

GCE 2005

January Series



Mark Scheme

Mathematics and Statistics B

(MBM3)

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Dr Michael Cresswell Director General

Key to Mark Scheme

| | | |
|---------------------------|---|---------------------|
| M | mark is for | method |
| m | mark is dependent on one or more M marks and is for | method |
| A | mark is dependent on M or m marks and is for | accuracy |
| B | mark is independent of M or m marks and is for | method and accuracy |
| E | mark is for | explanation |
| ✓ or ft or F | follow through from previous | incorrect result |
| CAO | correct answer only | |
| AWFW | anything which falls within | |
| AWRT | anything which rounds to | |
| AG | answer given | |
| SC | special case | |
| OE | or equivalent | |
| A2,1 | 2 or 1 (or 0) accuracy marks | |
| -x EE | deduct x marks for each error | |
| NMS | no method shown | |
| PI | possibly implied | |
| SCA | substantially correct approach | |
| c | candidate | |
| SF | significant figure(s) | |
| DP | decimal place(s) | |

Abbreviations used in Marking

| | |
|----------------------------------|---------------------------------|
| MC – x | deducted x marks for mis-copy |
| MR – x | deducted x marks for mis-read |
| ISW | ignored subsequent working |
| BOD | given benefit of doubt |
| WR | work replaced by candidate |
| FB | formulae booklet |

Application of Mark Scheme

No method shown:

| | |
|---------------------------------------|---------------------------------------|
| Correct answer without working | mark as in scheme |
| Incorrect answer without working..... | zero marks unless specified otherwise |

More than one method/choice of solution:

| | |
|---|--|
| 2 or more complete attempts, neither/none crossed out | mark both/all fully and award the mean mark rounded down |
| 1 complete and 1 partial attempt, neither crossed out | award credit for the complete solution only |

Crossed out work

do not mark unless it has not been replaced

Alternative solution using a correct or partially correct method

award method and accuracy marks as appropriate

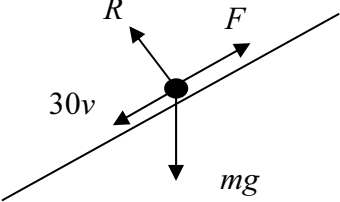
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| Question Number and part | Solution | Marks | Total | Comments |
|--------------------------|---|----------------|-----------|--|
| 1(a) | $4^2 = 20^2 + 2 \times 48a$ $a = \frac{16 - 400}{96} = -4 \text{ ms}^{-2}$ | M1 A1 | 2 | Use of constant acceleration equation to find a ag Correct acceleration from correct working |
| (b) | $0^2 = 4^2 + 2 \times (-4)s$ $s = \frac{16}{8} = 2 \text{ m}$ | M1 A1 A1 | 3 | use of constant acceleration equation to form equation for s Correct equation Correct s |
| (c) | $0 = 20 - 4t$ $t = 5$ | M1 A1 | 2 | Use of constant acceleration equation to form equation for t Correct t |
| (d) | $-F - 200 = 1100 \times (-4)$ $F = 4200$ | M1 A1 A1 | 3 | Three term equation of motion Correct equation Correct F |
| Total | | | 10 | |
| 2(a) | $R = 2 \times 9.8 \cos 40^\circ$ $F = 0.3 \times 2 \times 9.8 \cos 40^\circ$ $= 4.50 \text{ N}$ | M1 M1 A1 | 3 | Resolving perpendicular to the slope. Use of $F = \mu R$ Correct F |
| (b) | $2a = -2 \times 9.8 \sin 40^\circ - 4.50$ $a = \frac{-2 \times 9.8 \sin 40^\circ - 4.50}{2} = -8.55 \text{ ms}^{-2}$ | M1 A1 A1 | 3 | Three term equation of motion Correct equation Correct acceleration |
| Total | | | 6 | |
| 3(a) | $\mathbf{v} = -4e^{-t}\mathbf{i} + (6 - 3e^{-t})\mathbf{j}$ $t = 0$ $\mathbf{v} = -4\mathbf{i} + 3\mathbf{j}$ | M1 A1 A1 | 3 | Differentiating position vector Correct velocity Substituting $t = 0$ to obtain initial velocity |
| (b) | $\mathbf{a} = 4e^{-t}\mathbf{i} + 3e^{-t}\mathbf{j}$ | M1 A1 | 2 | Differentiating velocity Correct acceleration |
| (c) | $\mathbf{a} = 4\mathbf{i} + 3\mathbf{j}$ $a = \sqrt{4^2 + 3^2} = 5$ | M1 A1 | 2 | Finding acceleration when $t = 0$ Correct magnitude |
| (d) | $\mathbf{v} \rightarrow 0\mathbf{i} + 6\mathbf{j}$ | B1 B1 | 2 | For \mathbf{i} component For \mathbf{j} component |
| Total | | | 9 | |

