## GCE 2004 June Series

ASSESSMENT and
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ALLIANCE

## Mark Scheme

## Mathematics and Statistics B MBD1

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## Key to Mark Scheme

| M | mark is for | method |
| :---: | :---: | :---: |
| m | mark is dependent on one or more M marks and is for | method |
| A | mark is dependent on M or m marks and is for | accuracy |
| B | mark is independent of M or m marks and is for | accuracy |
| E | mark is for | explanation |
| $\checkmark$ or ft or F |  | follow through from previous incorrect result |
| cao |  | correct answer only |
| cso |  | correct solution only |
| awfw |  | anything which falls within |
| awrt |  | anything which rounds to |
| acf |  | any correct form |
| ag |  | answer given |
| sc |  | special case |
| oe |  | or equivalent |
| sf |  | significant figure(s) |
| dp |  | decimal place(s) |
| A2,1 |  | 2 or 1 (or 0 ) accuracy marks |
| $-x$ ee |  | deduct $x$ marks for each error |
| pi |  | possibly implied |
| sca |  | substantially correct approach |

## Abbreviations used in Marking

| MC $-\boldsymbol{x}$ |
| :--- |
| MR $-\boldsymbol{x}$ |
| isw |
| bod |
| wr |
| fb |

deducted $x$ marks for mis-copy deducted $x$ marks for mis-read ignored subsequent working given benefit of doubt work replaced by candidate formulae book

## Application of Mark Scheme

No method shown:

Correct answer without working
Incorrect answer without working
More than one method / choice of solution:
2 or more complete attempts, neither/none crossed out
1 complete and 1 partial attempt, neither crossed out
Crossed out work
Alternative solution using a correct or partially correct method
mark as in scheme zero marks unless specified otherwise
mark both/all fully and award the mean mark rounded down
award credit for the complete solution only
do not mark unless it has not been replaced
award method and accuracy marks as appropriate

## Mathematics and Statistics B Discrete 1 MBD1 June 2004

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 1 (a) | $\mathbf{A}$ $\mathbf{B}$ $\mathbf{C}$ flow <br> 0 0 0 0 <br> 0 0 1 0 <br> 0 1 0 0 <br> 0 1 1 1 <br> 1 0 0 0 <br> 1 0 1 0 <br> 1 1 0 1 <br> 1 1 1 1 <br> The three missing labels must be $\mathrm{A} / \mathrm{B}$ in the first row and B in the second | B1 B1 <br> B1 <br> B1 <br> M1 A1 <br> A1 | 4 3 | Second entry <br> Third \& fourth <br> Fifth \& sixth <br> Seventh \& eighth |
|  | Total |  | 7 |  |
| 2 (a) | CADEBFMLKJC | M1 A1 | 2 |  |
| (b) | Neither <br> More than two odd vertices | $\begin{aligned} & \text { B1 } \\ & \text { B1 } \end{aligned}$ | 2 |  |
| $\begin{array}{r} \text { (c) (i) } \\ \text { (ii) } \end{array}$ | $K L$ <br> Starting at $A$, say, we can only get to $B$ along $D E$, but then we cannot get back. | $\begin{aligned} & \text { B1 } \\ & \text { M1 } \\ & \text { A1 } \end{aligned}$ | $\begin{aligned} & 1 \\ & 2 \end{aligned}$ | (any sensible focus on the 'isthmus' $D E$ ) |
|  | Total |  | 7 |  |
| 3 (a) | Essential labels: | M1 |  |  |
|  | $B: 4 \quad E: 5 \quad$ I: $9 \quad F: 10,9$ | A1 |  | One temporary label |
|  | C:10 J: (14 poss), $13 \quad$ G: 16,14 | A1 |  | Six permanent labels |
|  | D: $15 \quad$ K: $20,19 \quad H: 20 \quad L: 24$ | A1 |  | Remaining permanent labels |
|  | Traceback to $A B C G K L$ of length 24 | M1 A1 | 6 |  |
| (b)(i) | Kruskal gives <br> $A B C G E F E I F J$ (@4) | M1 |  |  |
|  |  | A1 |  |  |
|  | AE CD GK KL (@ 5) | A1 |  |  |
|  | BC GH (@6) | A1 |  |  |
|  | $\text { Total length }=52 \mathrm{~km}$ | B1 | 5 | sc For correct tree only, with order of choice not given: 2 marks |
| (ii) |  |  |  |  |
|  |  | B1」 | 1 | ft |
| (c)(i) | $4+4+5+4+6+4+5+5=37$ | B1 | 1 |  |
| (ii) | Longest route on gritted paths $=37$, so original distance $\leq 9$. <br> Obvious contenders $J$ \& $K$ give distances 7 and 32. | M1 |  | (any sensible approach) |
|  |  | A1 | 2 |  |
|  | Total |  | 15 |  |

