt$ $= \int_0^{0.2} 30t(0.2 - t) dt$ $= [3t^2 - 10t^3]_0^{0.2}$ $= 0.12 - 0.08$ $= 0.04$	<p>M1</p> <p>M1A1</p> <p>A1</p>	4	
(b)	<p>Using impulse = change in momentum</p> $0.04 = 0.005 (6 + v)$ $= 0.03 + 0.005v$ <p>Speed is <math>2 \text{ ms}^{-1}</math></p>	<p>M1</p> <p>A1✓</p> <p>B1</p> <p>A1✓</p>	4	<p>for 0.005</p> <p>ft dep on M2 in (a)</p>
<b>Total</b>			<b>8</b>	

**MBM5 (cont)**

Question Number and Part	Solution	Marks	Total	Comments
3(a)	Using transverse component of acceleration is $r \frac{d^2\theta}{dt^2}$	B1		
	$ml \frac{d^2\theta}{dt^2} = -mg \sin\theta$	M1		
	$\frac{d^2\theta}{dt^2} = -\frac{g \sin\theta}{l}$			
	For small angles, $\sin\theta \approx \theta$	B1		
	$\therefore \frac{d^2\theta}{dt^2} = -\frac{g\theta}{l}$	A1	4	sc 3 if lost ‘-’ sign
(b)(i)	$A = \frac{\pi}{20}$	B1		
	$\omega = \frac{1}{2}\sqrt{g}$	B1		
	$\alpha = 0$	B1	3	
(ii)	When change in $\theta$ is $\frac{3\pi}{40}$ ,			
	$\theta = -\frac{\pi}{40}$ ,	M1 A1		
	$-\frac{1}{2} = \cos \frac{1}{2}\sqrt{g}t$	B1		For $-\frac{1}{2}$
	$\frac{1}{2}\sqrt{g}t = \frac{2\pi}{3}$	M1		
	$t = \frac{4\pi}{3\sqrt{g}}$	A1	5	
	<b>Total</b>		<b>12</b>	
4	$m = M + \lambda t$ Initial $m \rightarrow v$ Final $m + \delta m \rightarrow v + \delta v$ Conservation of linear momentum $mv = (m + \delta m)(v + \delta v)$ $mv = mv + v\delta m + m\delta v$ (to first order of $\delta$ terms) $0 = m\delta v + v\delta m$ $\therefore (M + \lambda t) \frac{dv}{dt} + v \frac{dm}{dt} = 0$ $\frac{dm}{dt} = \lambda$ $\Rightarrow \therefore (M + \lambda t) \frac{dv}{dt} + v\lambda = 0$	B1    M1A1    M1  B1  A1	          6	
	<b>Total</b>		<b>6</b>	

## MBM5 (cont)

Question Number and Part	Solution	Marks	Total	Comments
5(a)	Distance perpendicular to slope: $S = V \sin 20 t - \frac{1}{2} g \cos 20 t^2$ Strikes slope when $s = 0$ $t = \frac{2V \sin 20}{g \cos 20} \quad [t = 0 \text{ not required}]$ Velocity perpendicular to slope $V_{\text{perp}} = V \sin 20 - g \cos 20 t$ $= V \sin 20 - g \cos 20 \frac{2V \sin 20}{g \cos 20}$ $= -V \sin 20$ $[= -0.342V]$ Velocity along slope $V_{\text{along}} = V \cos 20 + g \sin 20 t$ $= V \cos 20 + g \sin 20 \frac{2V \sin 20}{g \cos 20}$ $= \frac{V}{\cos 20} (\cos^2 20 + 2 \sin^2 20)$ $= 1.19V$	M1 A1 A1  M1 A1 M1  A1  M1  A1  A1	9	Could be stated M1 A1 Accept $V \sin 20$
(b)	After rebounding from plane, velocity along the plane is $1.19V$ Velocity perpendicular to the plane is $\frac{1}{3} \times 0.342V = 0.114V$ $\therefore$ Angle direction makes with the plane is  $\tan^{-1} \frac{0.114}{1.19}$ $= 5.48^\circ$	B1  M1A1   M1 A1	5	5.4785.. accept 5.47
<b>Total</b>			<b>14</b>	

## MBM5 (cont)

Question Number and Part	Solution	Marks	Total	Comments
6(a)	CF $\ddot{x} + \dot{x} = 0$ $x = Ae^{nt}$ $n^2 + n = 0$ $n = 0, -1$ $x = A + Be^{-t}$  PI $x = C\cos 2t + D\sin 2t$ $-4C\cos 2t - 4D\sin 2t - 2C\sin 2t + 2D\cos 2t$ $= k\sin 2t$ $-4C + 2D = 0$ and $-4D - 2C = k$ $C = -\frac{k}{10}$ ; $D = -\frac{k}{5}$ $x = A + Be^{-t} - \frac{k}{10}\cos 2t - \frac{k}{5}\sin 2t$ $t = 0, x = a$ $a = A + B - \frac{k}{10}$ $\dot{x} = -Be^{-t} + \frac{k}{5}\sin 2t - \frac{2k}{5}\cos 2t$ $t = 0, \dot{x} = 0$ ; $0 = -B - \frac{2k}{5}$ $B = -\frac{2k}{5}$ $A = a + \frac{k}{10} - B$ $A = a + \frac{k}{2}$ $x = a + \frac{k}{2} - \frac{2k}{5}e^{-t} - \frac{k}{10}\cos 2t - \frac{k}{5}\sin 2t$	M1 A1 A1 M1  A1 A1✓ A1✓ M1✓ A1  A1 A1	11	Need both terms  A1 if at least one correct  ft dep on M2 above  ft dep on M2 above
b	If $e^{-t}$ term may be ignored, range of $\frac{k}{10}\cos 2t + \frac{2k}{10}\sin 2t$ using $a\cos\theta + b\sin\theta = R\cos(\theta - \alpha)$ is $\pm \frac{k\sqrt{5}}{10}$ $\therefore$ values are $a + \frac{k}{2} - \frac{k\sqrt{5}}{10}$ and $a + \frac{k}{2} + \frac{k\sqrt{5}}{10}$ These are $a + 0.276k$ and $a + 0.7236k$	M1 M1 A1 A1✓	4	M1 [Max/min]  ft dep on all M gained in (a)  if differentiation used, sc 2 for either
	<b>Total</b>		<b>15</b>	
	<b>TOTAL</b>		<b>60</b>	