

## General Certificate of Education

# Mathematics 6300 Specification A

MAD1 Discrete 1

# Mark Scheme

# 2005 examination - June series

Mark schemes are prepared by the Principal Examiner and considered, together with the relevant questions, by a panel of subject teachers. This mark scheme includes any amendments made at the standardisation meeting attended by all examiners and is the scheme which was used by them in this examination. The standardisation meeting ensures that the mark scheme covers the candidates' responses to questions and that every examiner understands and applies it in the same correct way. As preparation for the standardisation meeting each examiner analyses a number of candidates' scripts: alternative answers not already covered by the mark scheme are discussed at the meeting and legislated for. If, after this meeting, examiners encounter unusual answers which have not been discussed at the meeting they are required to refer these to the Principal Examiner.

It must be stressed that a mark scheme is a working document, in many cases further developed and expanded on the basis of candidates' reactions to a particular paper. Assumptions about future mark schemes on the basis of one year's document should be avoided; whilst the guiding principles of assessment remain constant, details will change, depending on the content of a particular examination paper.



#### **Key to Mark Scheme**

M	mark is for	method
m	mark is dependent on one or more M marks and is for	method
A	mark is dependent on M or m marks and is for	accuracy
В	mark is independent of M or m marks and is for	accuracy
E	mark is for	explanation
$\sqrt{\text{or ft or F}}$		follow through from previous incorrect
		result
CAO		correct answer only
AWFW		anything which falls within
AWRT		anything which rounds to
AG		answer given
SC		special case
OE		or equivalent
A2,1		2 or 1 (or 0) accuracy marks
-x EE		deduct x marks for each error
NMS		no method shown
PI		possibly implied
SCA		substantially correct approach
c		candidate
sf		significant figure(s)
dp		decimal place(s)

#### Abbreviations used in Marking

MC-x	deducted x marks for mis-copy
MR-x	deducted x marks for mis-read
ISW	ignored subsequent working
BOD	given benefit of doubt
WR	work replaced by candidate
FB	formulae book

### **Application of Mark Scheme**

No method shown:			
Correct answer without working	mark as in scheme		
Incorrect answer without working	zero marks unless specified otherwise		
More than one method / choice of solution:			
2 or more complete attempts, neither/none crossed out	mark both/all fully and award the mean mark rounded down		
1 complete and 1 partial attempt, neither crossed out	award credit for the complete solution only		
Crossed out work	do not mark unless it has not been replaced		
Alternative solution using a correct or partially correct method	award method and accuracy marks as appropriate		

#### MAD1

Q	Solution	Marks	Total	Comments
1	V B W C X D E Z	M1		bipartite graph
		A1	2	
(b)	Initial BV, CU, DX, FZ			
	$A \rightarrow V  B \rightarrow U  C \rightarrow W$	M1A1		starting with A, W Either
	$E \rightarrow Z  F \rightarrow Y$	M1A1		starting with E, Y Order
				Or:
				$E \to X \to D \to W$
	Match:			$A \rightarrow V \rightarrow B \rightarrow U \rightarrow C \rightarrow W \rightarrow D \rightarrow X$
	AV, BU, CW, DX, EZ, FY (CX, DW)	B1	5	
	Total		7	
2(a)	23 12 17 18 5 9 19 16	M1		SCA
	5 23 9 12			4 sublists
	17 19	M1		
	16 18			
	5 9 17 16 23 12 19 18	A1		
	5 17 19 23			2 sublists
	9 12 16 18 5 9 17 12 19 16 23 18	M1		
	5 9 12 16 17 18 19 23	A1 A1	6	all correct
(b)(i)	Comparisons = 4	B1	1	
(ii)	Swaps = 3	B1	1	
	Total		8	

MAD1 (cont)

MAD1 (cont)			_	
Q	Solution	Marks	Total	Comments
3(a)	AB = 3	M1		SCA
	FG = 4	<b>A</b> 1		FG second
	ED = 5			
	FC = 6			
	BD = 7 or $AD = 7$	B1		6 edges
	CD = 9	A1	4	all correct
				an concet
(b)	Length $= 34$	B1	1	
(c)				
1	B E			B E
	^ /			
		B1		
		B1F	2	
	A D PG	DII		A D G
				1
	Č F			Č F
	Total		7	
4(a)(i)				
	# 8 - B			
	(S) (S)			
	至	N / 1		SCA
		M1		SCA
	= *	A1		3 values at D
		711		3 values at B
	z z	M1		2 values at <i>I</i>
	N N			
	2 2			
	1 N	M1		3 values at L
	[2]			
	**	A 1		all aggregat
	~ ^a \	A1		all correct
	4			
	# N	B1	6	45 at <i>L</i>
		Б1	Ü	ie ucz
	* \ / "			
	¥0			
(ii)	ACDEFHJL	B1	1	
(b)(i)	Odd vertices at $A$ and $L$	M1		
	Total (155) (+ their 45)	M1		
	= 200	A1	3	CAO
(ii)	Order of $F = 4 + 2 = 6$			
()	∴ F appears 3 times	B1	1	
	Total	וע	11	
	1 Utai		11	

MAD1 (cont)

Q	Solution	Marks	Total	Comments
5(a)	A B C D E A			
	7 8 5 10 3			
	= 33	B1	1	
(b)	Tour; may be improved	E1E1	2	
(c)	$A \rightarrow E \rightarrow C \rightarrow D \rightarrow B \rightarrow A$ $3  4  5  6  7$ $= 25$	M1 M1 A1 B1	4	tour visits all vertices correct order
(d)	MST			
	E B C	M1		MST with 3 edges
	= 4+5+6=15 Add 3+7 $15+10=25$	A1 M1 A1	4	or $15 + 2 \times 3 = 21$
(e)	Cannot be lower than a lower bound	E1	1	
	Total		12	

MAD1 (cont)

Q	Solution	Marks	Total	Comments
6(a)	$y \ge \frac{1}{2}x \Rightarrow 2y \ge x$	B1		
	$20x + 10y \le 600 \text{ so } 2x + y \le 60$	B1	2	
	$20x + 10y \le 600$ so $2x + y \le 60$	DI	2	
(b)	$x \ge 5, \ y \ge 5, \ y \le 25$	B1		all correct
	P = 3x + y	B1	2	
(c)	y •	B1×2		diagonal lines
	60	B1		$x \ge 5, y \ge 5, y \le 25$
	50-			
	40-			
	30			
	20-			
	PK PK			
	10-			
	0	B1		feasible region
	0 10 20 30 x	B1	5	objective line
(d)	Max at $x = 24$ , $y = 12$	M1		
	P = 84	A1	2	
(e)	P = 2x + 2y			
	Max at (17.5,25)	M1		
	Not integers	B1,B1		
	Values $(17,25)$ and $(18,24)$ give $P = 510 (6 \text{ hrs}) + 84 (1 \text{hr})$	D1,D1		
	= £594	A1	4	CAO
	Total	711	15	
	TOTAL		60	