

# Mark scheme January 2004

## **GCE**

### **Mathematics A**

### **Unit MAD2**

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#### **Key to mark scheme**

M	mark is for	method
m	mark is dependent on one or more M marks and is for	method
A	mark is dependent on M or m mark and is for	accuracy
В	mark is independent of M or m marks and is for	method and accuracy
E	mark is for	explanation
$$ or ft or $\mathbf{F}$		follow through from previous
		incorrect result
CAO		correct answer only
AWFW		anything which falls within
<b>AWRT</b>		anything which rounds to
AG		answer given
SC		special case
OE		or equivalent
A2,1		2 or 1 (or 0) accuracy marks
-x EE		Deduct x marks for each error
NMS		No method shown
PI		Perhaps implied
c		Candidate

### Abbreviations used in marking

MC-x	deducted x marks for miscopy
MR-x	deducted x marks for misread
ISW	ignored subsequent working
BOD	gave benefit of doubt
WR	work replaced by candidate

### Application of mark scheme

Correct answer without working	mark as in scheme
Incorrect answer without working	zero marks unless specified otherwise

Award method and accuracy marks as appropriate to an alternative solution using a correct method or partially correct method.

Q	Solution	Marks	Total	Comments
1	$\begin{bmatrix} 1 & 3 & 2 & 1 \\ 8 & 10 & 9 & 10 \\ 7 & 9 & 8 & 7 \\ 3 & 2 & 4 & 1 \end{bmatrix} \begin{bmatrix} 1 \\ 8 \\ 7 \\ 1 \end{bmatrix}$	M1		
	$ \begin{bmatrix} 0 & 2 & 1 & 0 \\ 0 & 2 & 1 & 2 \\ 0 & 2 & 1 & 0 \end{bmatrix} $	A1		
	$\begin{bmatrix} 2 & 1 & 3 & 0 \end{bmatrix}$ $0 & 1 & 1 & 0$	M1		
	$ \begin{bmatrix} 0 & 1 & 0 & 0^{\bullet} \\ 0 & 1 & 0^{\bullet} & 2 \\ 0 & 0 & 0 \end{bmatrix} $	A1		OE
	4 lines = optimal			
	Match: Michael $\rightarrow A$ Rick $\rightarrow B$			or $E \to A$
	Hilary $\rightarrow C$			$R \to B$ $H \to C$
	Edwina $\rightarrow D$	B1		$M \!  o \! D$
				or $H \to A$
				$R \rightarrow B$
				$M \rightarrow C$
				$E \rightarrow D$
				or
				$E \rightarrow C$
				$H \rightarrow A$
				$M \rightarrow D$
	Total = 19	B1	6	$R \rightarrow B$
	Total	DI	6 <b>6</b>	

Q	Solution	Marks	Total	Comments
2 (a)(i)	K 22 26	M1		Forward
		A1	2	
(ii)		M1		Back
	1 r	A1	2	
	G G I G Z D I			
	16 Z H H 16 Z 16 Z 17 Z 17 Z 17 Z 17 Z 17 Z 17 Z			
	B 16 10 16 F 10 16 16 10 16 16 10 16 16 16 16 16 16 16 16 16 16 16 16 16			
	B 4 D 1 T 1			
	A 0			
(b)	CP = A C E G K			
	Min time = 26	B1	1	Both
(a)				Dom
(c)	B, D	B1	1	

Q	Solution	Marks	Total	Comments
2 (d)	26	M1		
	74			
		A2	3	−1 EE
	22			
	20			
	∞ ∞			
	92			
	41			
	2			
	9			
	4			
	7			
	3 0 0			
(e)(i)	Min time = 28	B1		
	1 worker critical path			
	other activities ⇒ J takes until 24			
	∴ overrun = 2	E1	2	
(ii)	ACEGK			
	and			
	B D F (H) I J	B1	1	H either
	Total		12	

Q	Solution	Marks	Total	Comments
3	**************************************			Working Backwards
	46° J 1 T 1 T 1 T 1 T 1 T 1 T 1 T 1 T	M1		SCA $\begin{cases} SCA & M1 \\ 7 & \text{at } L & A1 \\ 17 & \text{at } I & A1F \\ 43 & \text{at } E & A1F \\ 47 & \text{at } D & A1F \end{cases}$
	37.5	A1		at C
	23 <sup>4</sup> F	A1F		at E
	11.3 E	A1F		at I
	B 61 St 47 32 D 71	A1F		at K
	A	B1		for 54
	Route: A D C E F I L K M	B1	7	
	Total		7	

	Q	Solution	Marks	Total	Comments
4	(a)	A, B, C, D	B1	1	
	<b>(b)</b>	I	B1	1	
	(c)	20+20+10+10+40+50+30	M1		
		= 180	A1	2	
	<b>(d)</b>	$ \begin{array}{cccccccccccccccccccccccccccccccccccc$	M1		SCA
		$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$	M1		1 complete flow
		$ \begin{array}{c ccccccccccccccccccccccccccccccccccc$			
		Final: A 10 20 B  10 20 F  10 50 I 50 F			
		D $C$	A1		OE

Q	Solution	Marks	Total	Comments
4 (e)		M1		Their max – 10
	Max flow = 170	A1	2	CAO
	Total		11	

Q	Solution	Marks	Total	Comments
5 (a)(i)	$All \ge 0$	B1	1	
(ii)	P = 2.4	B1		
	n = 0.4, $y = 0.2$ , $z = 0$	B1	2	All three
<b>(b)</b>	x $y$ $z$ $r$ $s$ $P$			
	3 4 2 1 0 0 2	M1A1		Tableau
	3 4 2 1 0 0 2	M1		Pivot
	1 3 2 0 1 0 1	M1		Row reduce
	-3-6 $-2$ 0 0 1 0			
	5° 0 -2 1 -1 0 2	A1		All correct
	5 0 -2 1 -1 0 2	M1		Pivot
	1 3 2 0 1 0 1	M1		Row reduce
	_1 0 2 0 2 1 2	A1		All correct
	5 0 -2 1 -1 0 2			
	0 15 12 -1 6 0 3			
	0 0 8 1 9 5 12			
	All positive			
	$\therefore P = 2.4$			
	x = 0.4, y = 0.2, z = 0	B1	9	
	Total		12	

Q	Solution	Marks	Total	Comments
6 (a)(i)	Row min (-2, 2 -3)	M1		
	Max 2			
	Column max (3, 5, 2, 6)			
	Min 2	A1		
	2 = 2, therefore stable solution	E1	3	
(ii)	1 saddle point at (2, 3)	B1	1	
<b>(b)</b>	Colin plays I with prob $p$ , II with $(1-p)$	M1		
	Return $p(x+2)+3(1-p)$	A1		
	p(x-1)+5(1-p)	A1		
	$p(x-1) + 3 = \frac{19}{5}$	M1		equating to value
	$p(x-6) + 5 = \frac{19}{5}$			
	$p(x-1) = \frac{4}{5}$	A1		or solving for $p$ first
	$p(x-6) = -\frac{6}{5}$	A1		
	$\frac{4}{5(x-1)} = \frac{-6}{5(x-6)}$	M1		
	4x - 24 = -6x + 6			
	x = 3	A1	8	CAO
	Total		12	
	Total		60	