MBM3 (cont)

| Question Number and part | Solution | Marks | Total | Comments |
|--------------------------|--|---------------------------------|-----------|--|
| 4(a) | $EPE = \frac{1}{2} \times \frac{40}{2} \times 3^2 = 90 \text{ J}$ | M1 A1 | 2 | Finding EPE ag Correct EPE from correct working |
| (b) | $90 = \frac{1}{2} \times 5v^2$ $v^2 = 36$ $v = 6$ | M1 A1 A1 | 3 | Use of EPE = KE Correct equation ag Correct speed from correct working |
| (c) | $EPE = \frac{1}{2} \times \frac{40}{2} \times 1^2 = 10 \text{ J}$ $90 - 10 = \frac{1}{2} \times 5v^2$ $v^2 = 32$ $v = 5.66 \text{ ms}^{-1}$ (to 3 sf) | M1 A1 M1 A1 A1 | 5 | Finding EPE 3 metres from <i>O</i> Correct EPE Using EPE lost = KE Correct equation Correct speed |
| | | | 10 | |
| 5(a) | $P = 2000$ $Q = 100$ | B1 B1 | 2 | Correct value for <i>P</i> Correct value for <i>Q</i> |
| (b) | $a = -\frac{F}{1000} = \frac{t}{10} - 2$ | M1 A1 | 2 | Use of $F = ma$ ag Correct expression from correct working |
| (c) | $v = \frac{t^2}{20} - 2t + c$ $0 = \frac{20^2}{20} - 2 \times 20 + c$ $c = 20$ $v = \frac{t^2}{20} - 2t + 20$ | M1 A1 M1 A1 | 4 | Integrating acceleration to give velocity Correct velocity with or without <i>c</i> Finding <i>c</i> Correct expression for the velocity |
| (d) | $s = \int_0^{20} \frac{t^2}{20} - 2t + 20 \text{ dt}$ $= \left[\frac{t^3}{60} - t^2 + 20t \right]_0^{20}$ $= 133 \text{ m}$ | M1 A1 A1 M1 A1✓ | 5 | Integrating velocity Correct integral Correct limits / value of <i>c</i> Finding distance by substituting limits Correct distance ft incorrect constants from (b) |
| Total | | | 13 | |

MBM3 cont

| Question Number and part | Solution | Marks | Total | Comments |
|--------------------------|--|--------------------------------|-----------|--|
| 6(a) |  | B1 | 1 | Correct force diagram |
| (b) | $F = 1500g \cos 85^\circ + 300$ $P = (1500g \cos 85^\circ + 300) \times 10$ $= 15800 \text{ W (to 3 sf)}$ | M1 A1 M1 A1 | 4 | Finding F Correct F Use of $P = Fv$ ag Correct answer from correct working |
| (c) | $F = 1500g \cos 85^\circ + 30v$ $35000 = v(1500g \cos 85^\circ + 30v)$ $0 = 30v^2 + 1281v - 35000$ $v = \frac{-1281 \pm \sqrt{1281^2 + 4 \times 30 \times 35000}}{2 \times 30}$ $= 18.9 \text{ or } -61.6$ | M1 A1 m1 A1 m1 | | F in terms of v Correct expression for F Using $P = Fv$ to obtain a quadratic Correct quadratic Solving quadratic equation |
| | Max Speed = 18.9 ms ⁻¹ | A1 | 6 | Correct speed |
| | Total | | 11 | |

MBM3 (cont)

| Question Number and part | Solution | Marks | Total | Comments |
|--------------------------|--|-----------------------------------|-----------|---|
| 7(a) | $\mathbf{v} = (3\mathbf{i} - 10\mathbf{j}) + (4\mathbf{i} + 2\mathbf{j})t$ $= (3 + 4t)\mathbf{i} + (2t - 10)\mathbf{j}$ | M1 A1 | 2 | Use of $\mathbf{v} = \mathbf{u} + \mathbf{a}t$ ag Correct result from correct working |
| (b) | $2t - 10 = 0$ $t = 5$ | M1 A1 | 2 | j component equal to zero Correct time |
| (c)(i) | $\mathbf{r} = (3\mathbf{i} - 10\mathbf{j}) \times 10 + \frac{1}{2}(4\mathbf{i} + 2\mathbf{j}) \times 10^2$ $= 230\mathbf{i}$ | M1 A1 A1 | 3 | Finding r when $t = 10$ Correct expression Correct final answer |
| (c)(ii) | $\mathbf{v} = (3 + 4 \times 10)\mathbf{i} + (2 \times 10 - 10)\mathbf{j}$ $= 43\mathbf{i} + 10\mathbf{j}$ | B1 | 1 | Correct velocity |
| (d) | $\mathbf{r} = 230\mathbf{i} + (43\mathbf{i} + 10\mathbf{j}) \times 10$ $= 660\mathbf{i} + 100\mathbf{j}$ $r = \sqrt{660^2 + 100^2}$ $= 668 \text{ m}$ | M1 M1 A1 A1 M1 A1✓ | 6 | Uses zero acceleration Uses both answers from (c) Correct expression for r Correct simplified result Finding magnitude Correct distance Follow through from part (c) |
| Total | | | 14 | |
| 8(a) | $a = 0.6 \times 10^2 = 60 \text{ ms}^{-2}$ | M1 A1 | 2 | Use of $a = r\omega^2$ Correct acceleration |
| (b) | $R = 0.05 \times 60 = 3 \text{ N}$ | M1 A1✓ | 2 | Finding product of mass and acceleration Correct R |
| (c) | $R - 0.05 \times 9.8 = 0.05 \times 60$ $R = 3.49 \text{ N}$ | M1 A1 A1✓ | 3 | Follow though incorrect a . Equation of motion at lowest point Correct equation Correct R Follow though incorrect a . |
| Total | | | 7 | |
| TOTAL | | | 80 | |