## MBD1 (cont)

| Question Number and Part | Solution | Marks | Total | Comments |
| :---: | :---: | :---: | :---: | :---: |
| 4 (a) (b)(i) <br> (ii) | $\mathbf{j} \Rightarrow \mathbf{u}$ false (June) <br> $\mathbf{t} \Rightarrow \sim \mathbf{y}$ true (30-days end in $\mathrm{L} / \mathrm{E} / \mathrm{R} / \mathrm{R}$ ) $(\mathbf{j} \wedge \mathbf{y}) \Rightarrow \mathbf{u}$ true (January/July) $\begin{array}{ccccccc} \mathbf{p} & \mathbf{q} & \mathbf{r} & \mathbf{I} & \mathbf{p \wedge \mathbf { q }} & \mathbf{I I} & \mathbf{I} \Rightarrow \mathbf{I I} \\ 0 & 0 & 0 & 1 & 0 & 1 & 1 \\ 0 & 0 & 1 & 1 & 0 & 1 & 1 \\ 0 & 1 & 0 & 1 & 0 & 1 & 1 \\ 0 & 1 & 1 & 1 & 0 & 1 & 1 \\ 1 & 0 & 0 & 0^{*} & 0 & 1^{*} & 1 \\ 1 & 0 & 1 & 1 & 0 & 1 & 1 \\ 1 & 1 & 0 & 0 & 1 & 0 & 1 \\ 1 & 1 & 1 & 1 & 1 & 1 & 1 \end{array}$ <br> For II true and I false we need case * e.g. p: June begins with a J $\mathbf{q}$ : June ends in a $Y$ r: June has 31 days | B1 <br> B1 B1 <br> B1 B1 <br> M1 <br> M1 <br> A1 <br> A1 <br> A1 <br> M1 <br> A1 | 2 | 8 rows <br> appropriate columns <br> $\wedge$ correct <br> any $\Rightarrow$ correct <br> all correct |
|  | Total |  | 12 |  |
| 5 (a) | Line 1: $3 x+2 y=42$ <br> Line 2: $x+2 y=30$ <br> Line 3: $x+y=16$ | B1 <br> B1 | 2 | For one <br> For other two |
| (b) | $\begin{aligned} & \begin{array}{l} 3 x+2 y=42, x+y=16 \Rightarrow \\ x=10, y=6 \end{array} \\ & \text { Hence } C \text { is }(10,6) \end{aligned}$ | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { A1 } \end{aligned}$ | 3 | For either coordinate |
| (c) | Trying all vertices leads to $P=2 x+3 y$ maximised at $(2,14)$ So maximum of $P$ is 46 by making 2 Xtremes and 14 Yltras | $\begin{gathered} \text { M1 } \\ \text { A1 A1 } \\ \text { A1 } \end{gathered}$ | 4 | (or by lines/gradients) |
| (d)(i) (ii) | New contraint is $y \leq 0.2(x+y)$ and so $4 y \leq x$. <br> This crosses the boundary of the feasible region at $(12,3)$. <br> In new region maximum of $P$ is at $(12,3)$ so they should make 12 Xtremes and 3 Yltras | $\begin{aligned} & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \text { A1 } \\ & \text { M1 } \\ & \\ & \text { A1 } \end{aligned}$ | 2 4 |  |
|  | Total |  | 15 |  |

MBD1 (cont)


